



AI Bridge

Lecture 4

SUPERVISED LEARNING

Supervised learning

- “**Supervised learning (SL)** is the [machine learning](#) task of learning a function that [maps](#) an input to an output based on example input-output pairs. It infers a function from *labeled [training data](#)* consisting of a set of *training examples*.” – Wikipedia
- Most widely used ML techniques in real world applications.

Supervised Learning

- Classification:

- Predicting a label/class/category
- Ex: spam or not, cancer or not, cat or dog, red wine vs. white wine

- Regression:

- Predicting a (continuous) quantity
- Ex: Survival rate, wine quality, yield prediction

Example

- You're running a company, and you want to develop learning algorithms to address each of two problems.
 - Problem 1: You have a large inventory of identical items. You want to predict how many of these items will sell over the next 3 months.
 - Problem 2: You'd like software to examine individual customer accounts, and for each account decide if it has been hacked/compromised.
- Are they classification or regression?

Conversion



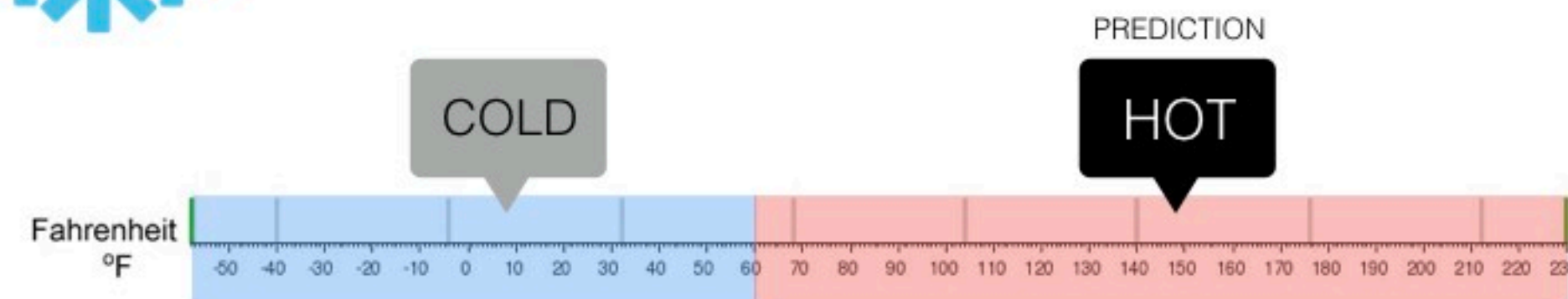
Regression

What is the temperature going to be tomorrow?



Classification

Will it be Cold or Hot tomorrow?



Example

- You're running a company, and you want to develop learning algorithms to address each of two problems.
 - Problem 1: You have a large inventory of identical items. You want to predict how many of these items will sell over the next 3 months.
- Can we formulate it as a classification problem?

Ok, so, like...

what *is* Artificial Intelligence?

what *is* Artificial Intelligence

~~what is Artificial Intelligence~~

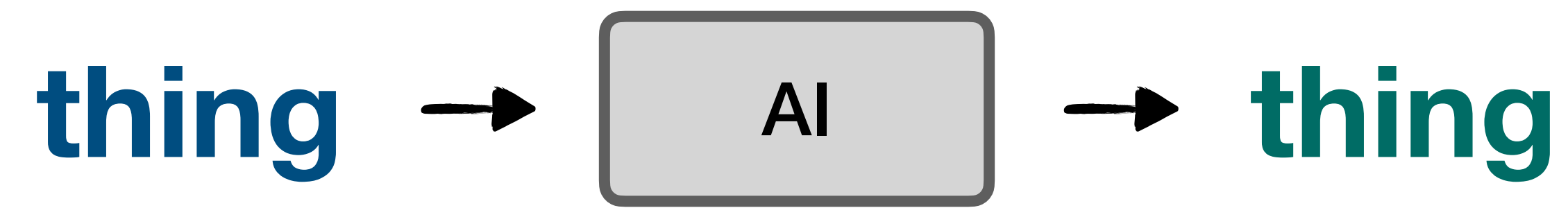
what can Artificial Intelligence do

...not everything

what can Artificial Intelligence do

“Given a thing, tell you a thing.”

what can Artificial Intelligence do



what can Artificial Intelligence do



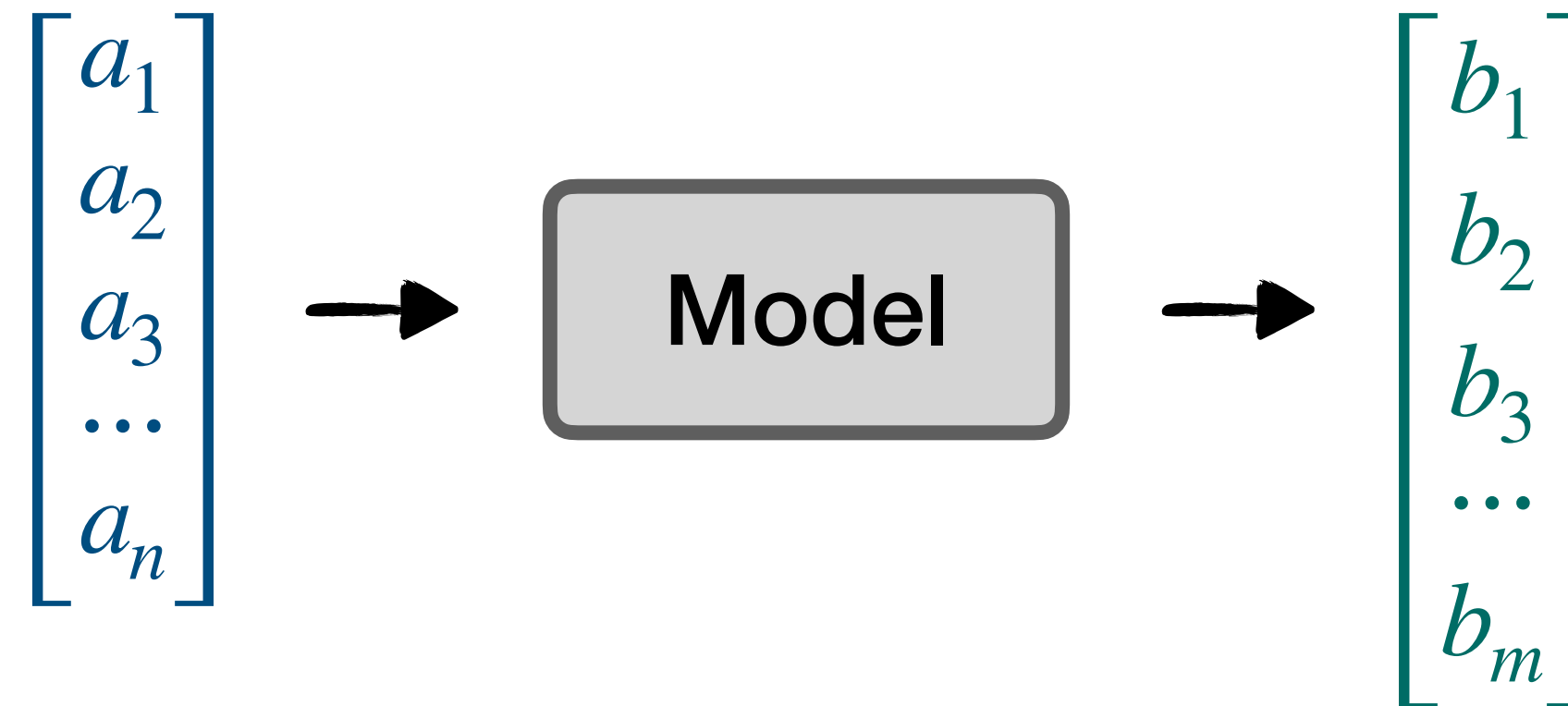
- models map **inputs** to **outputs**

what can Artificial Intelligence do



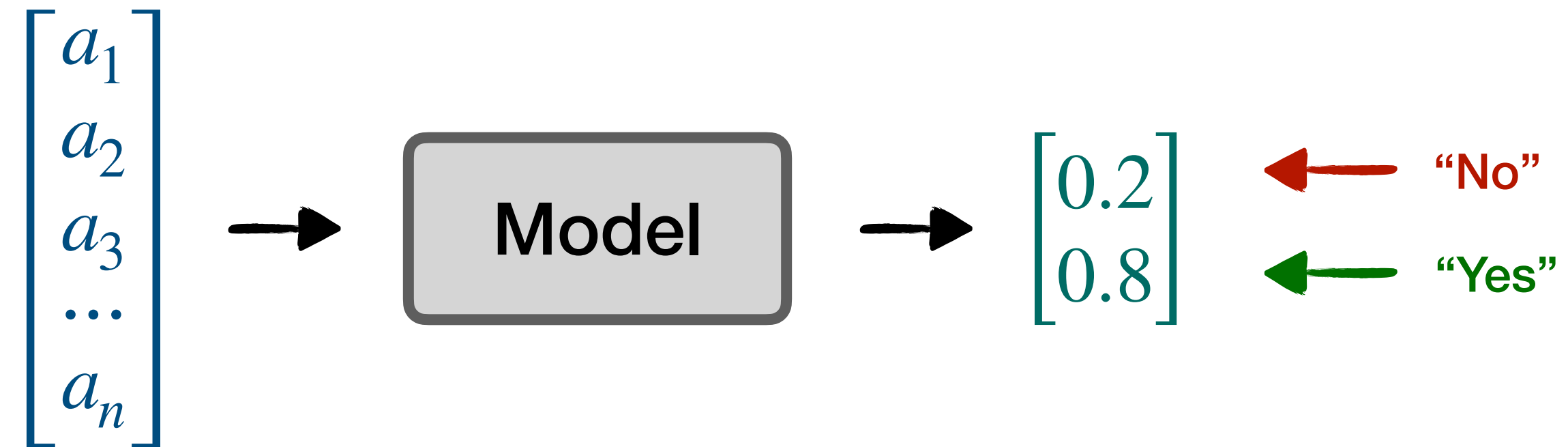
functions
models map **inputs** to **outputs**

what can Artificial Intelligence do



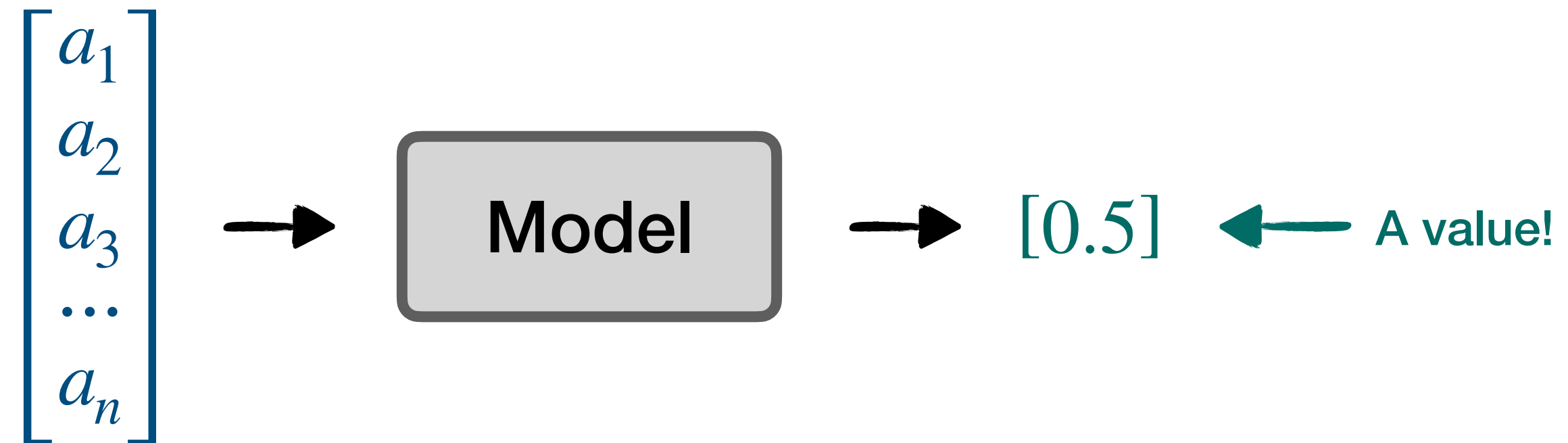
models are $\mathbb{R}^n \rightarrow \mathbb{R}^m$ functions

