



# AI Bridge

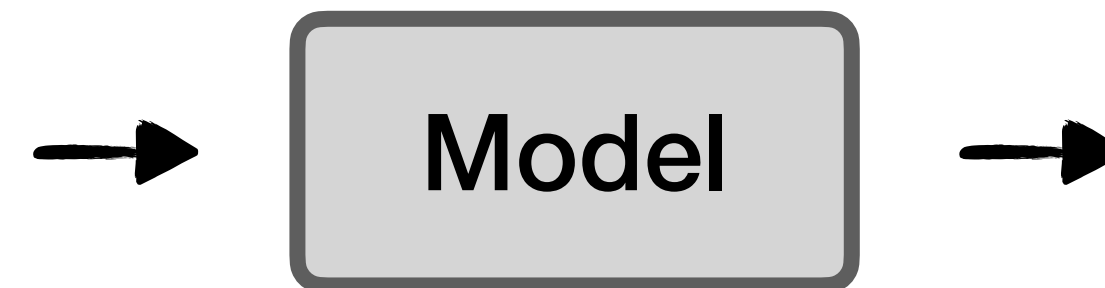
## Lecture 6

# ***Classification!***

# Classification!

quick review  
wine dataset

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol



**White = 0**  
**Red = 1**

a class



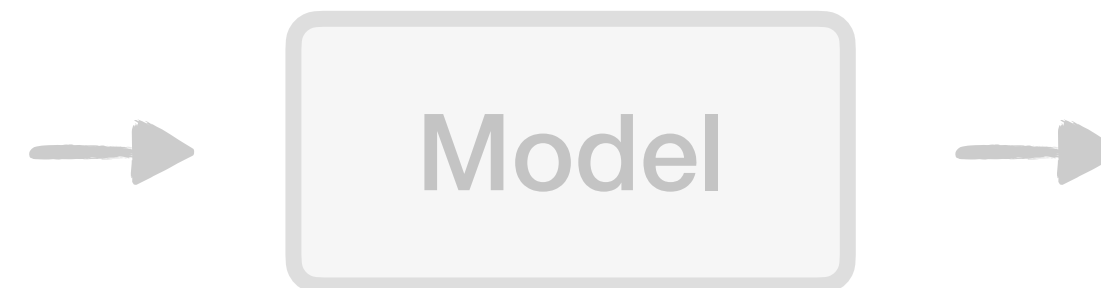
- categorical label outputs are named “**classes**”

# Classification!

quick review  
wine dataset

that's a lot  
of features!

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■ categorical label outputs are named “classes”

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**that's a lot  
of features!**

can they really be linear?  
even in high dimensions?

- as feature counts increase, and on complex data, linear type model may not be the best model

as feature counts increase, and on complex data,  
linear type models may not be the best model

**we need a more complex model**

# Decision Trees

# Decision Trees





# Decision Trees



Can I afford it?

# Decision Trees



Can I afford it?

Is it comfortable?

# Decision Trees



Can I afford it?

Is it comfortable?

Is it fashionable?

# Decision Trees

Can I afford it?

Is it comfortable?

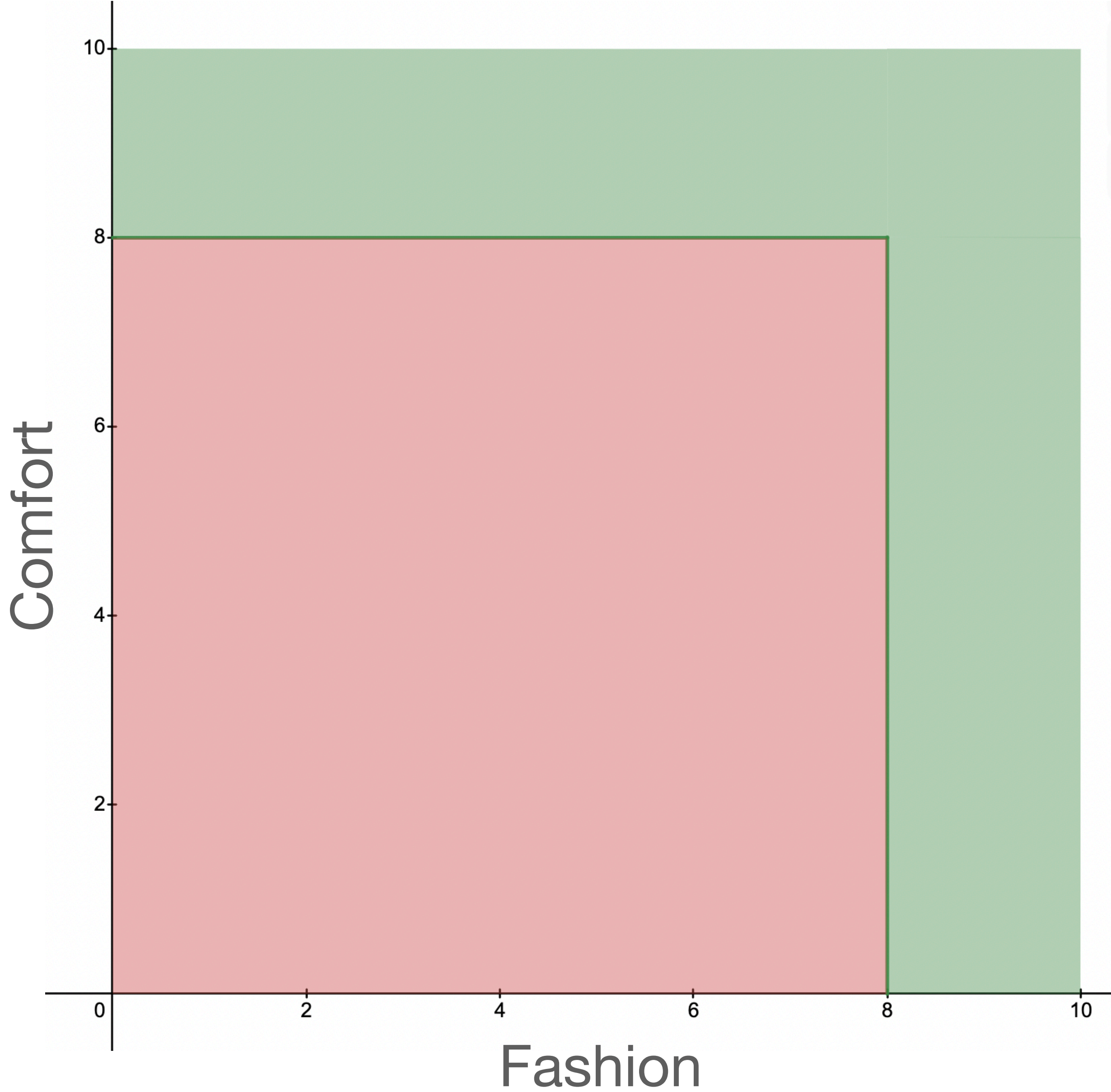
Is it fashionable?

# Decision Trees

Can I afford it?

Is it comfortable?

Is it fashionable?