what can Artificial Intelligence do



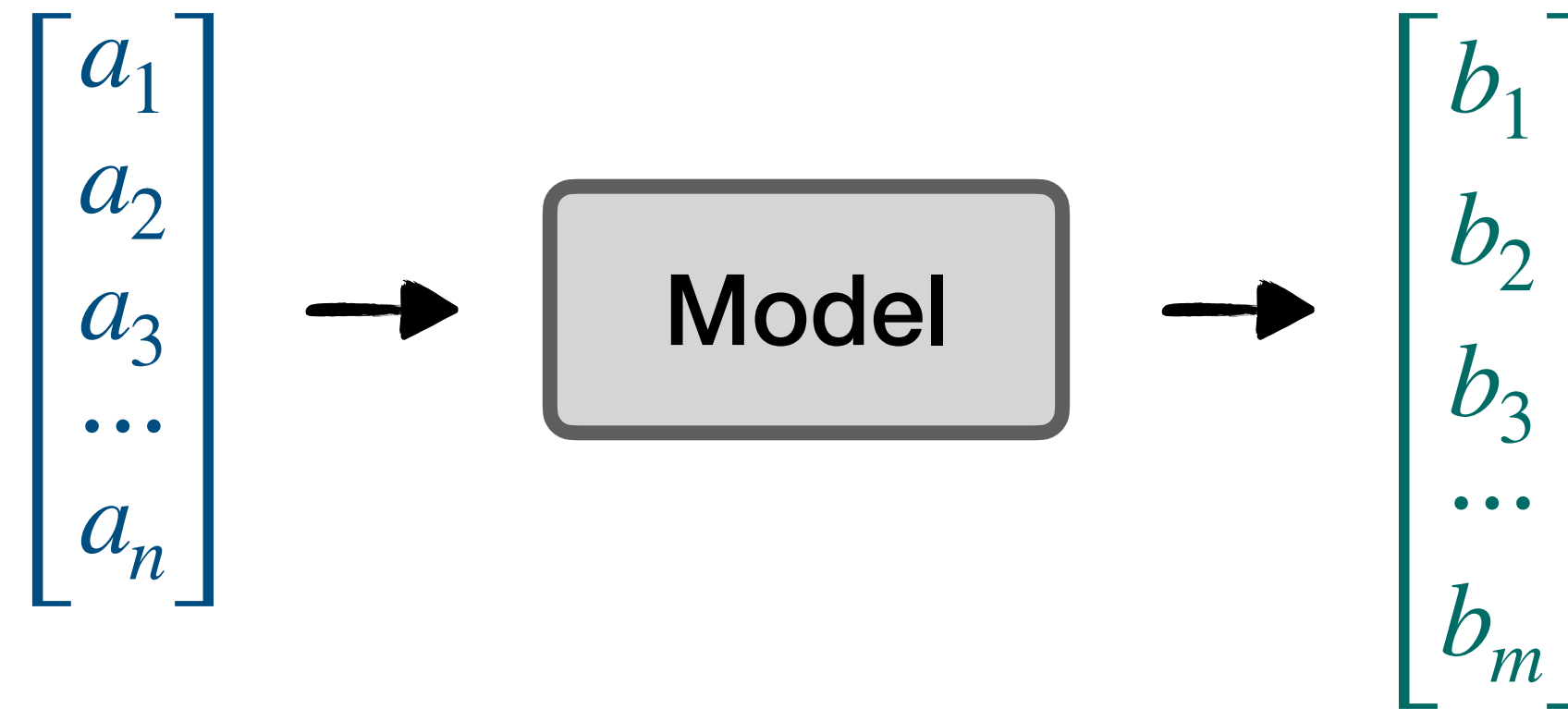
models are $\mathbb{R}^n \rightarrow \mathbb{R}^2$ functions

what can Artificial Intelligence do



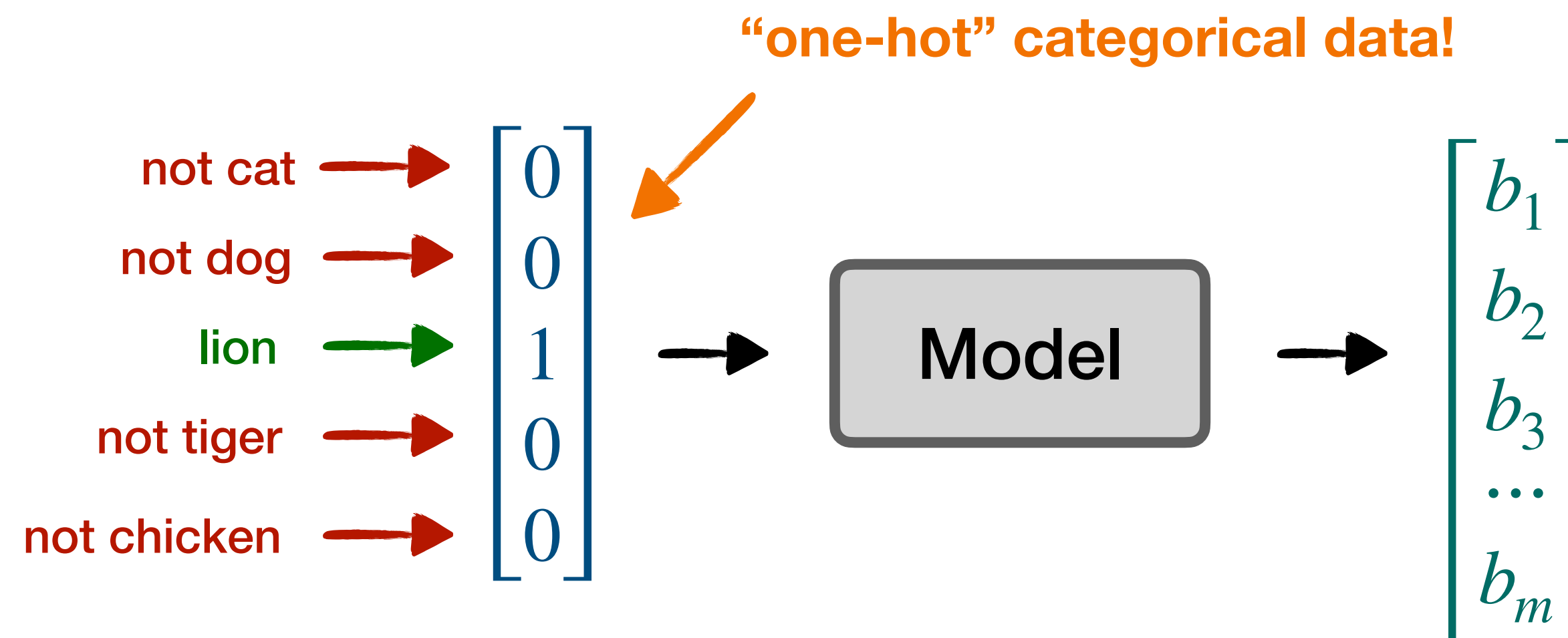
models are $\mathbb{R}^n \rightarrow \mathbb{R}^1$ functions

what can Artificial Intelligence do



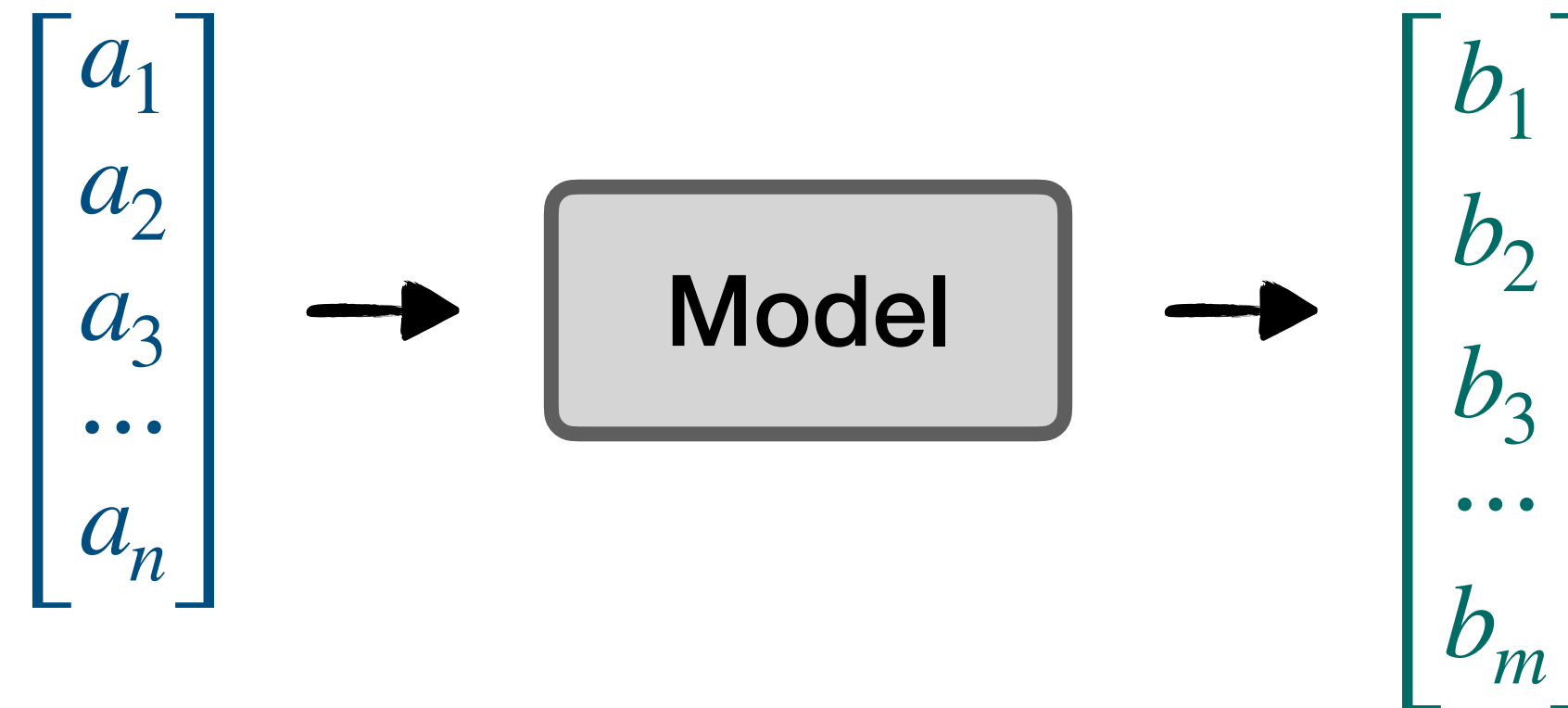
models are $\mathbb{R}^n \rightarrow \mathbb{R}^m$ functions

what can Artificial Intelligence do



models are $\mathbb{R}^n \rightarrow \mathbb{R}^m$ functions

what can Artificial Intelligence do



- by changing the shapes of input and output, models can represent a lot of different problems

we will get to those

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Wine Quality Data Set

Download: [Data Folder](#), [Data Set Description](#)

Abstract: Two datasets are included, related to red and white vinho verde wine samples, from the north of Portugal. The goal is to model wine quality based on physicochemical tests (see [Cortez et al., 2009], [[Web Link](#)]).



Data Set Characteristics:	Multivariate	Number of Instances:	4898	Area:	Business
Attribute Characteristics:	Real	Number of Attributes:	12	Date Donated	2009-10-07
Associated Tasks:	Classification, Regression	Missing Values?	N/A	Number of Web Hits:	1891084

Source:

Paulo Cortez, University of Minho, Guimarães, Portugal, <http://www3.dsi.uminho.pt/pcortez>
A. Cerdeira, F. Almeida, T. Matos and J. Reis, Viticulture Commission of the Vinho Verde Region(CVRVV), Porto, Portugal
@2009

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 @2009

1. Fixed acidity
2. Volatile acidity
3. Citric acid
4. Residual sugar
5. Chlorides
6. Free sulfur dioxide
7. Total sulfur dioxide
8. Density
9. pH
10. Sulphates
11. Alcohol
12. White/Red
13. Quality

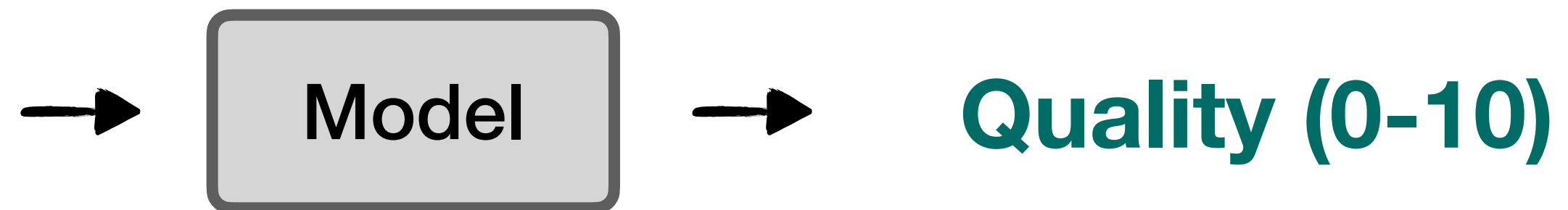
- Fixed acidity
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- Density
- pH
- Sulphates
- Alcohol
- White/Red



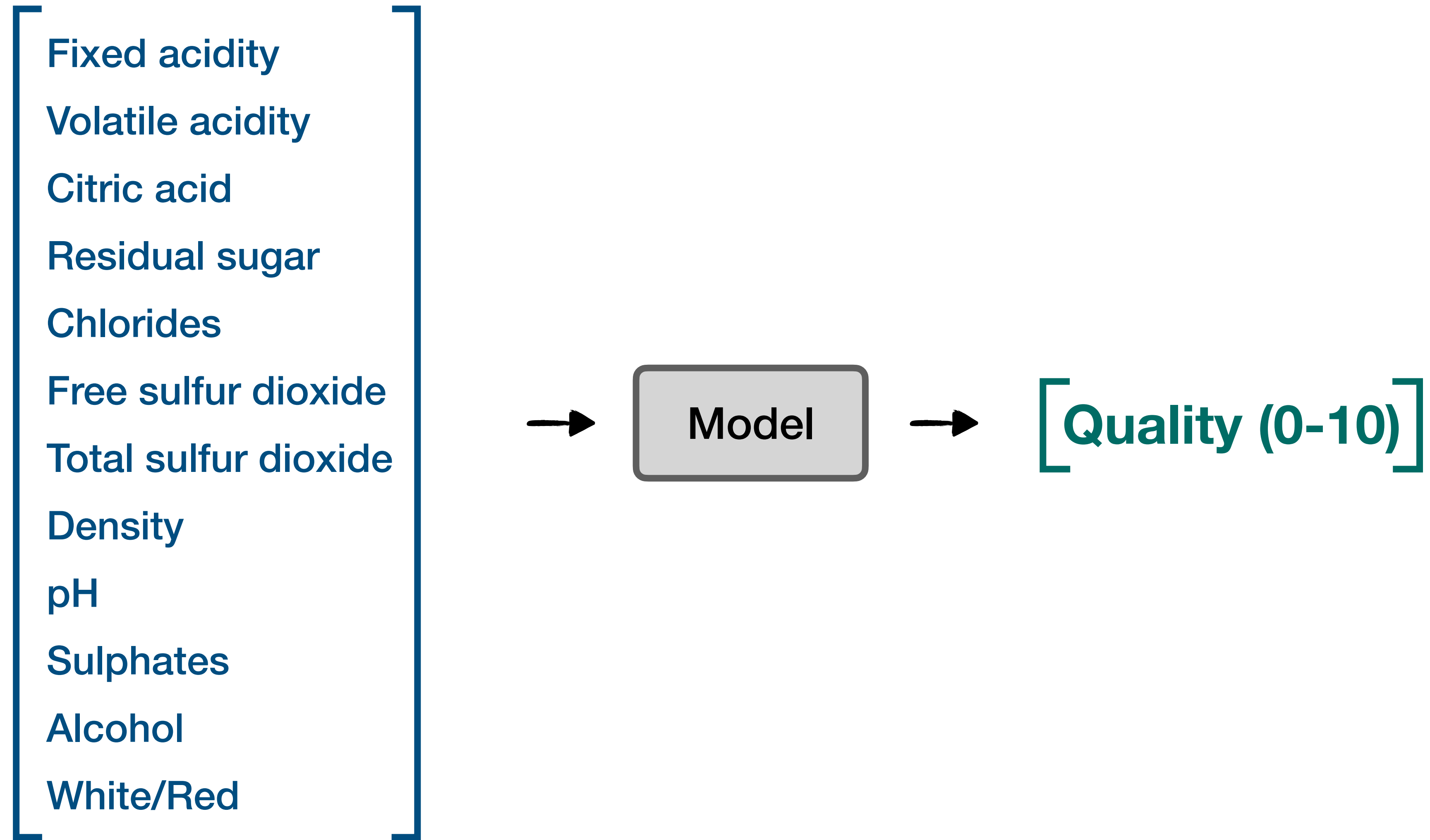
Quality (0-10)

Linear Regression

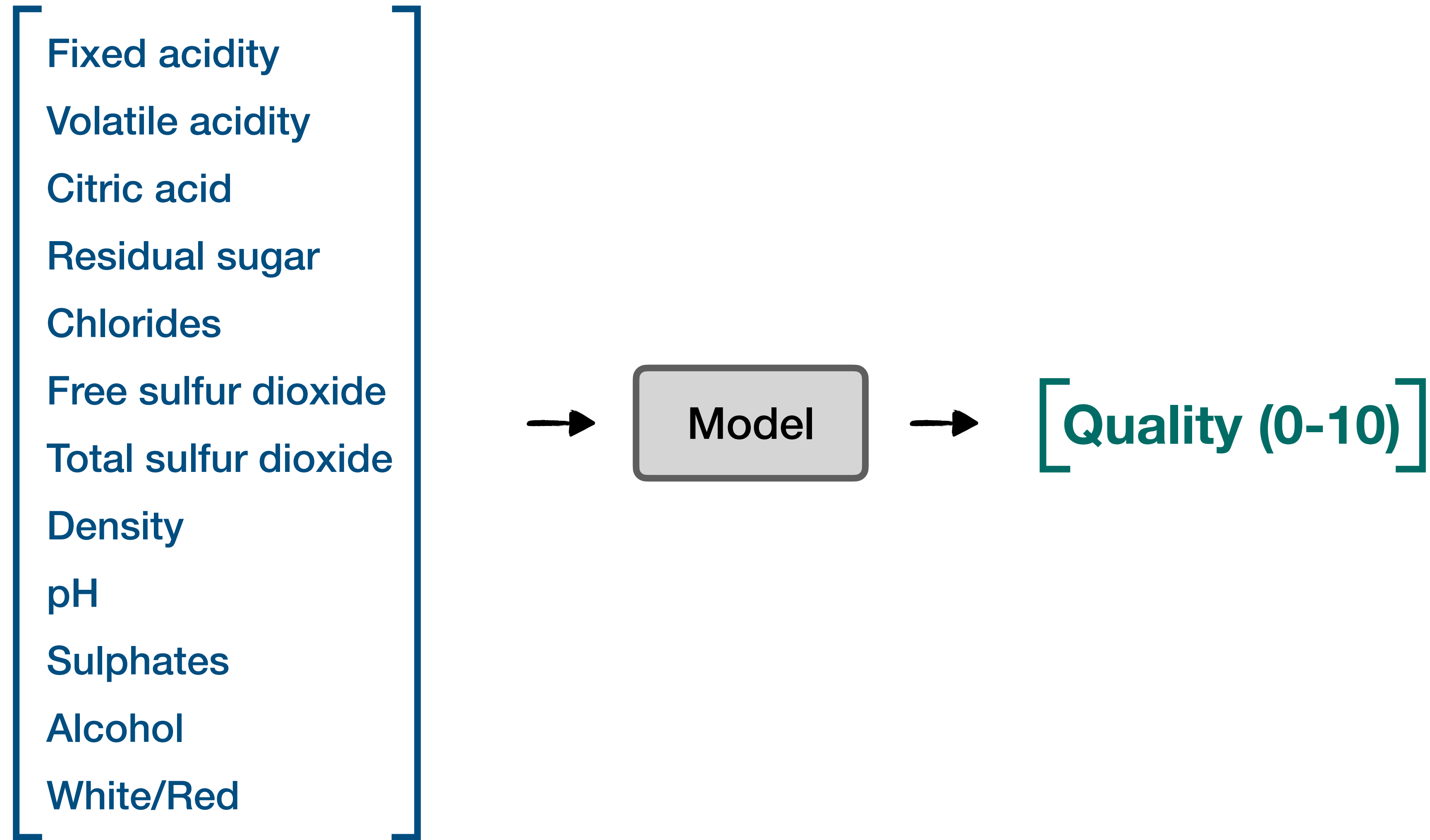
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Linear Regression



Linear Regression



this model could be a $\mathbb{R}^{12} \rightarrow \mathbb{R}^1$ function

Linear Regression

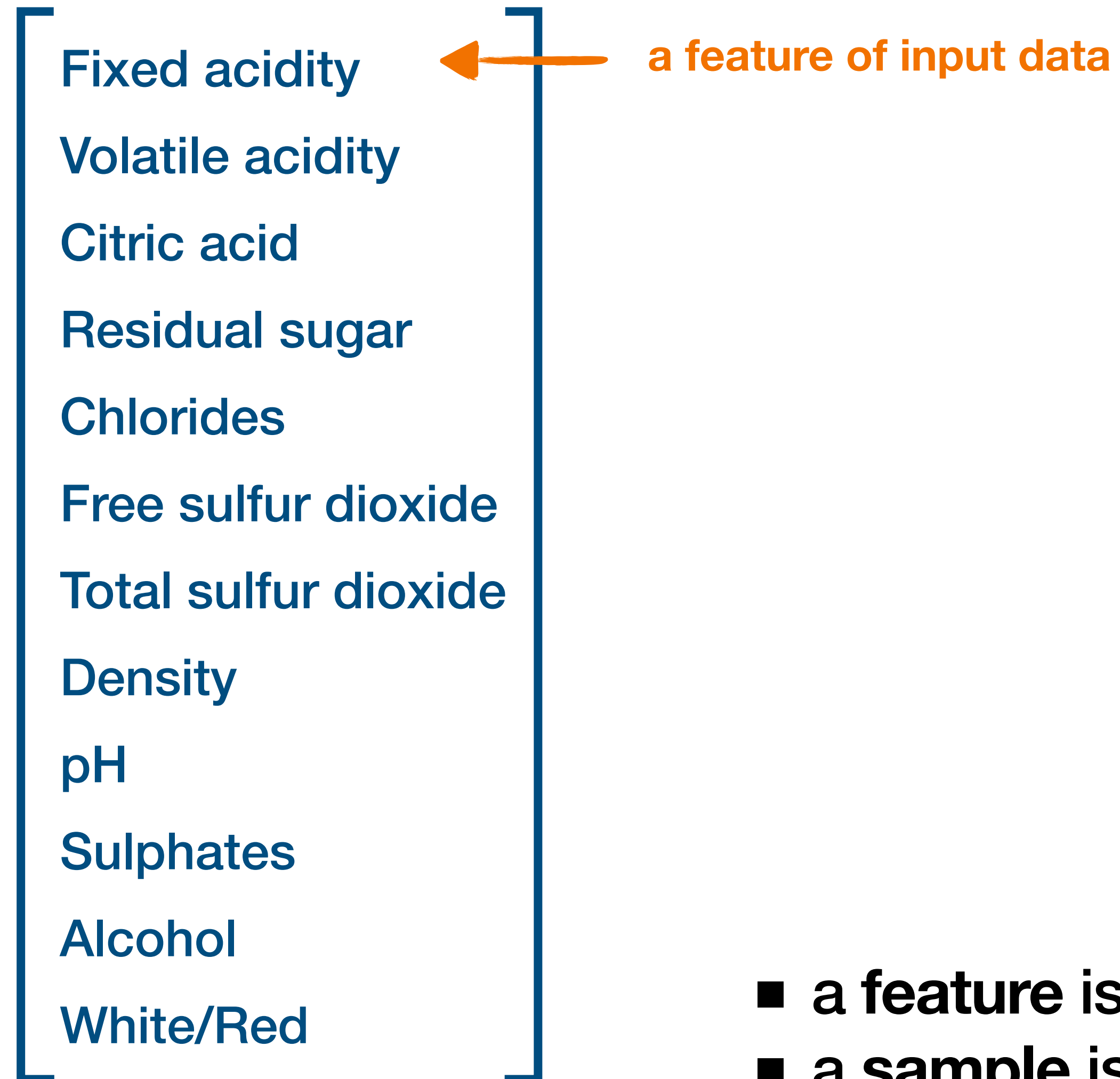
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- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol
- White/Red

← a feature of input data

- a feature is a facet of input data

hint: “this model could be a $\mathbb{R}^{12} \rightarrow \mathbb{R}^1$ function”

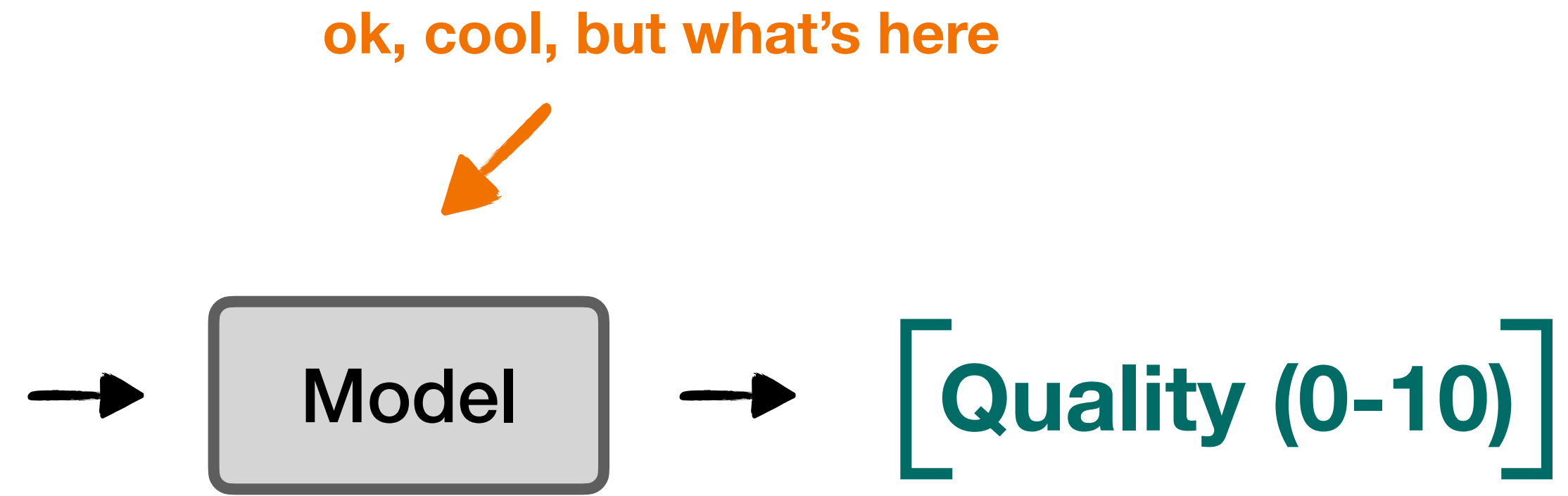
Linear Regression



- a feature is a facet of input data
- a sample is a collection of features

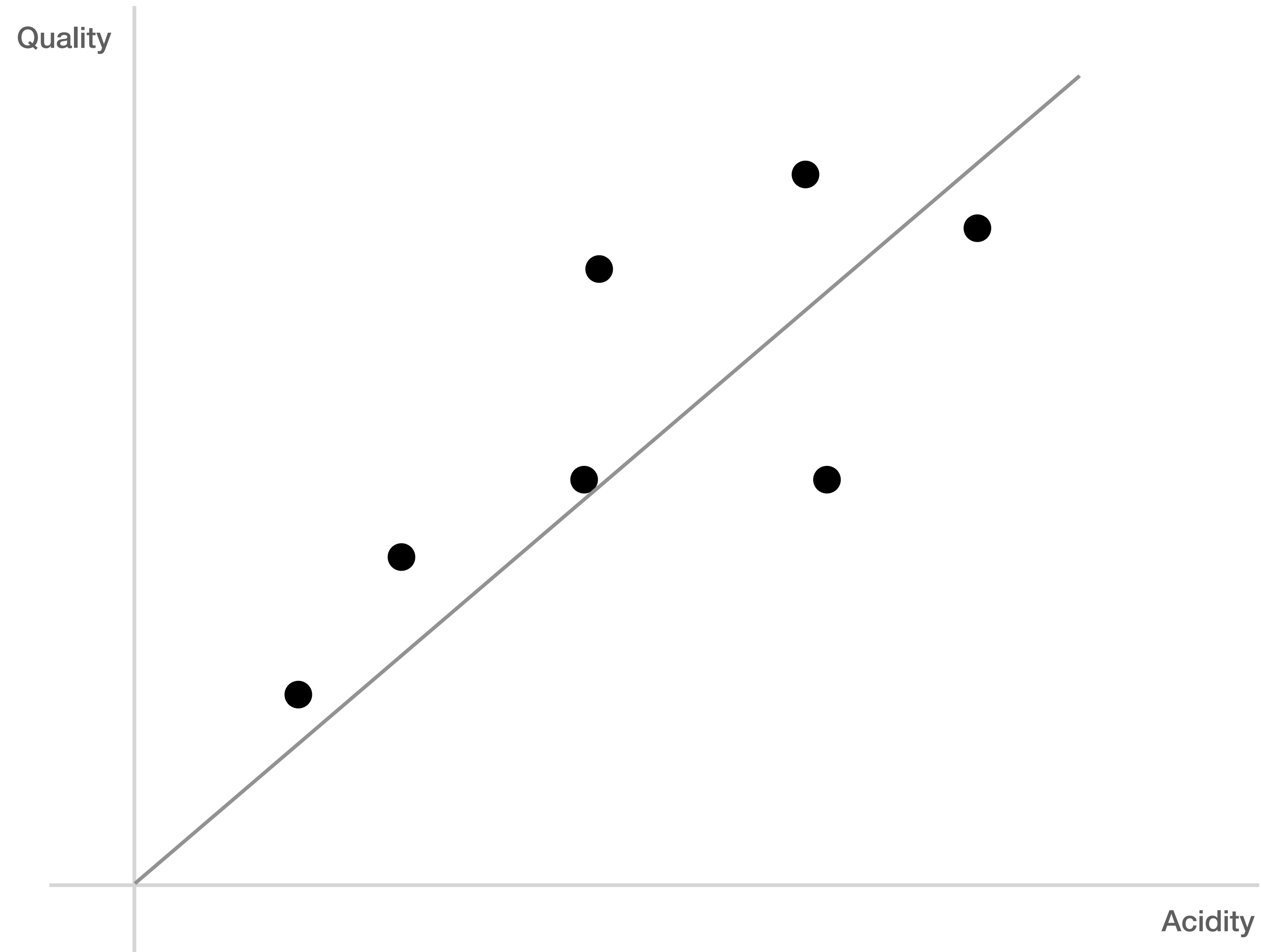
Linear Regression

- Fixed acidity
- Volatile acidity
- Citric acid
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- Alcohol
- White/Red