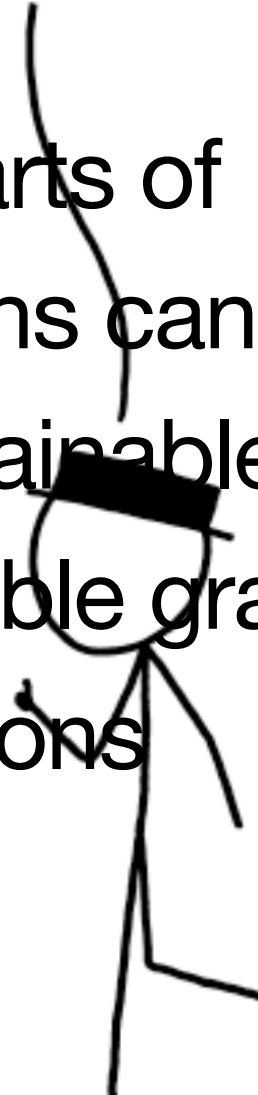
# Decision Trees



# Decision Trees

that seems awfully hard-coded!

- flowcharts of decisions can create an explainable and repeatable graph of predictions



# Decision Trees

Price	Comfort	Fashion	Purchased?
\$70	4	6	No
\$120	5	8	No
\$20	4	4	No
\$60	1	8	Yes
\$60	6	3	No
\$80	8	8	Yes



# Decision Trees

**Purchased?**

No

No

No

Yes

No

Yes

# Decision Trees

No

No

No

Yes

No

Yes

# Decision Trees

No	Yes
No	No
No	Yes

# Decision Trees

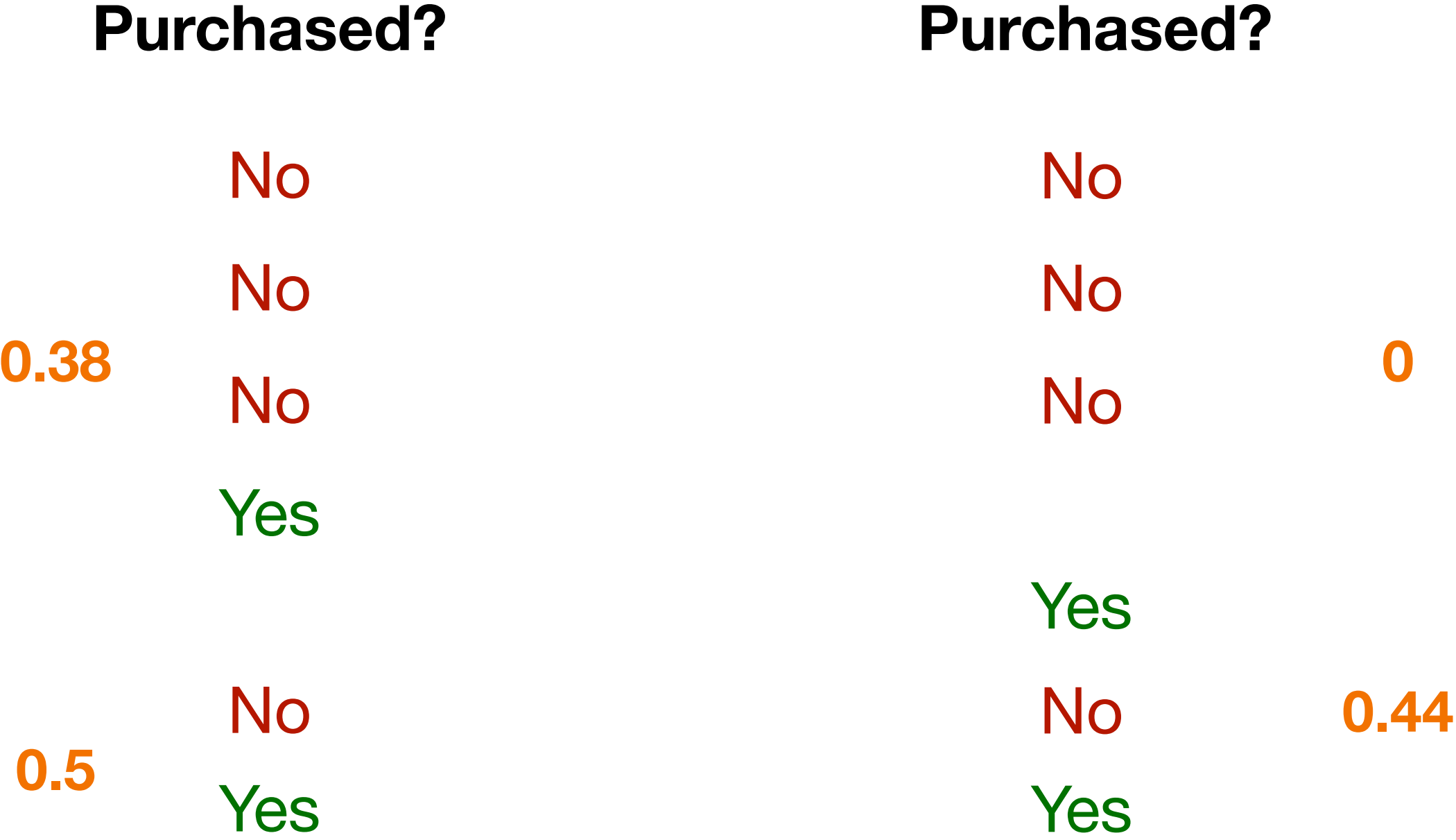
Which one is a better split?



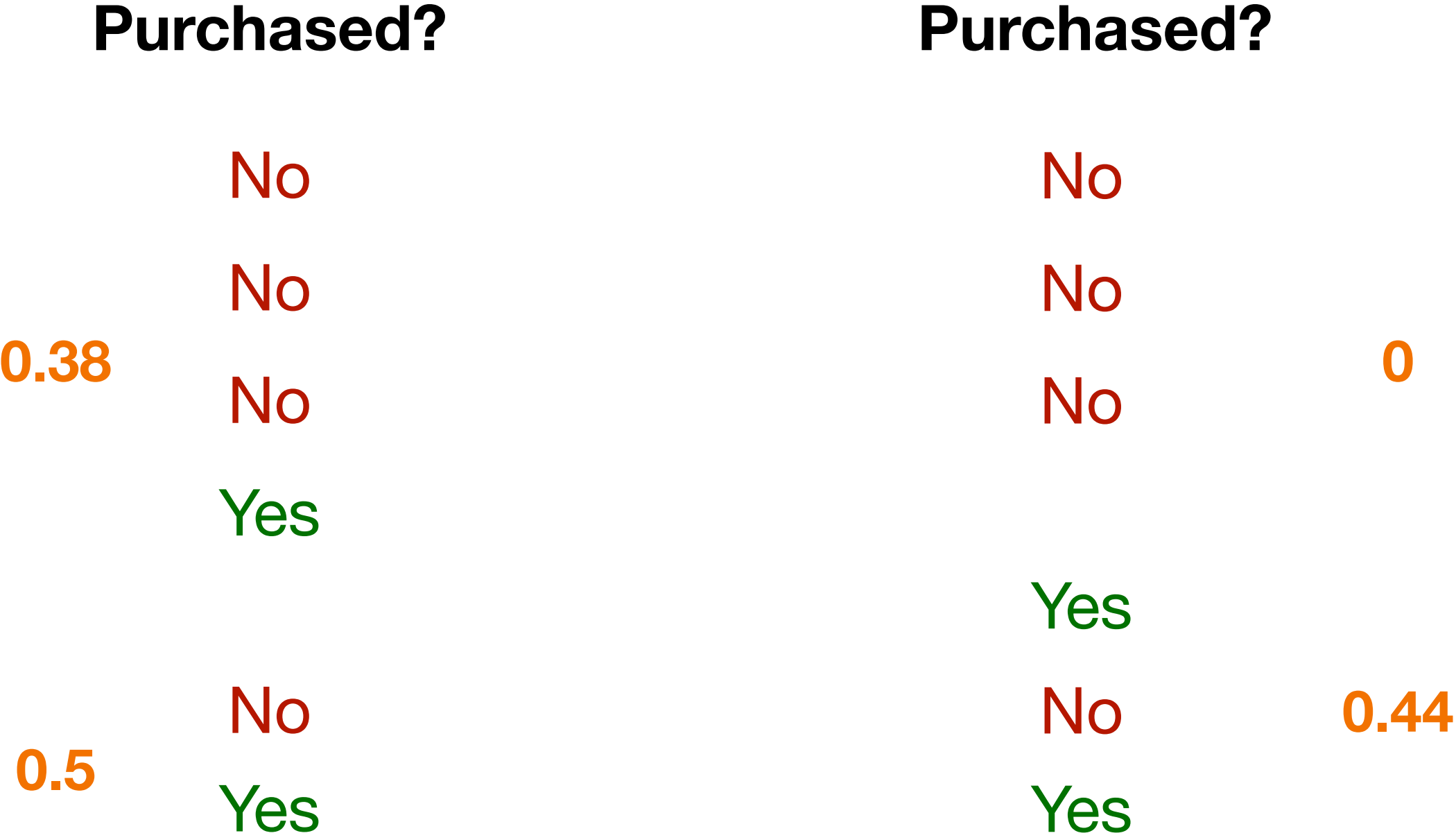
No  
No No  
No Yes  
Yes  
Mostly no

No Yes  
No No  
No Yes  
All no

**Mostly**  
(Gini impurity)



- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.



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- perfect groups => 0 **Gini Impurity** => 100% predictions

Portion of that one class in group      Portion of not that one class in the group

$$G = \sum_{i=1}^C P(i) \cdot (1 - P(i)) \blacksquare$$

Add them up for all groups

- **Gini impurity** measures the homogeneity in a group



# Decision Trees

**Purchased?**

No

0

No

No

Yes

0.5

No

Yes

---

0.5

# Decision Trees

**Purchased?**

No

No

**0.38**

No

Yes

No

**0.5**

Yes

---

**0.88**

# Decision Trees

we gotta do better than this, right?



Purchased?

No	
No	0
No	
Yes	
No	0.44
Yes	
	<hr/>
	0.44

# Decision Trees

**just split  
again!**

**Purchased?**

No

No 0

No

Yes

No 0.44

Yes

---

0.44

# Decision Trees

1. Make splits and calculate Gini impurity
2. Select the split with the lowest Gini impurity
3. If unhappy, **just split again!**
4. Repeat 1-3 as much as needed