Linear Regression

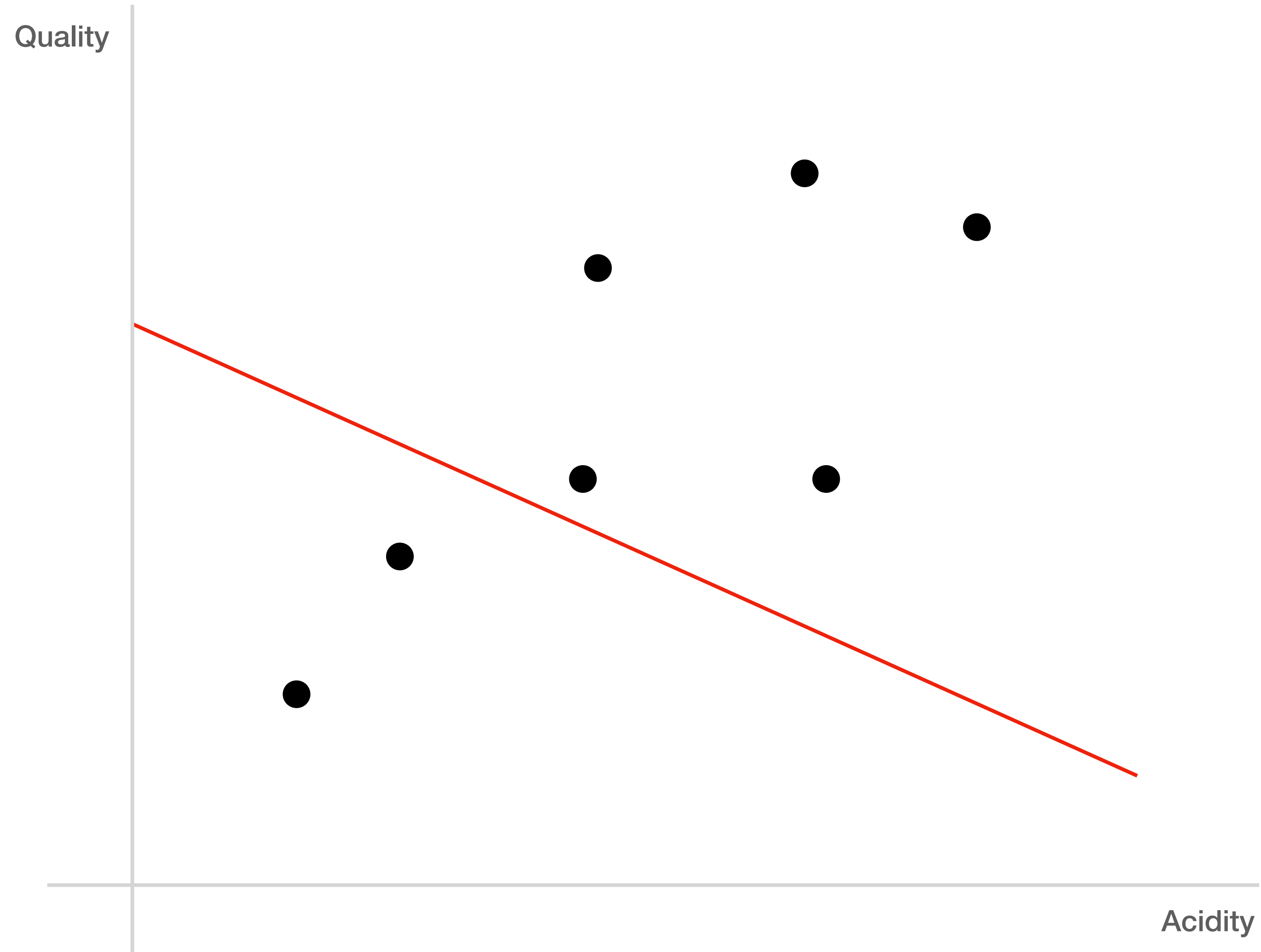
STATISTICS!



this model could be a $\mathbb{R}^1 \rightarrow \mathbb{R}^1$ function

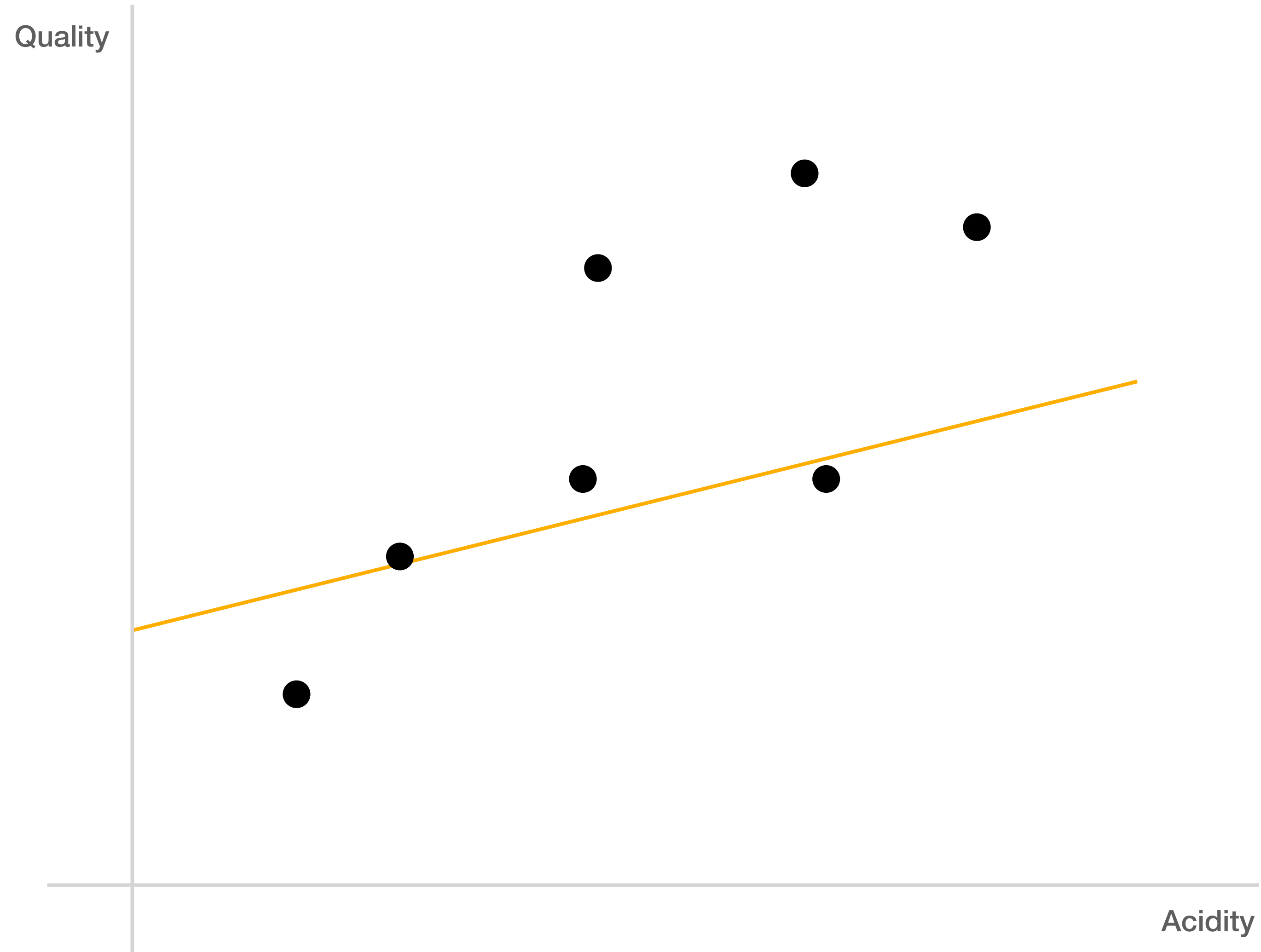
Linear Regression

STATISTICS!



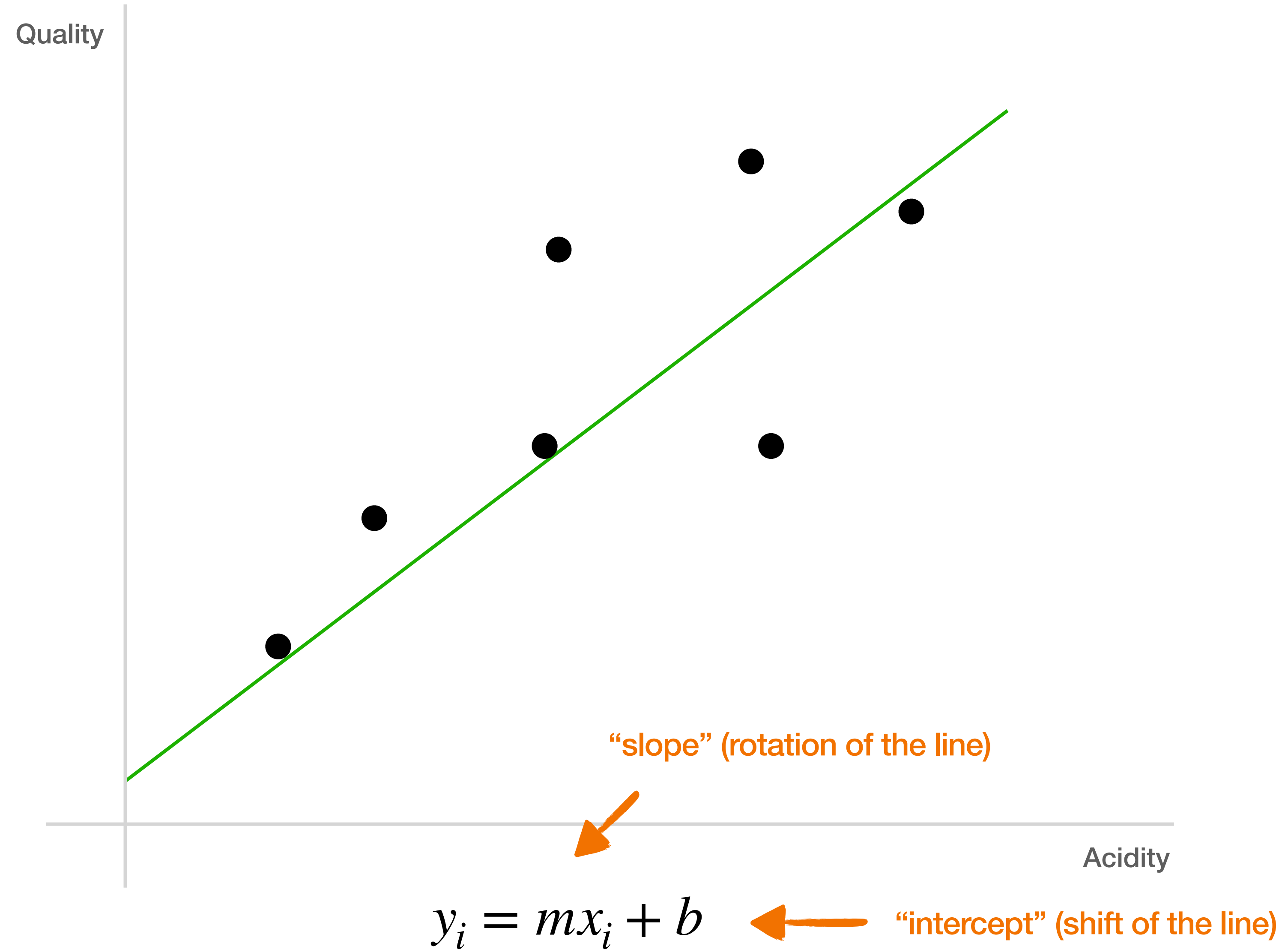
Linear Regression

STATISTICS!