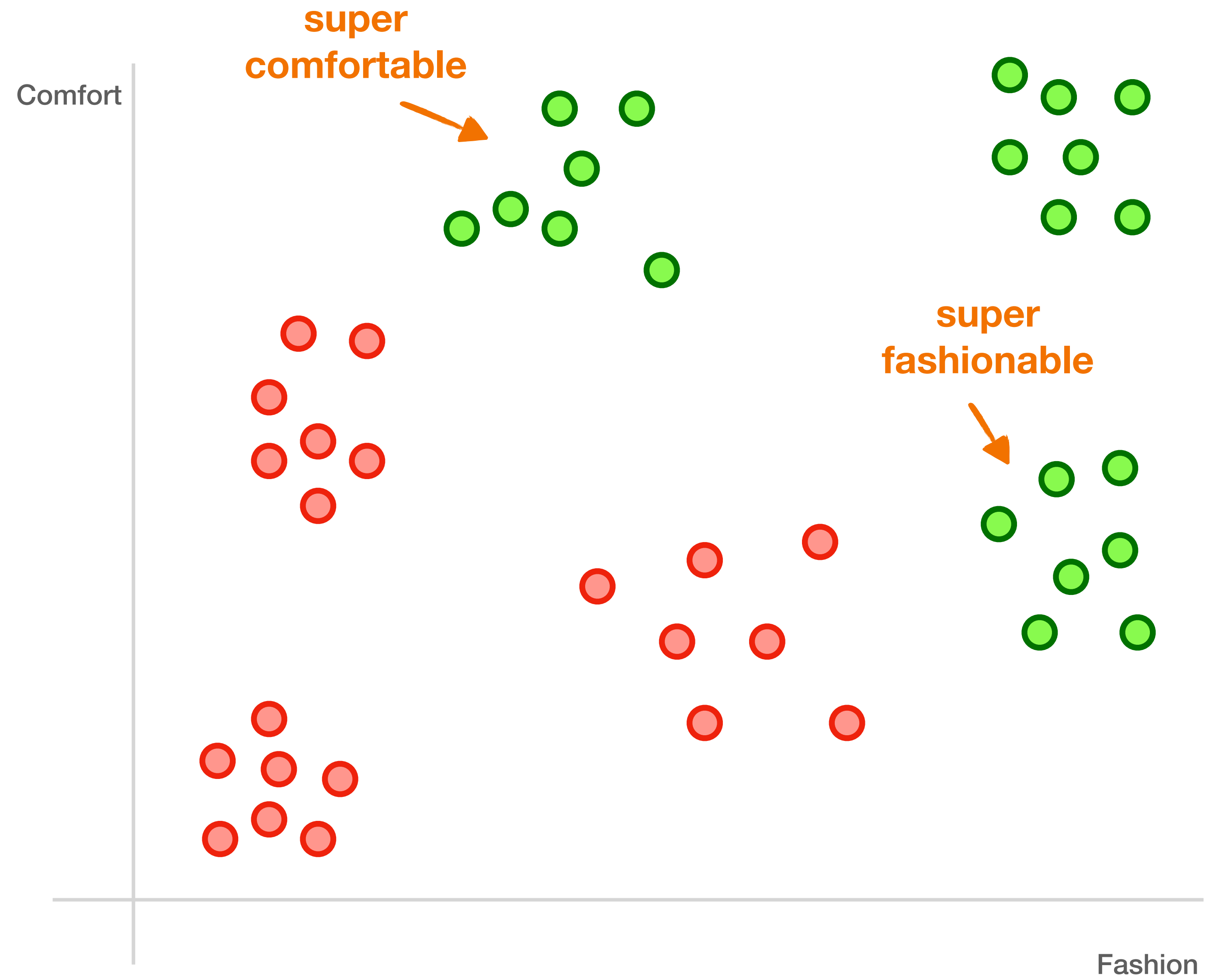


a hyperparameter

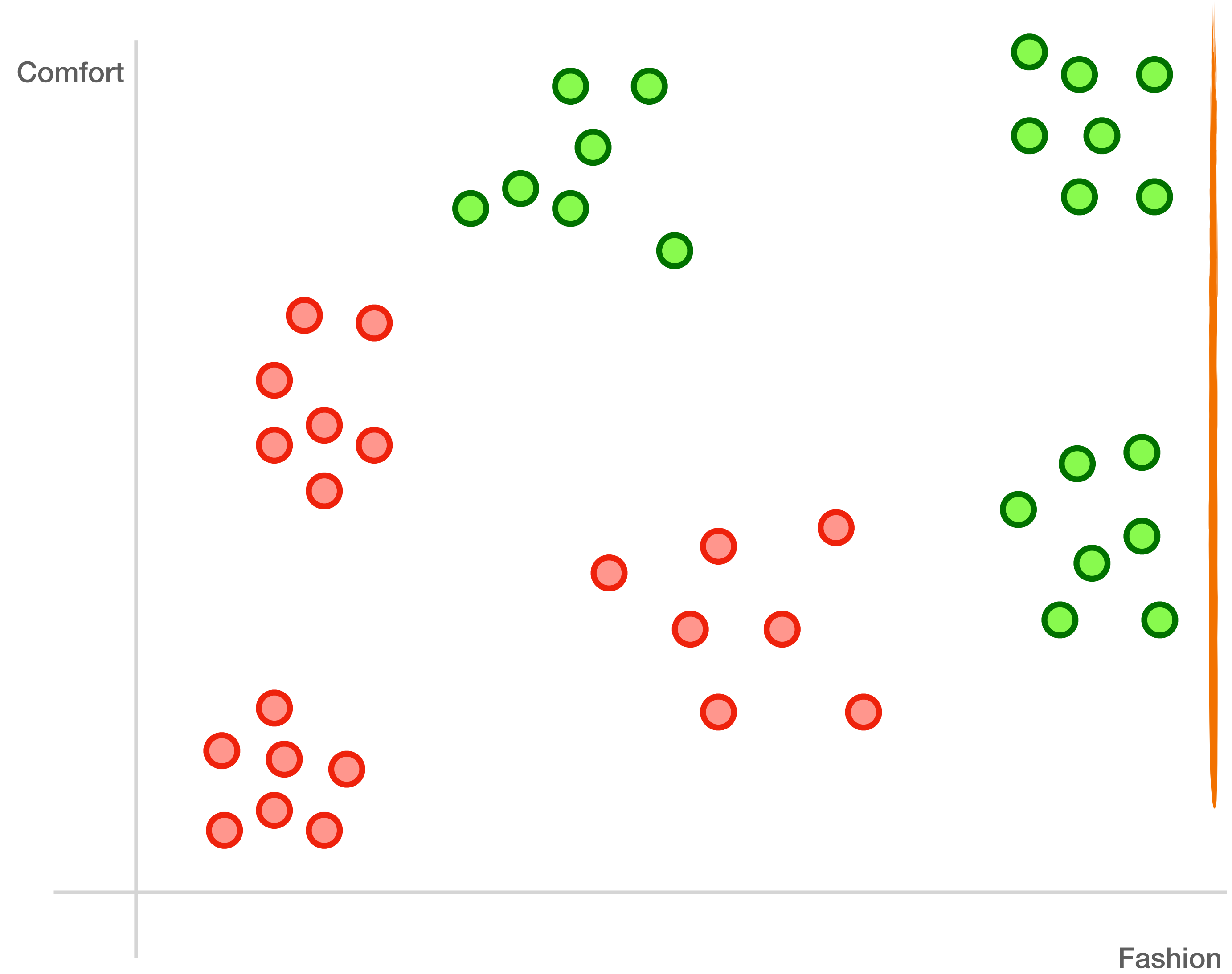


**“split”**

“split”

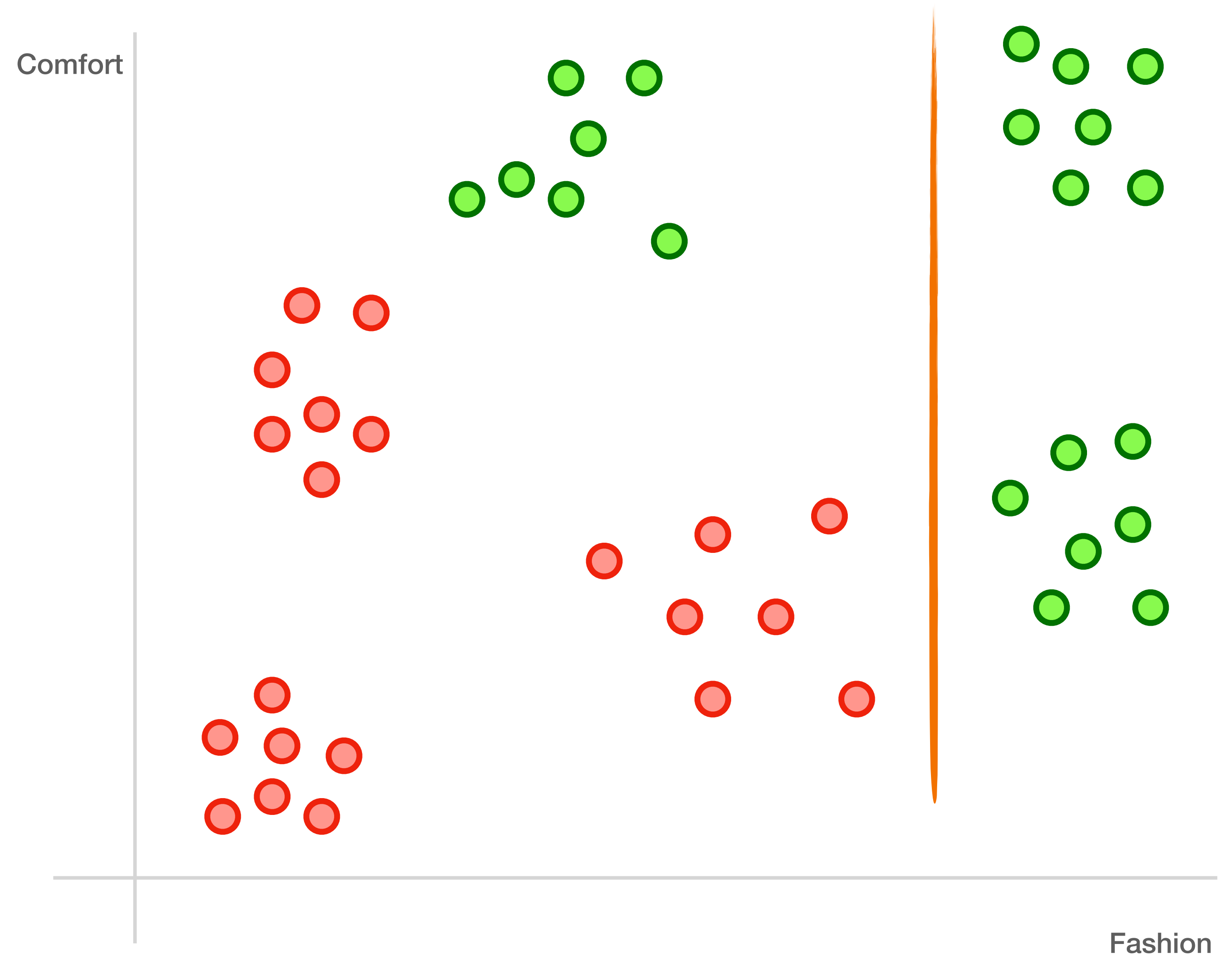


“split”

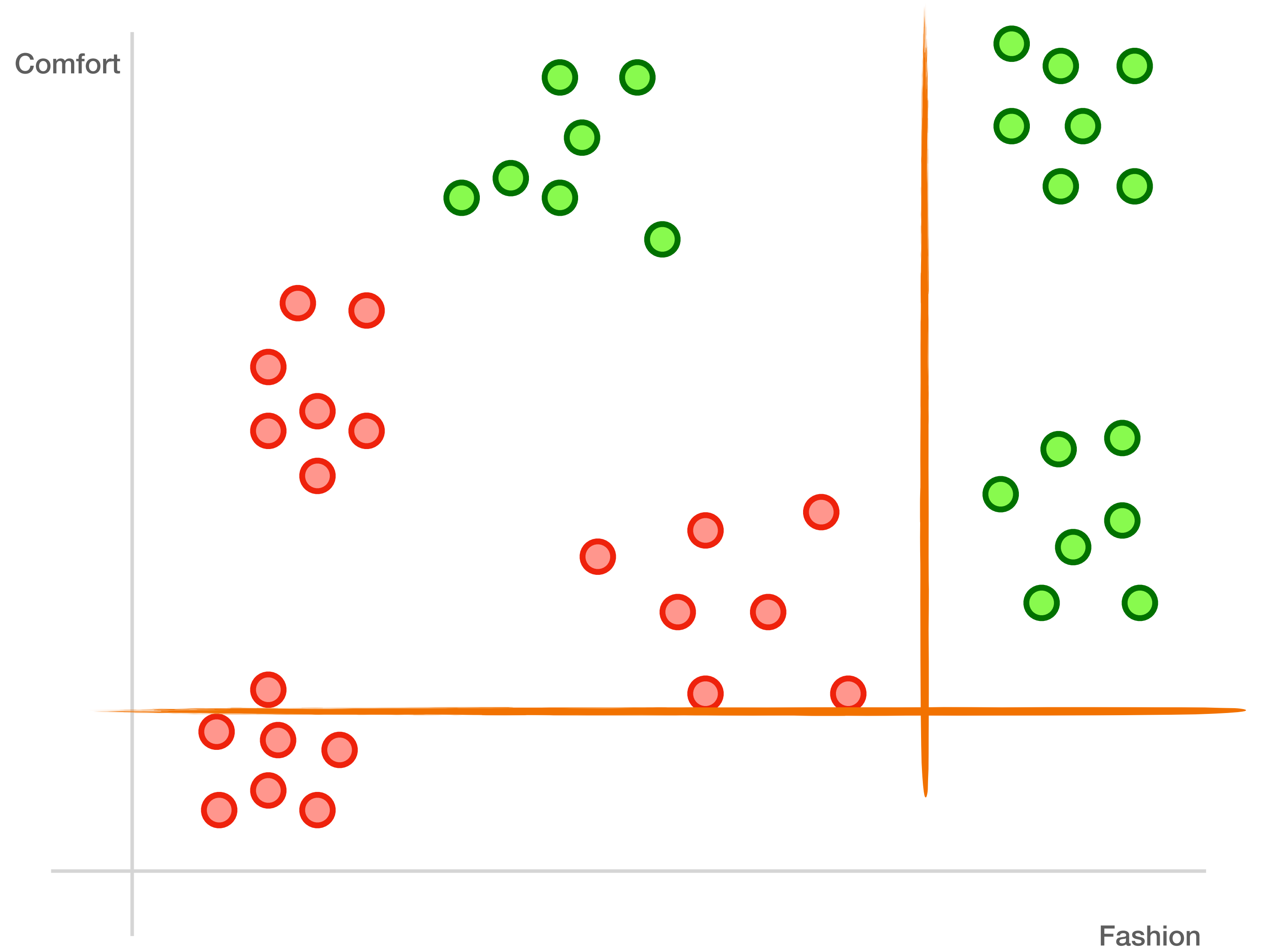




“split”