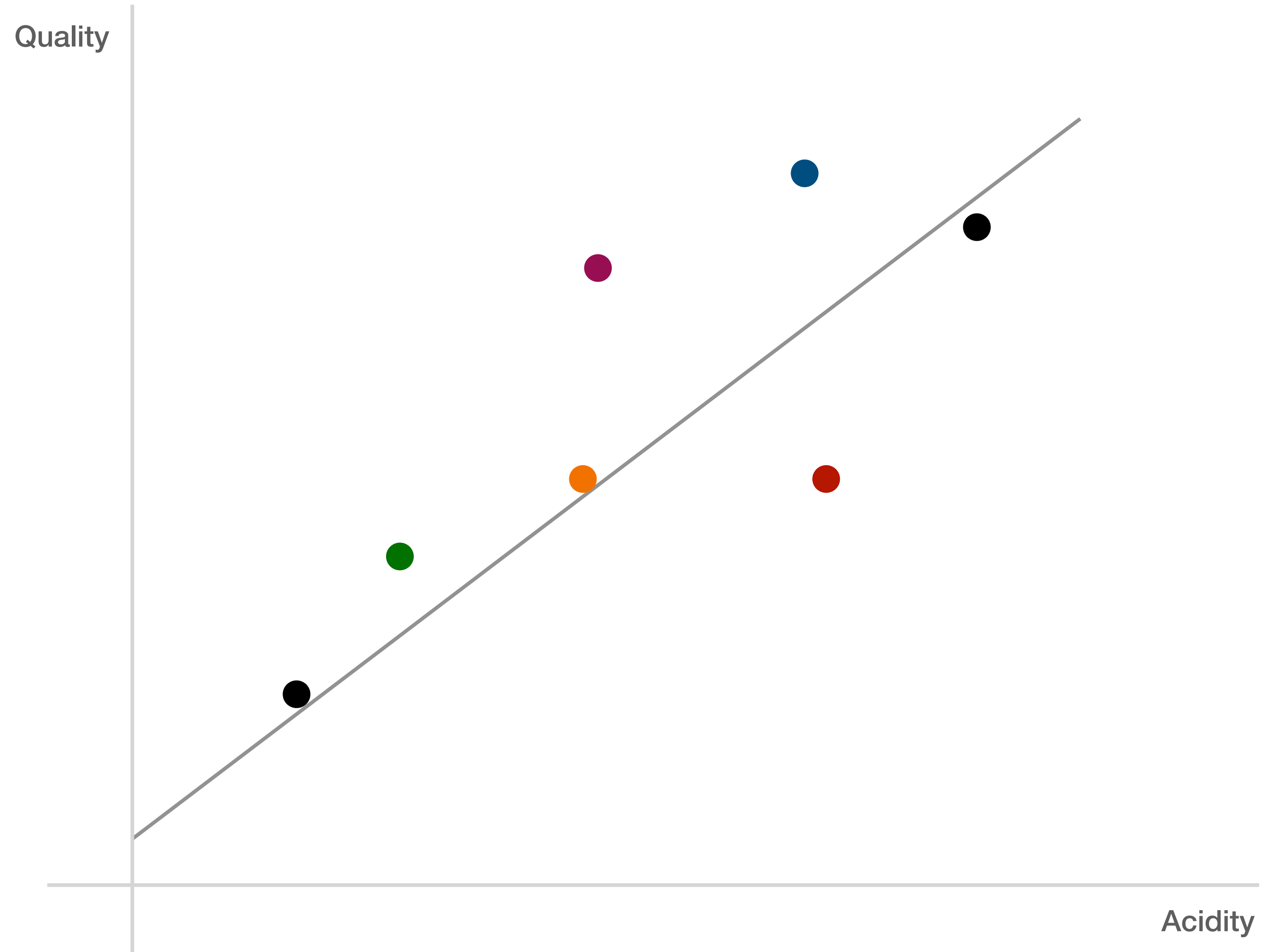
Linear Regression

STATISTICS!



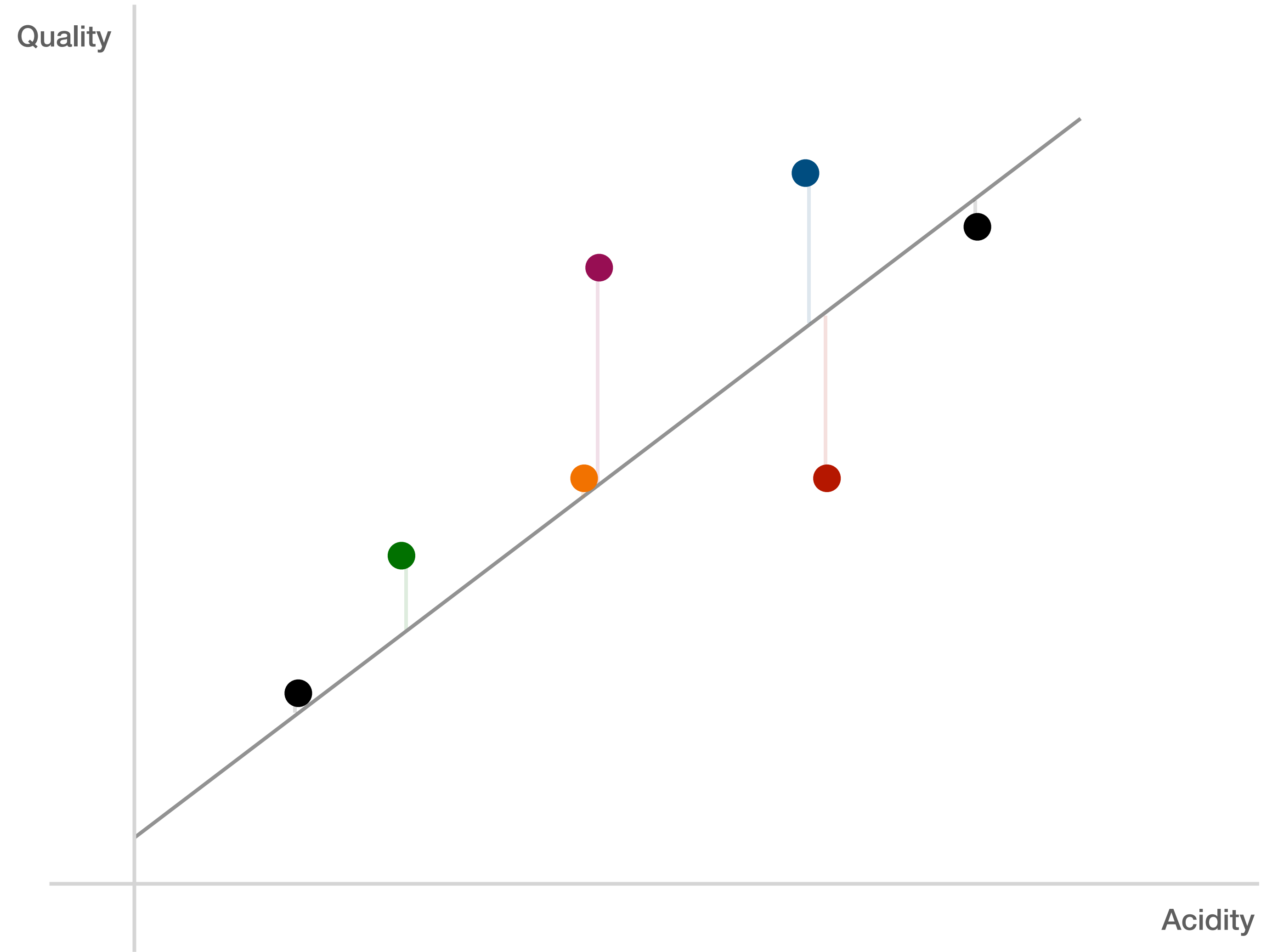
Linear Regression

STATISTICS!



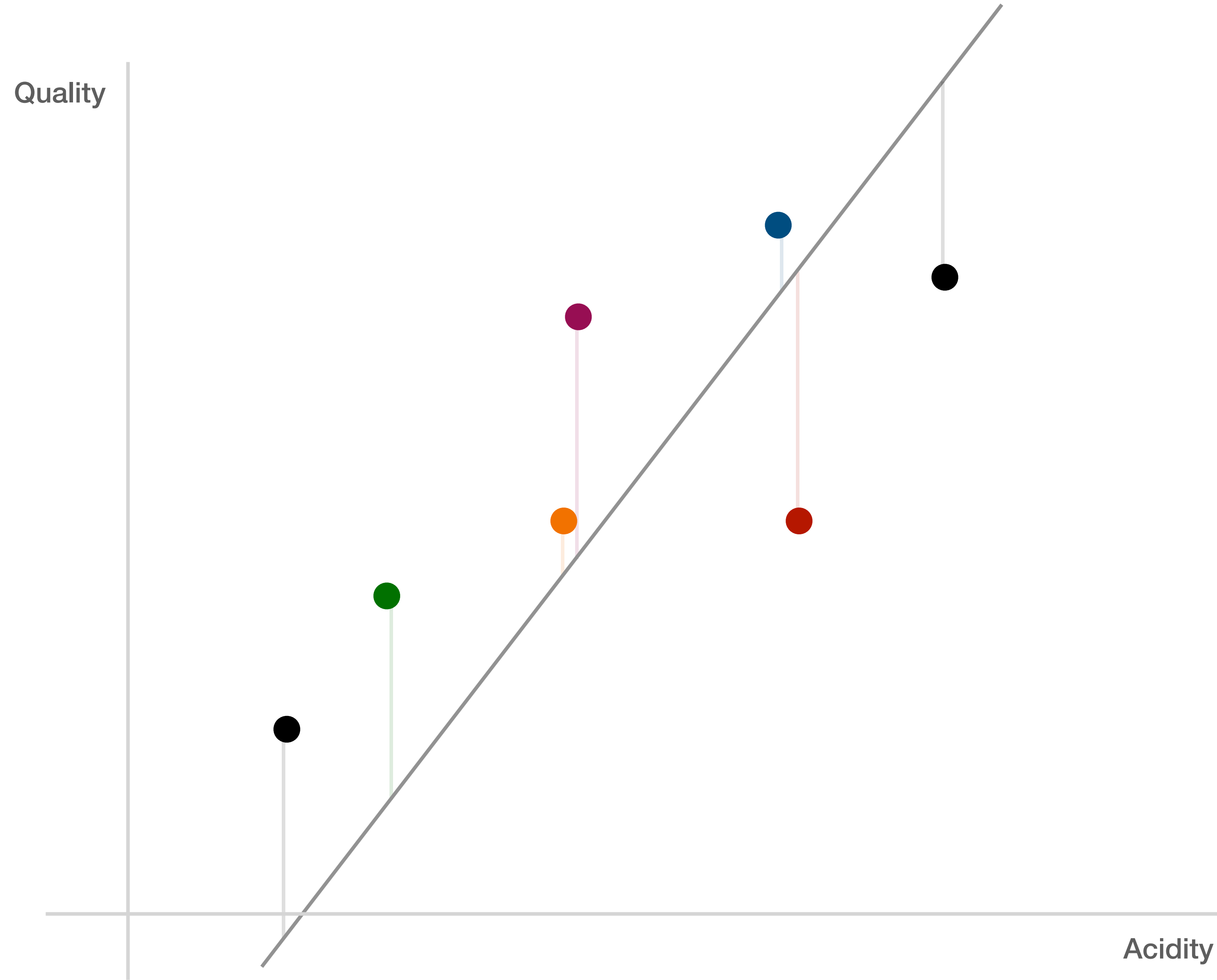
Linear Regression

STATISTICS!



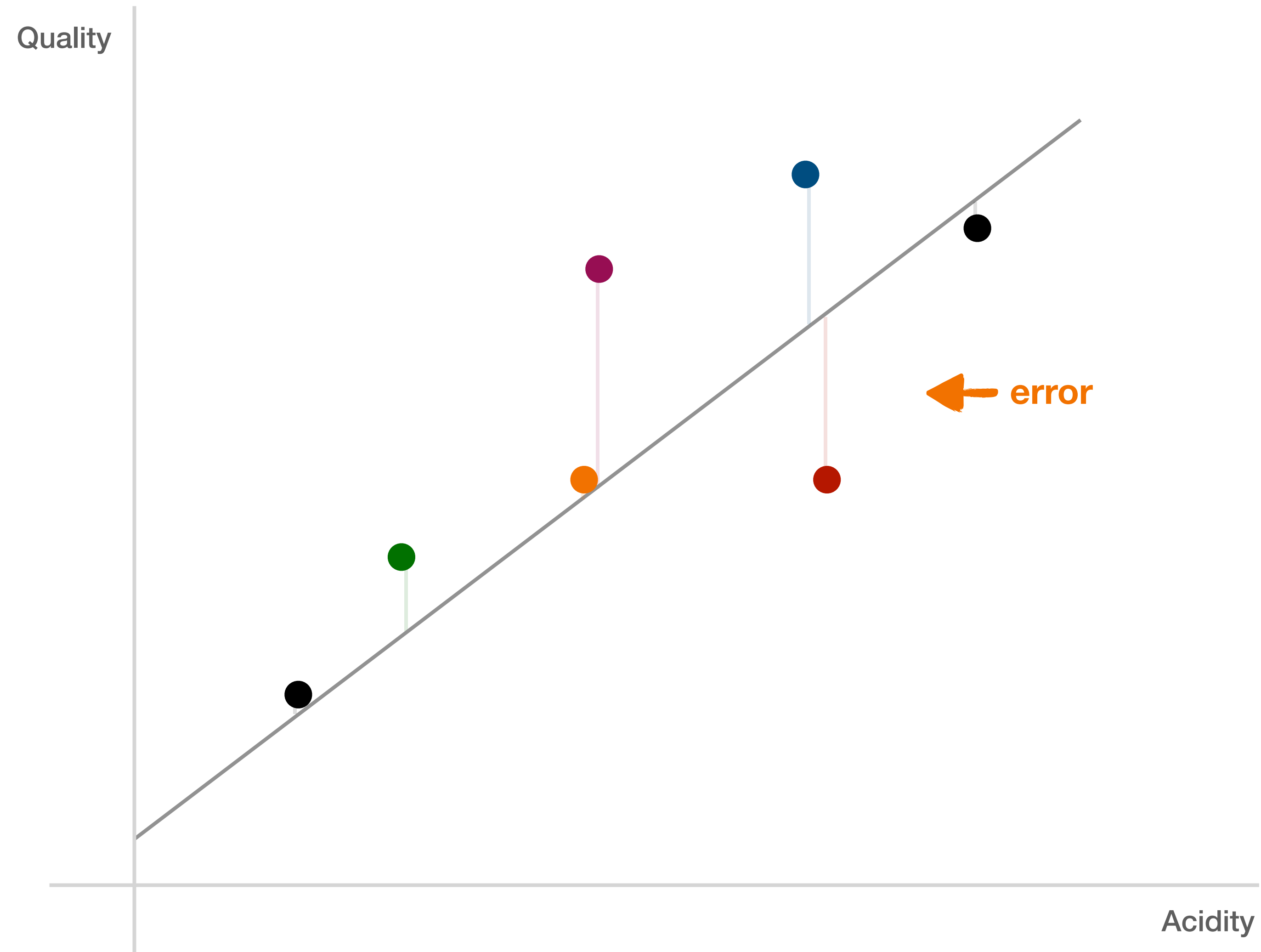
Linear Regression

STATISTICS!