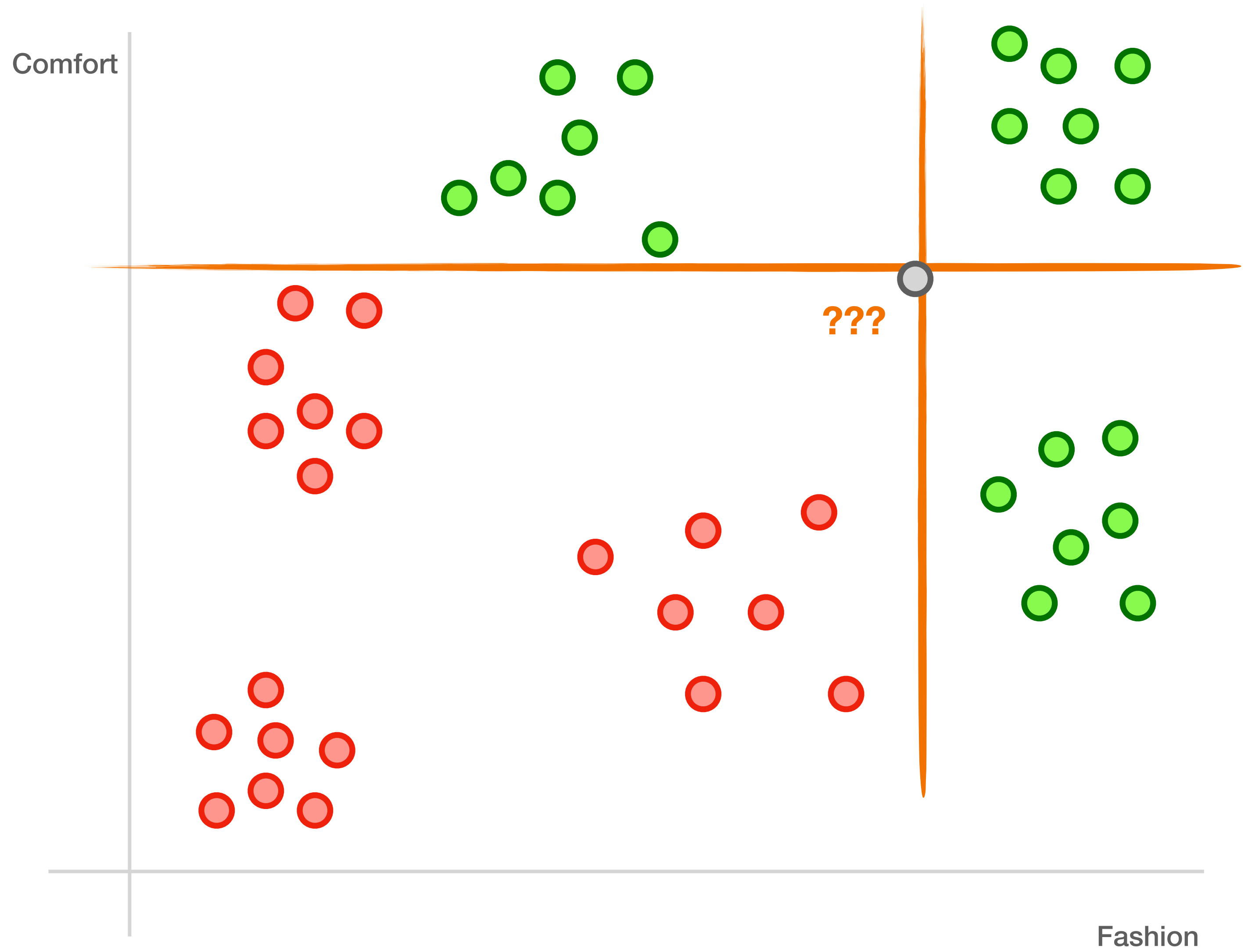


“split”



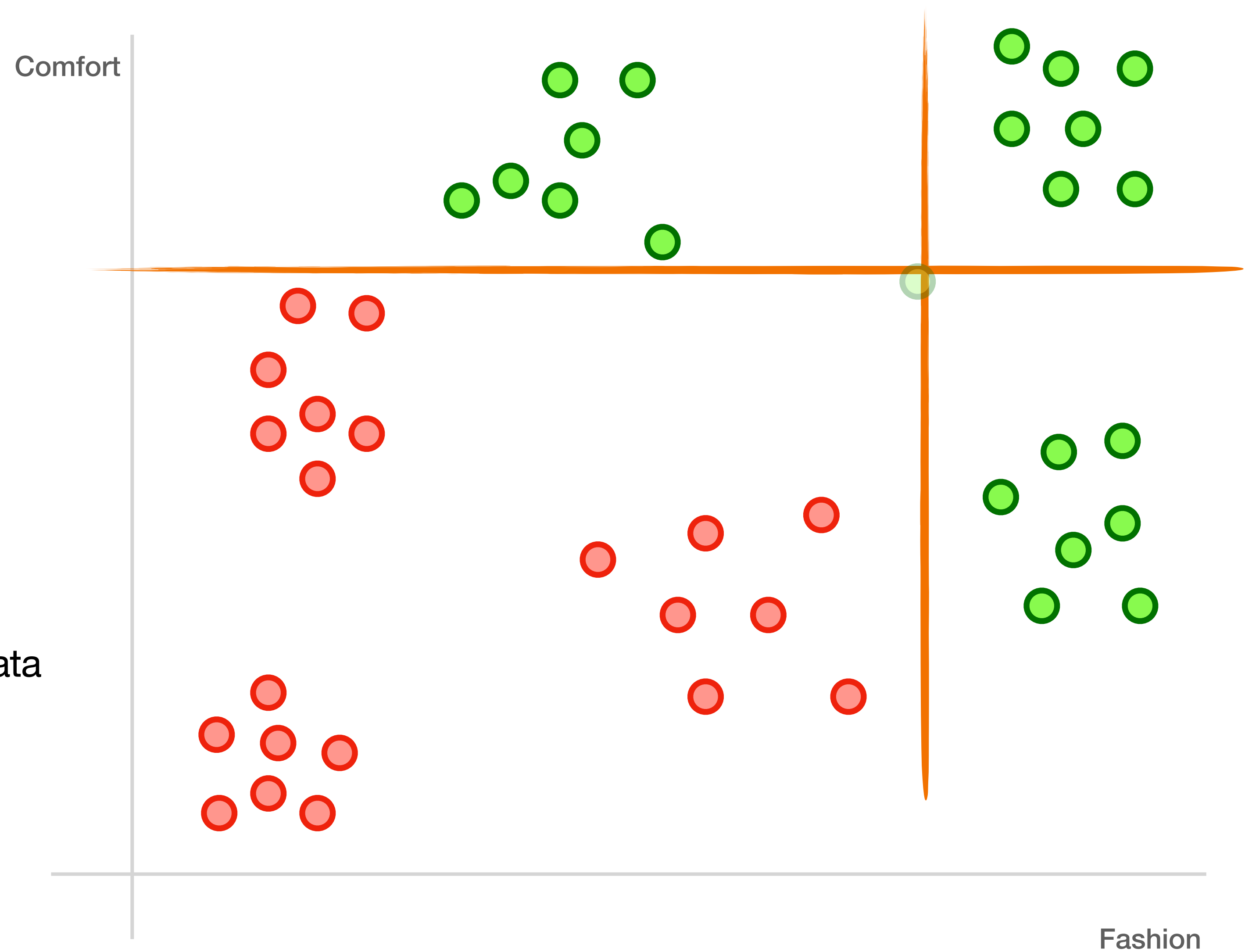
this is fine,  
but... 

“split”



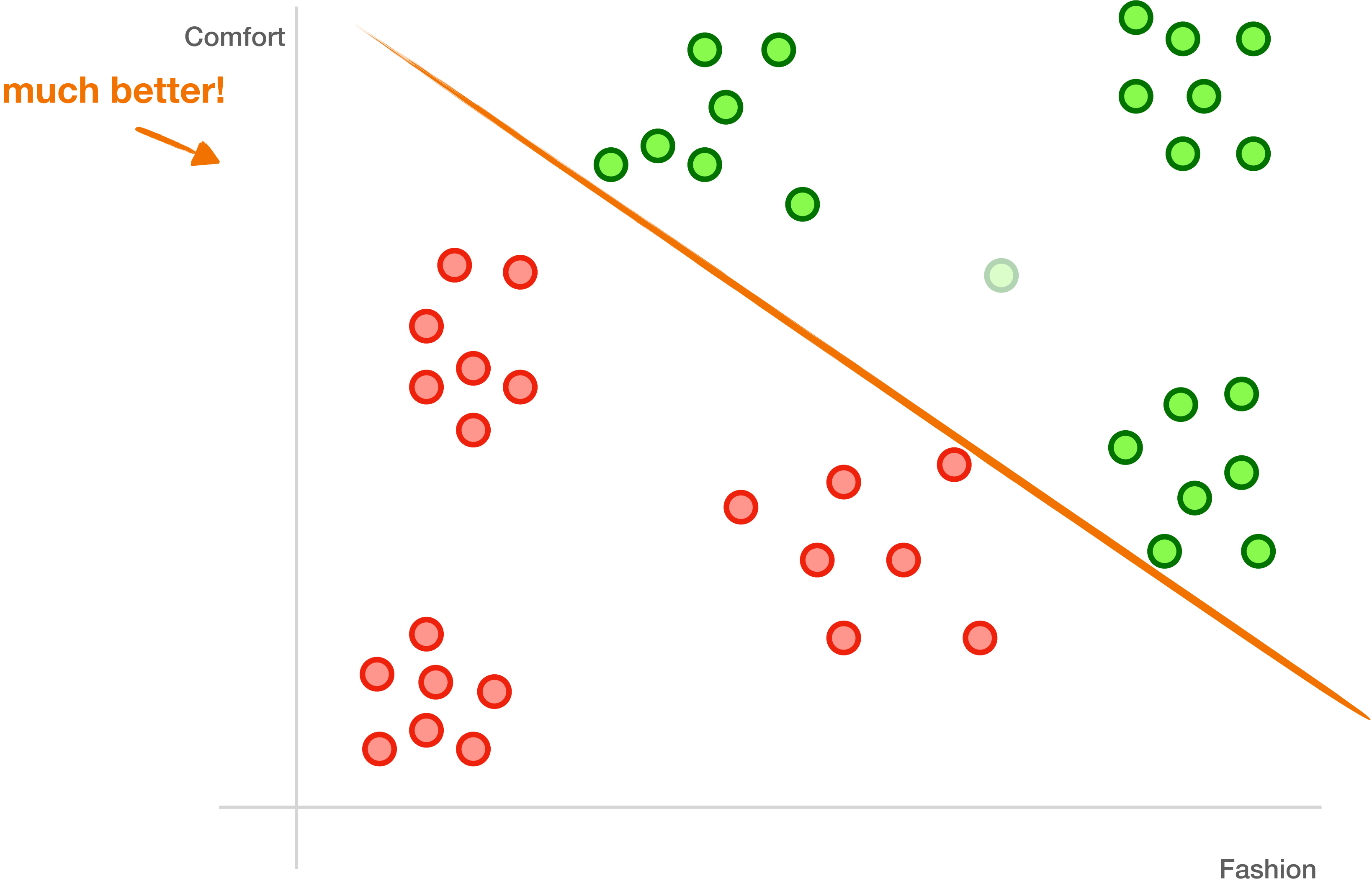
## “split”

- the **binary splits** in decision trees often don't do well in complex, multivariate data