Linear Regression

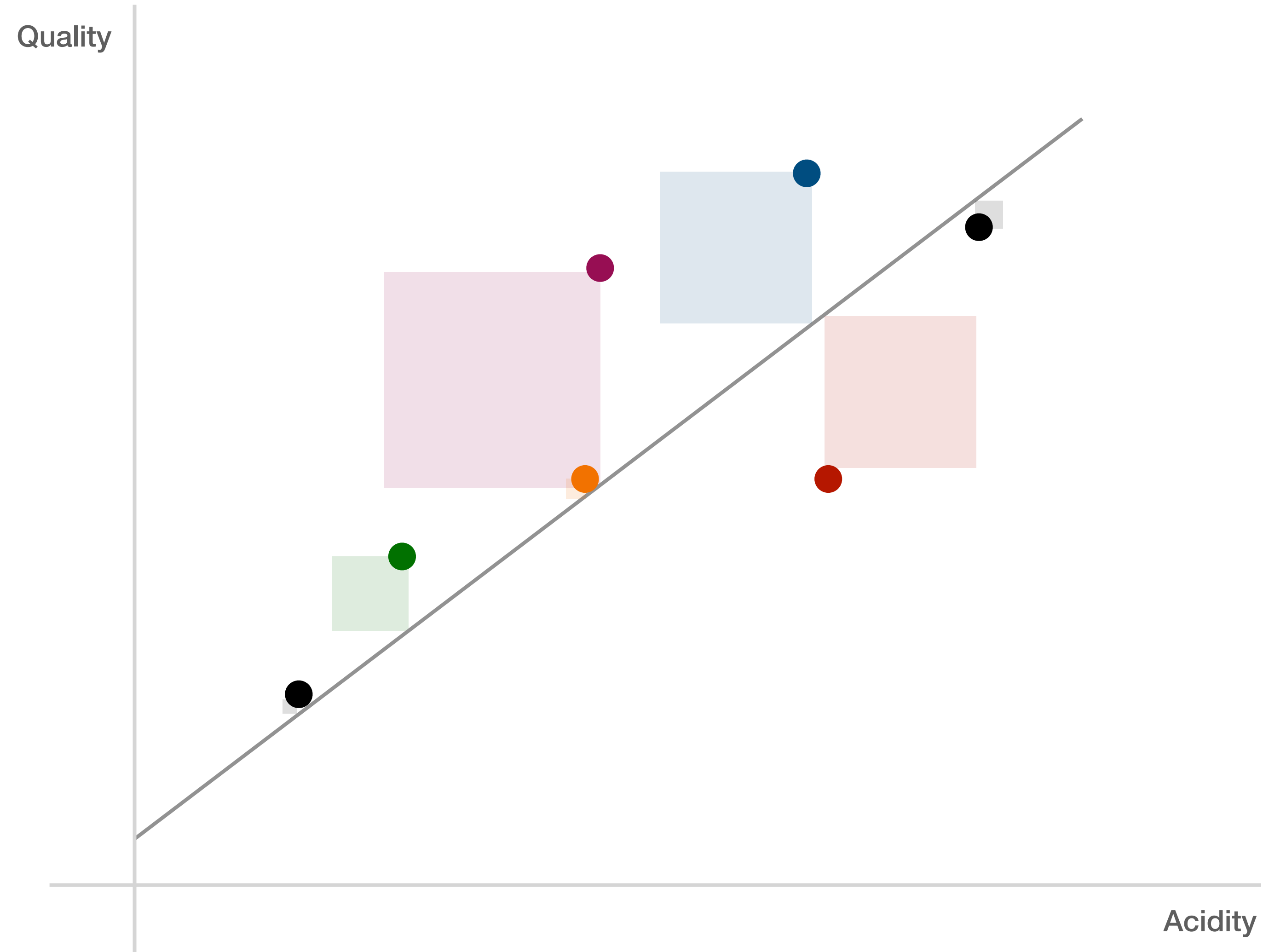
STATISTICS!



■ error is a measure of the “incorrectness” of a line

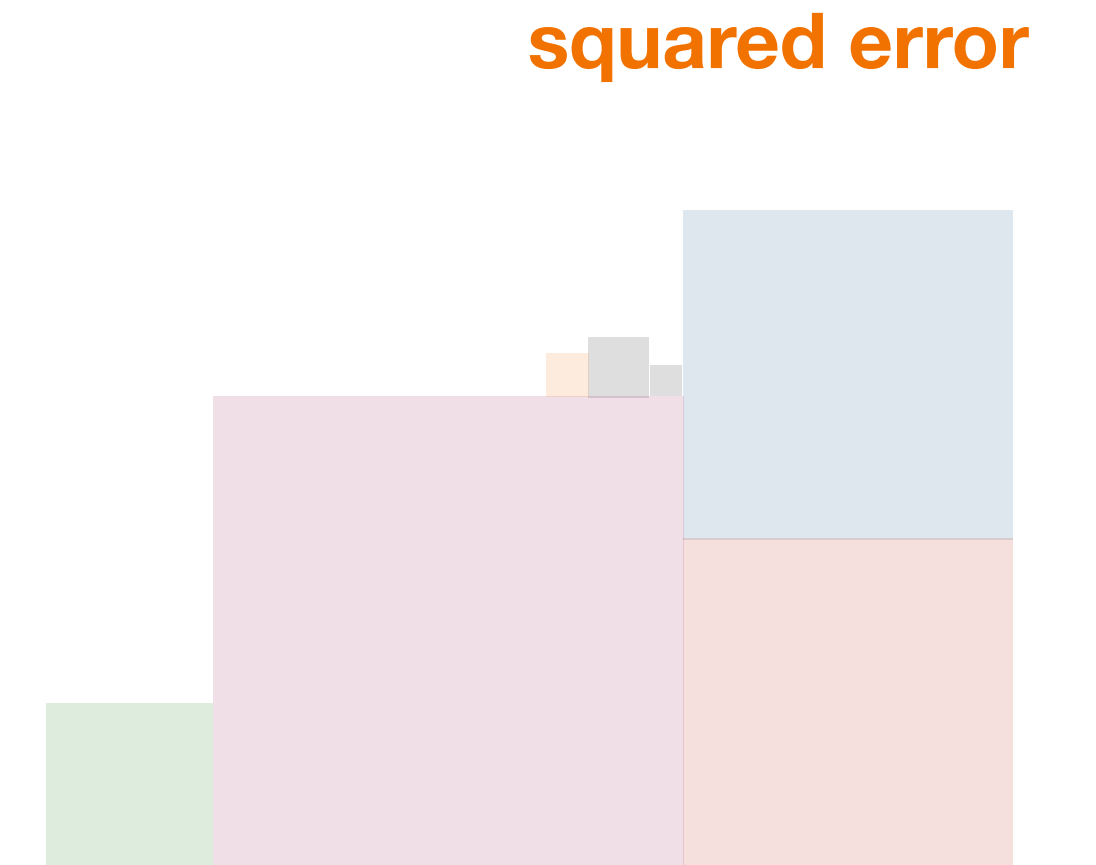
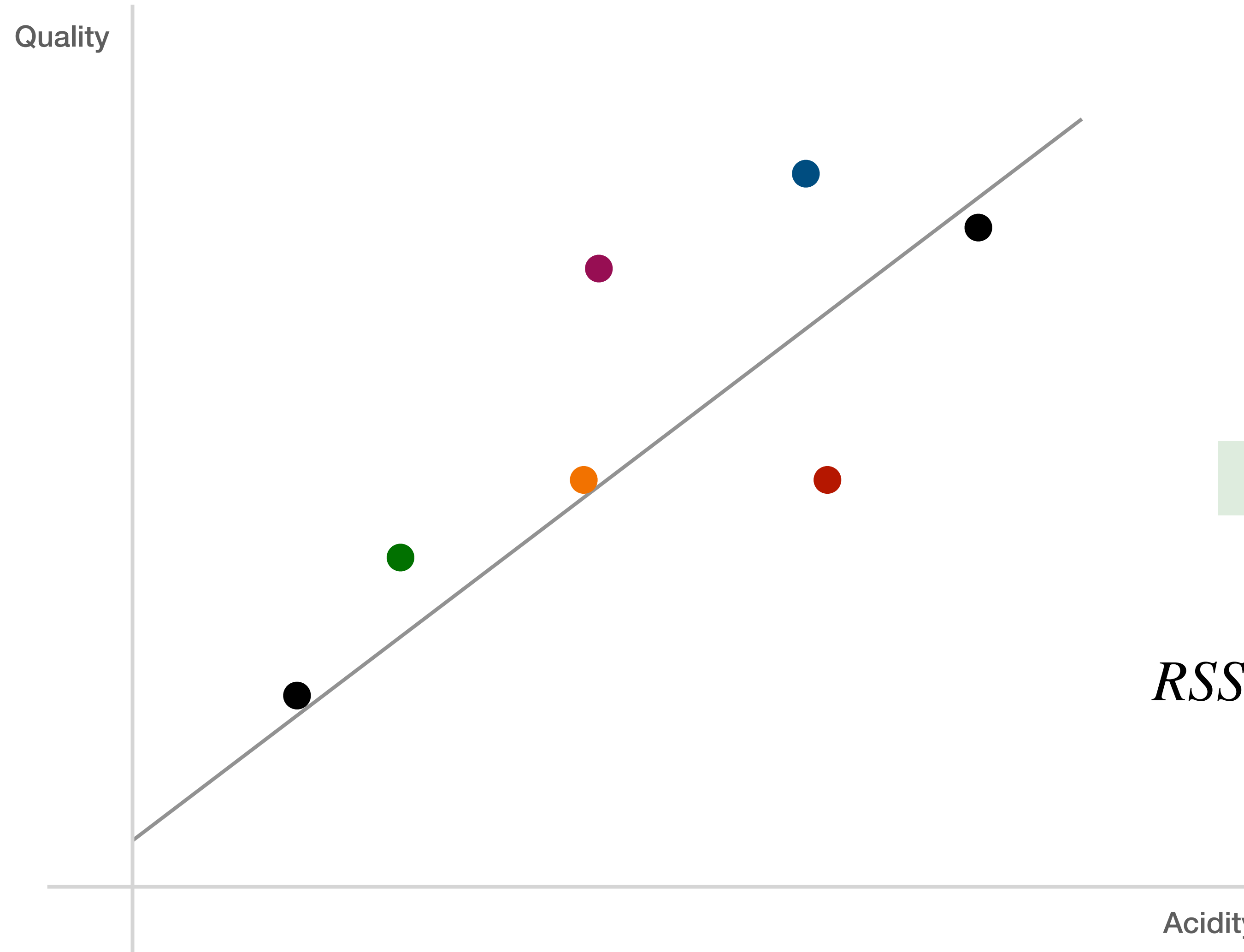
Linear Regression

STATISTICS!



Linear Regression

STATISTICS!

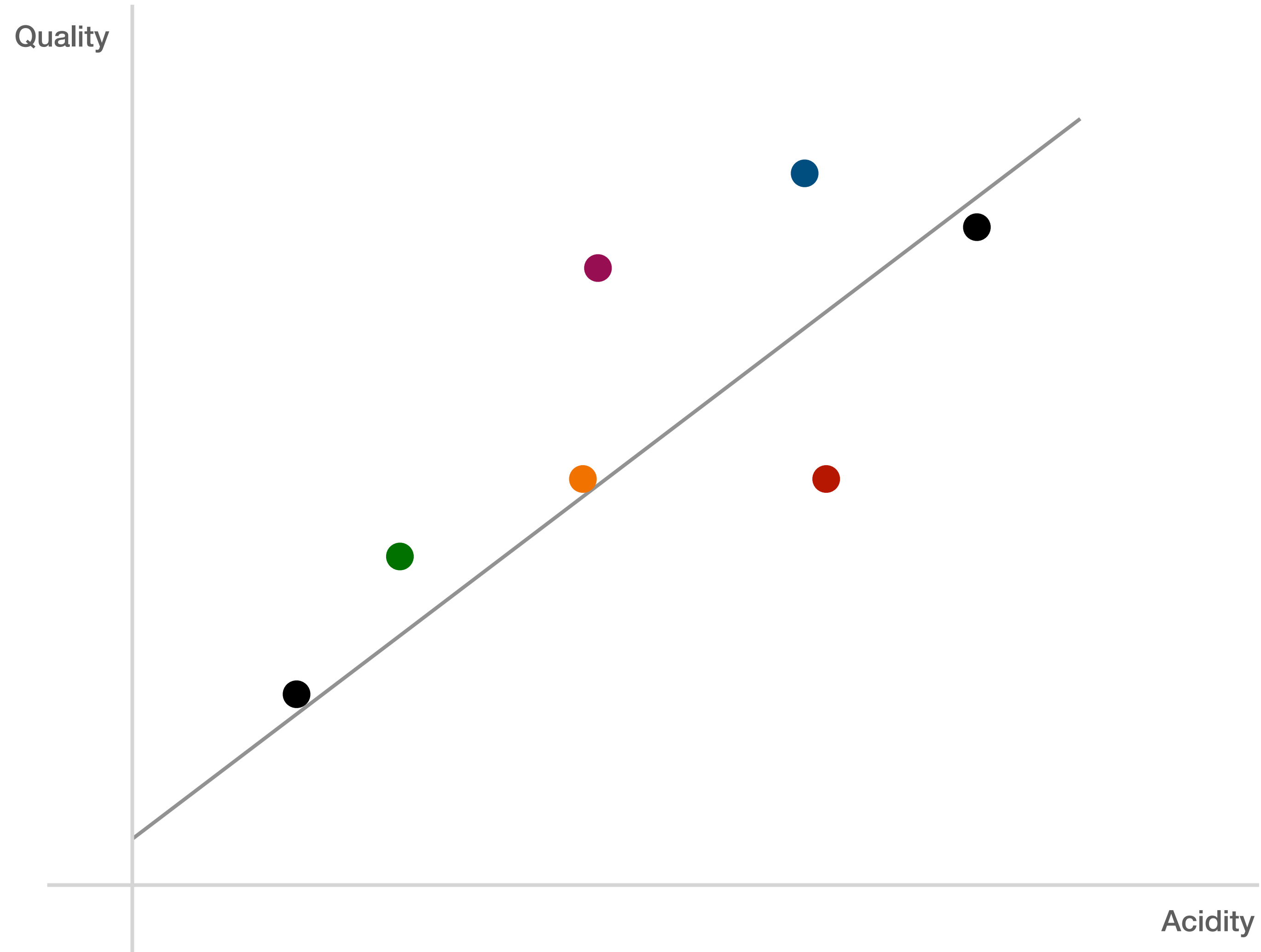


$$RSS = \sum_i (y_i - \hat{y}_i)^2$$

- **sum-of-squared error is a common error metric for linear regression**
- **sum-of-squared error is also known as “L2 Penalty”**

Linear Regression

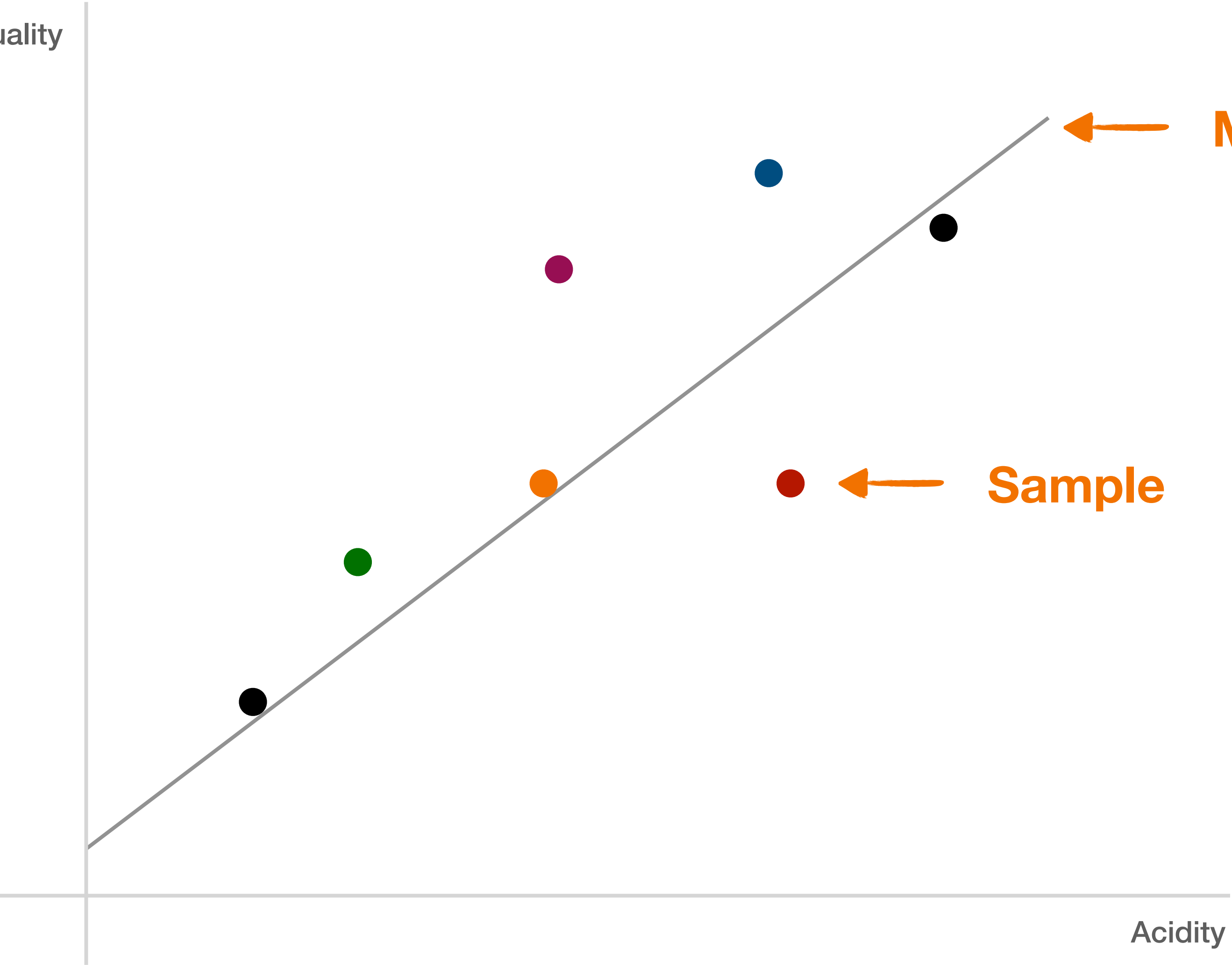
STATISTICS!



Linear Regression

Output

Quality



Acidity

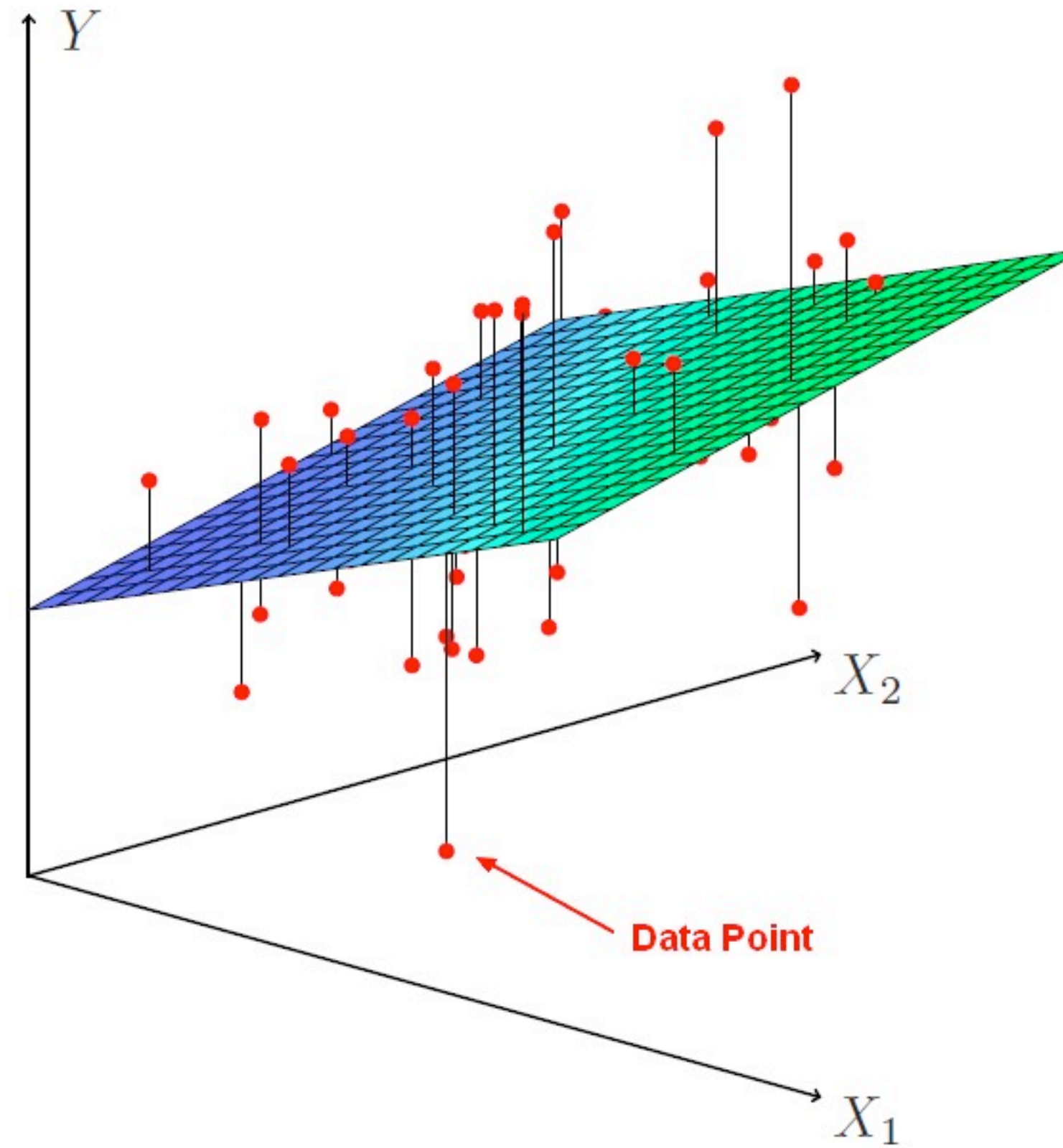
Input

Linear Regression

What if we have a
high-dimensional
vector for samples?



Linear Regression



$$y_i = m_0 w_i + m_1 x_i + \dots + b$$

Hyperplanes!
(details are about the same)

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol
- Red or White



Quality (0-10)

Logistic Regression

- Fixed acidity
- Volatile acidity
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White or Red

Logistic Regression

- Fixed acidity
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- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol



White or Red



how do we turn this into numbers?

Logistic Regression

a possible solution...

White = 0

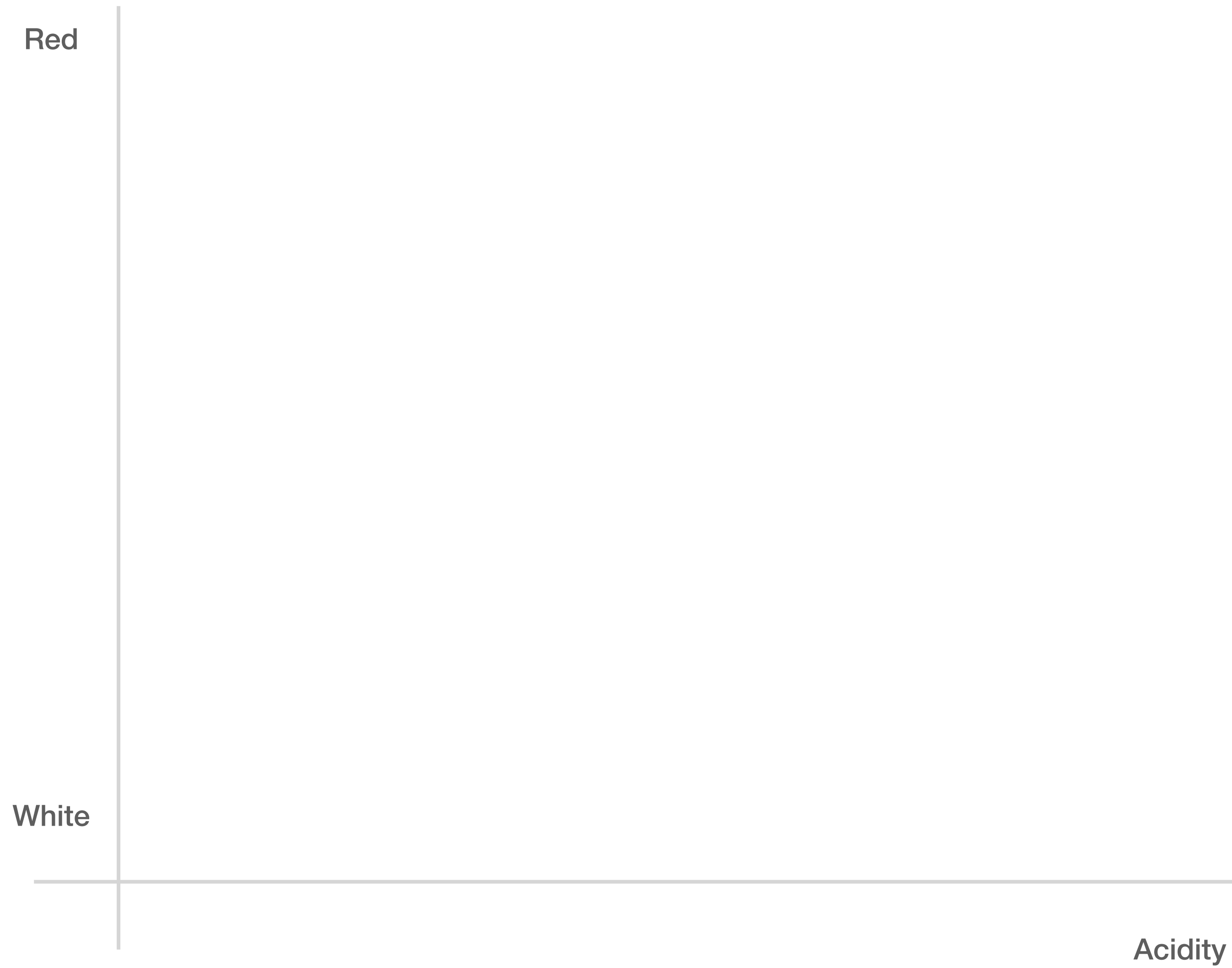
Red = 1

a class

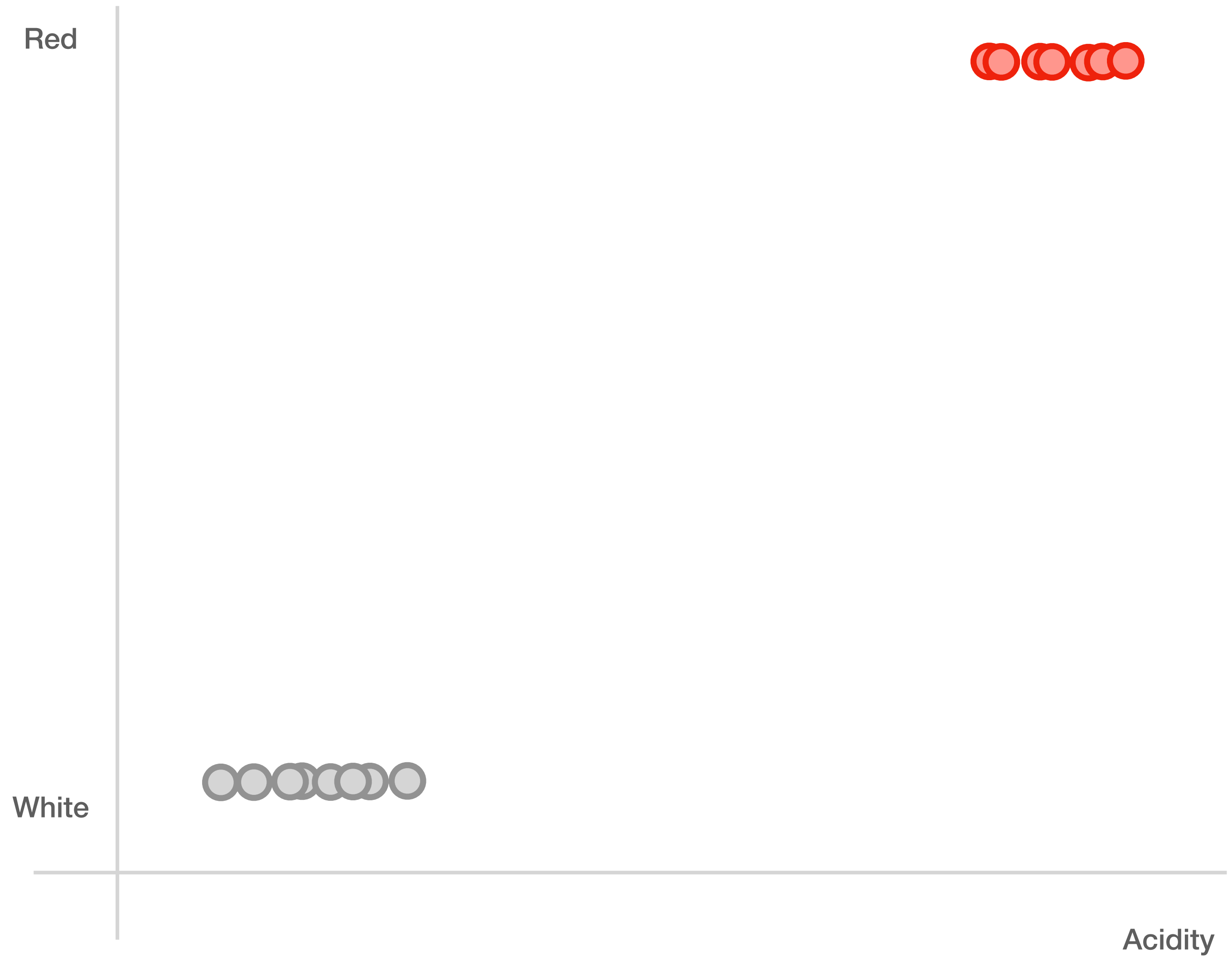


- categorical label outputs are named “classes”

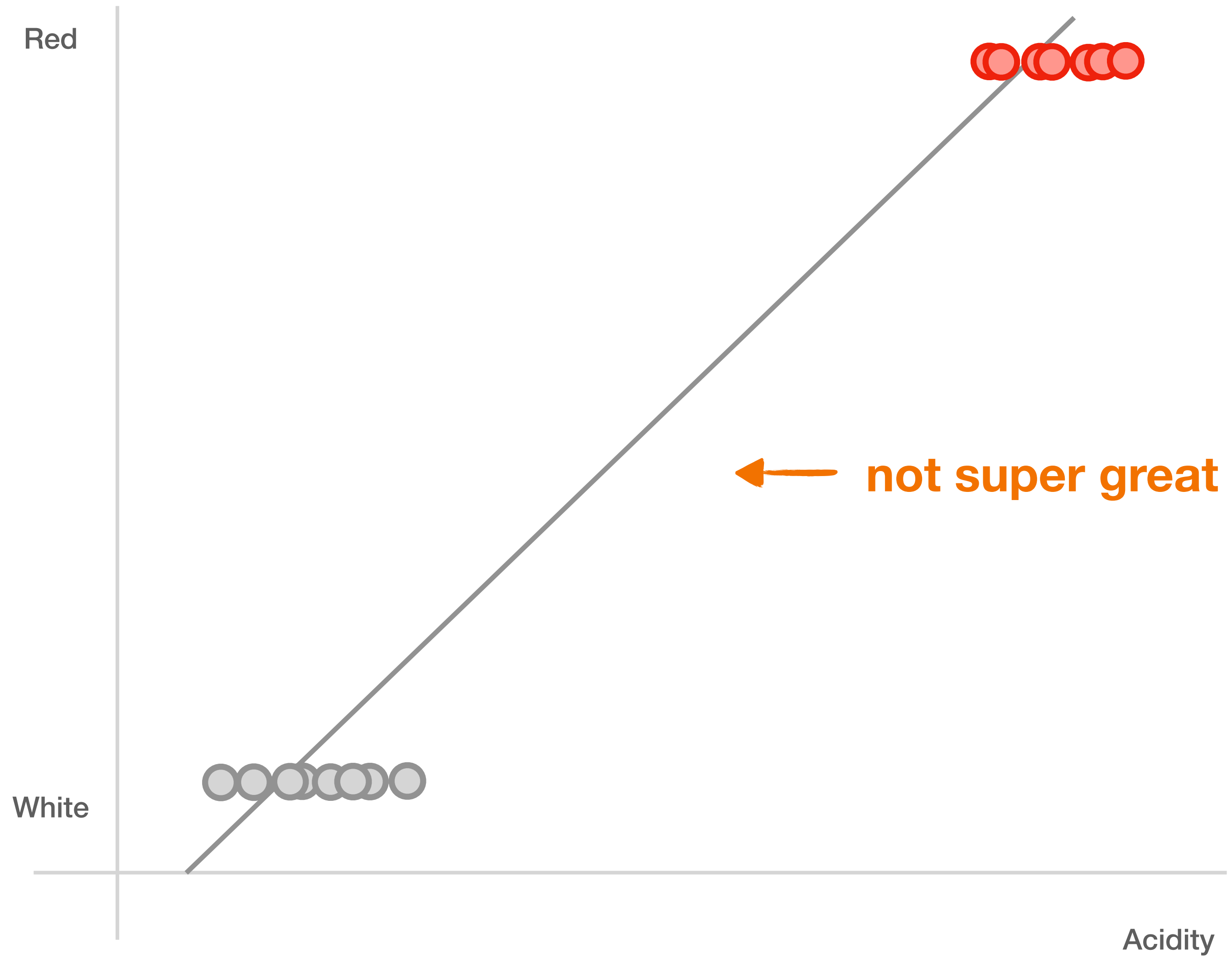
Logistic Regression



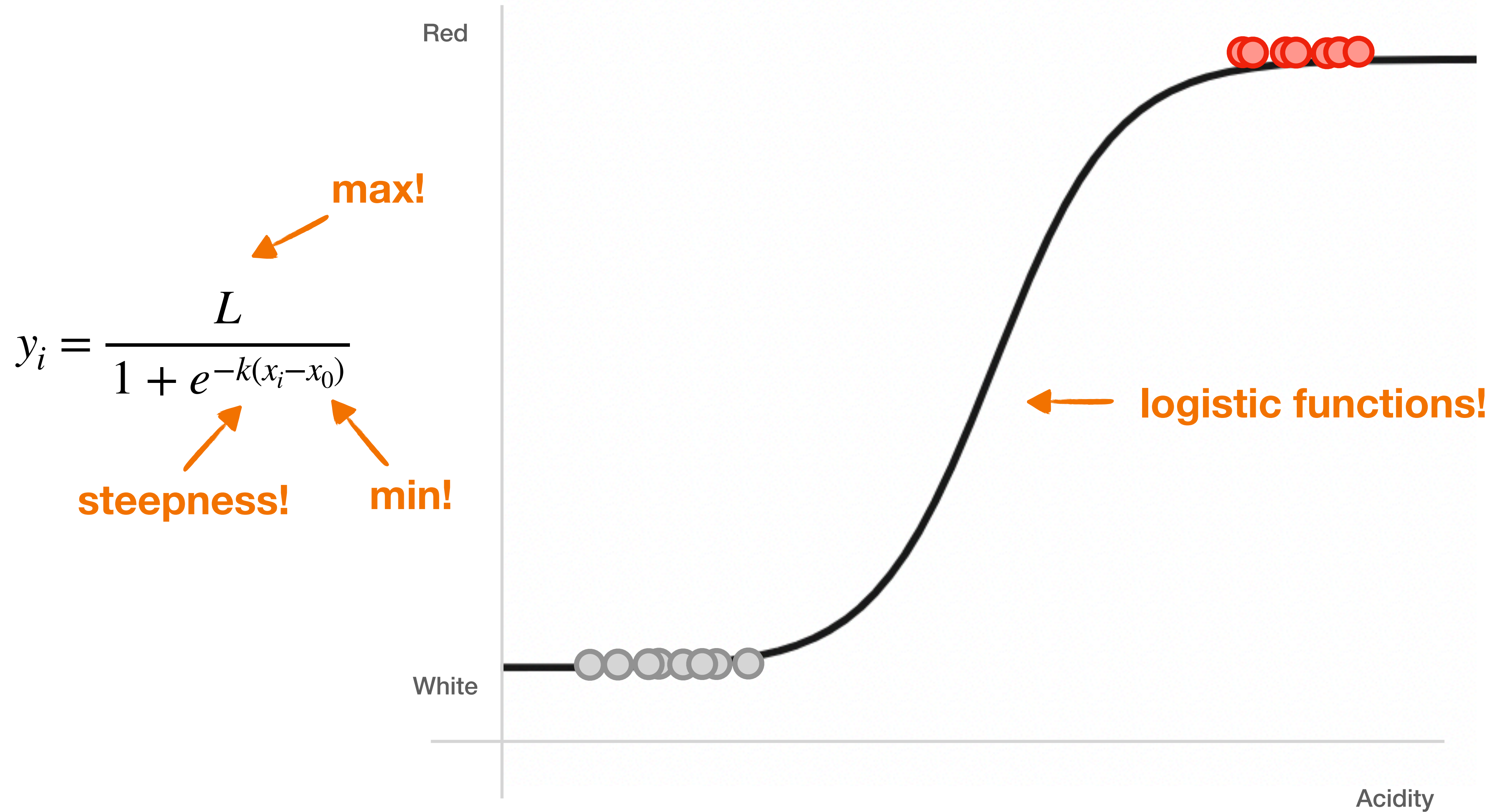
Logistic Regression



Logistic Regression



Logistic Regression



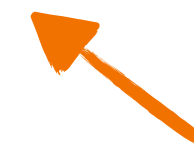
But what if we have more than two classes for output?



- **logistic functions** are a good way of making predictions on binary/categorical data
- **sum-of-squared error** is *still* a common error metric for logistic regression

Logistic Regression

White **Red** **Champagne**



pair them up!

Logistic Regression

White

Red

White

Champagne

Red

Champagne

Logistic Regression

White

Red

White

Champagne

Red

Champagne

Logistic Regression

White

Red

White

Champagne

Red

Champagne

Logistic Regression

White

Red

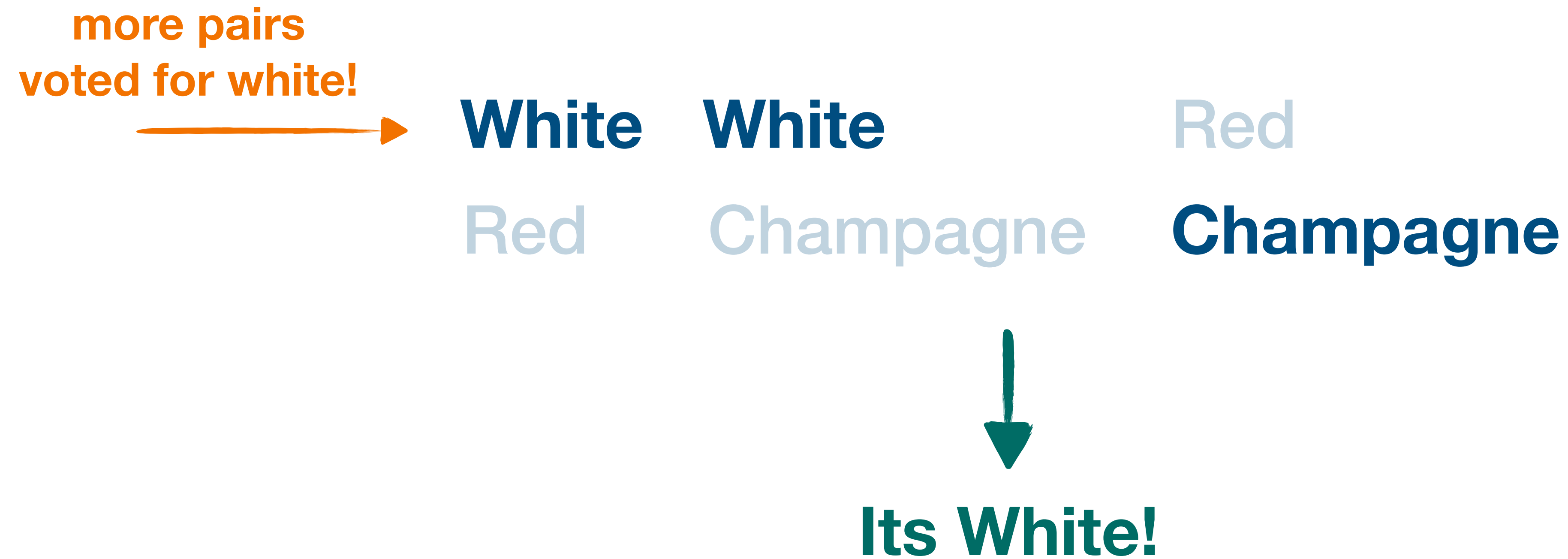
White

Champagne

Red

Champagne

Logistic Regression



- **One-vs-one** multiclass classification uses the most “voted for” class among paired models

Logistic Regression

White

Red

White

Champagne

Red

Champagne

Logistic Regression

White

Red Champagne

Red

Champagne White

Champagne

Red White

Logistic Regression



pick the answer with highest probability

- **One-vs-all** multiclass classification uses the most highest probability paring result among all combinations

Ok. Time for doing stuff.