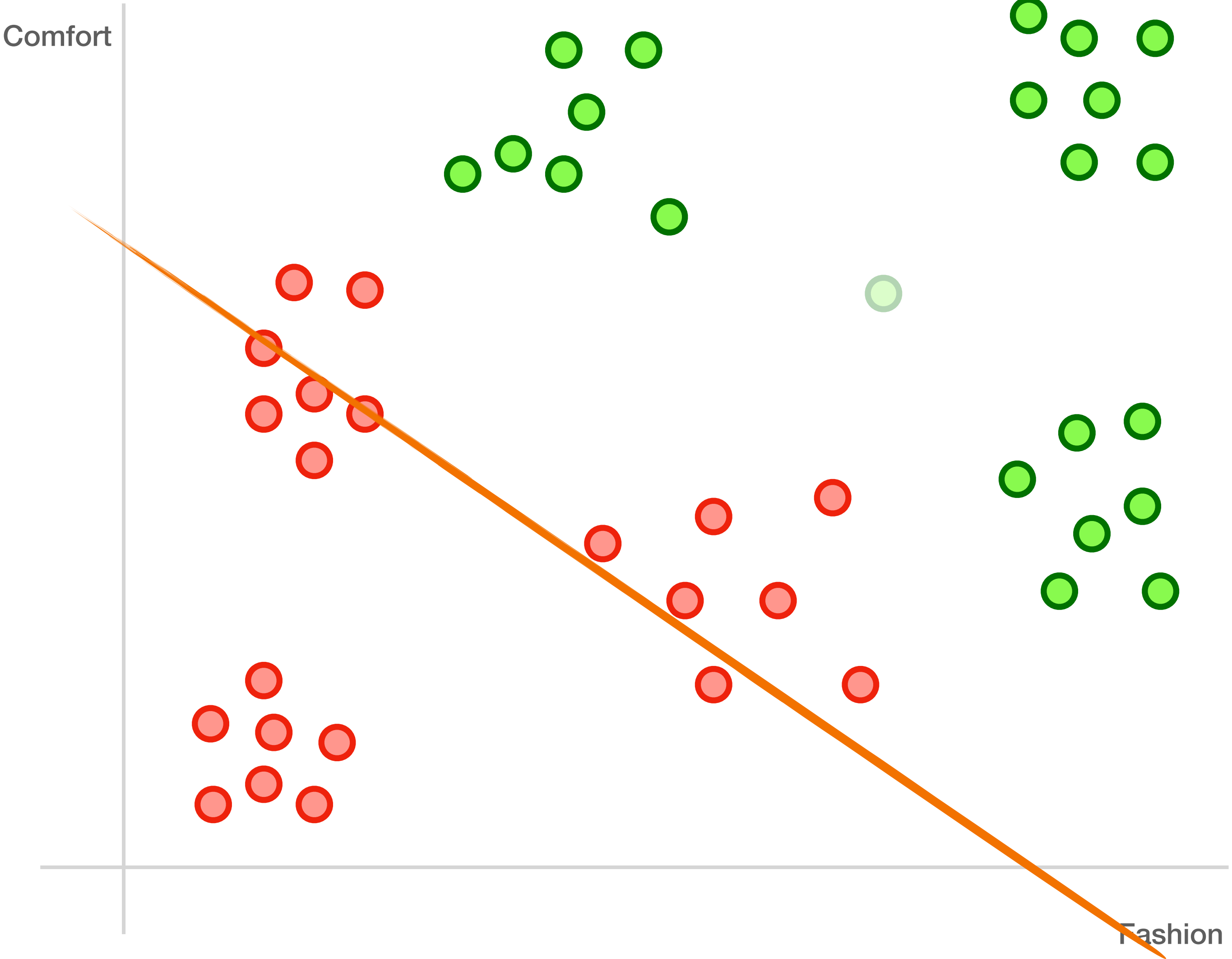


we need a more complex model  
**Support vector machines!**

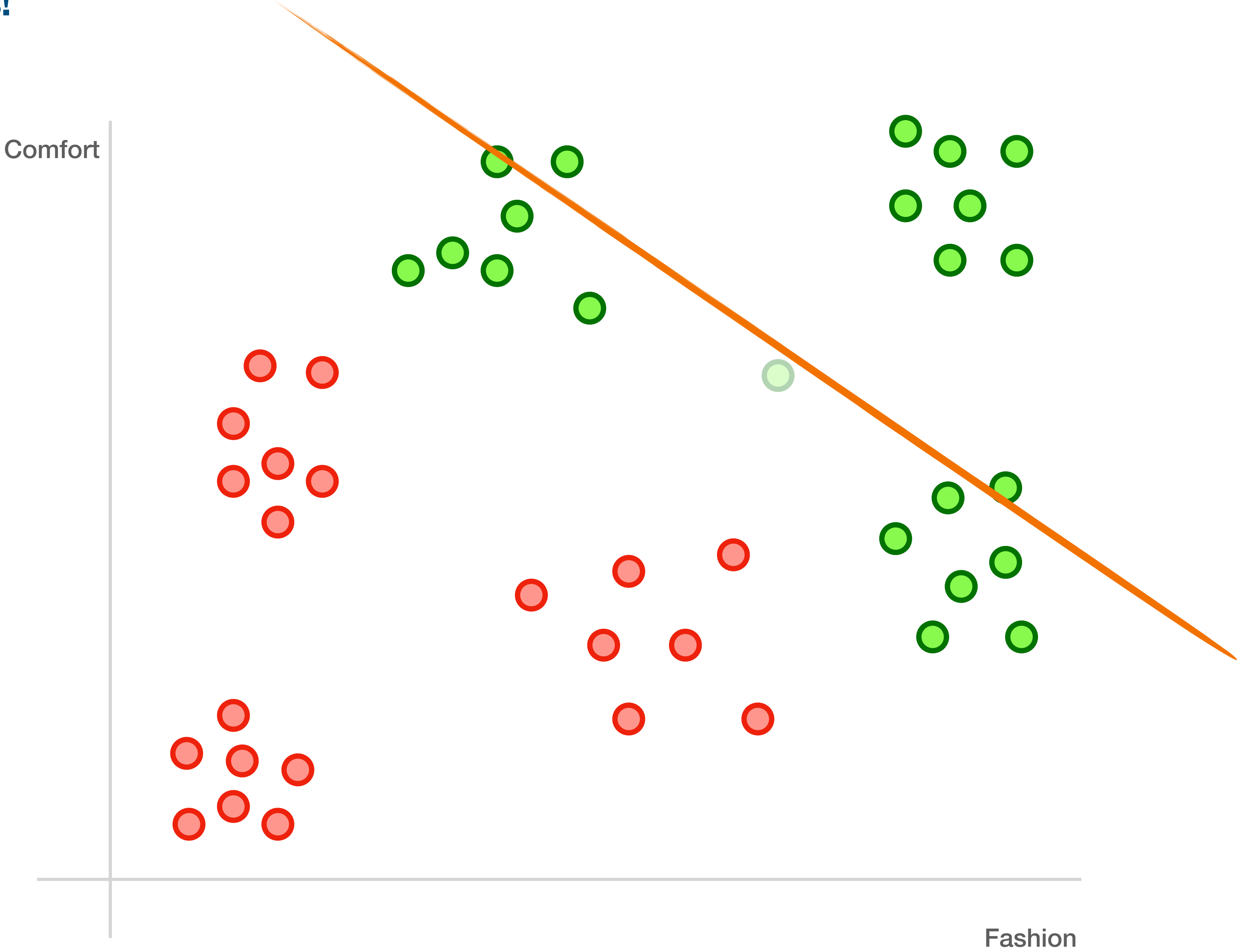
# Support vector machines!



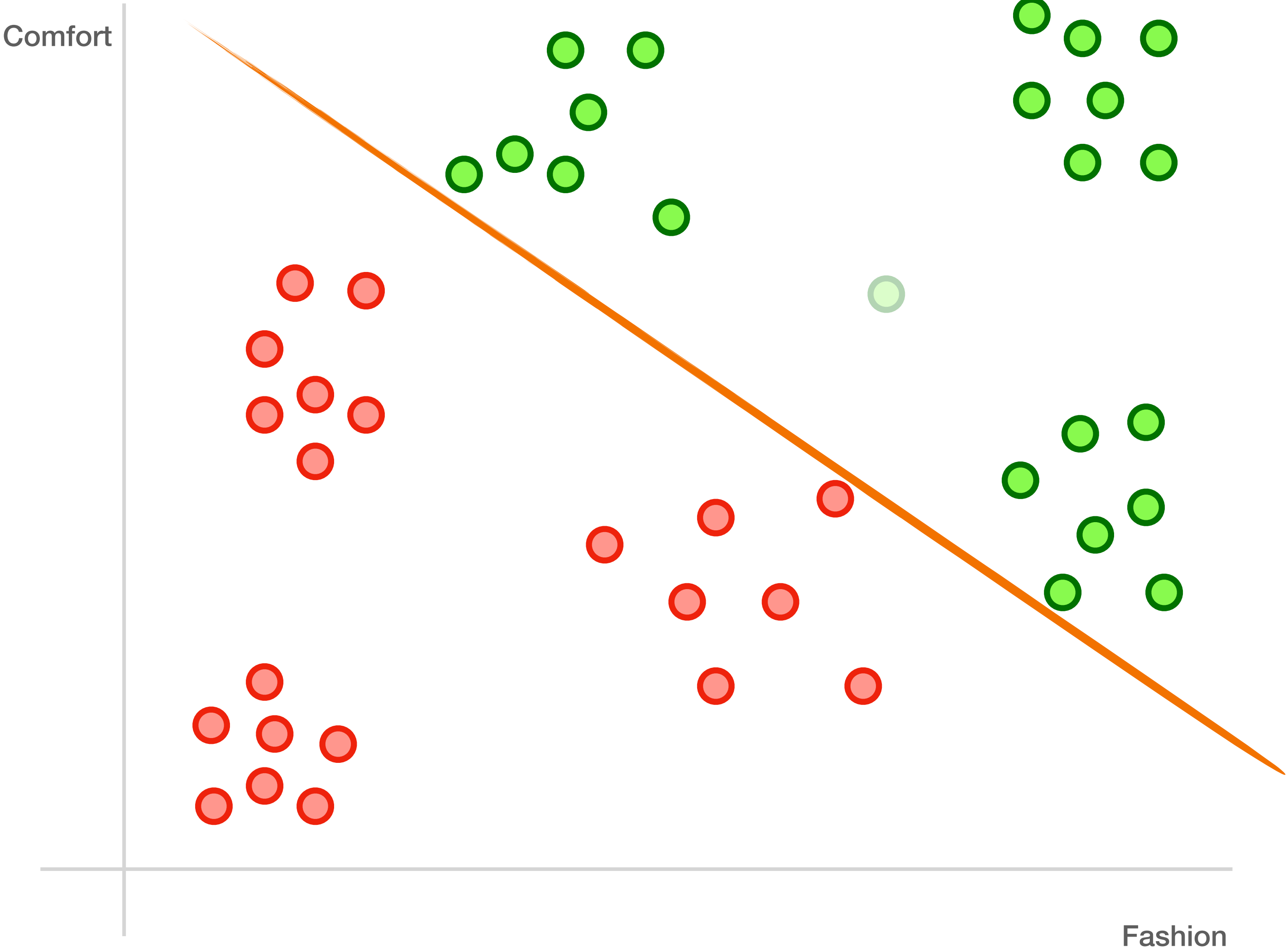
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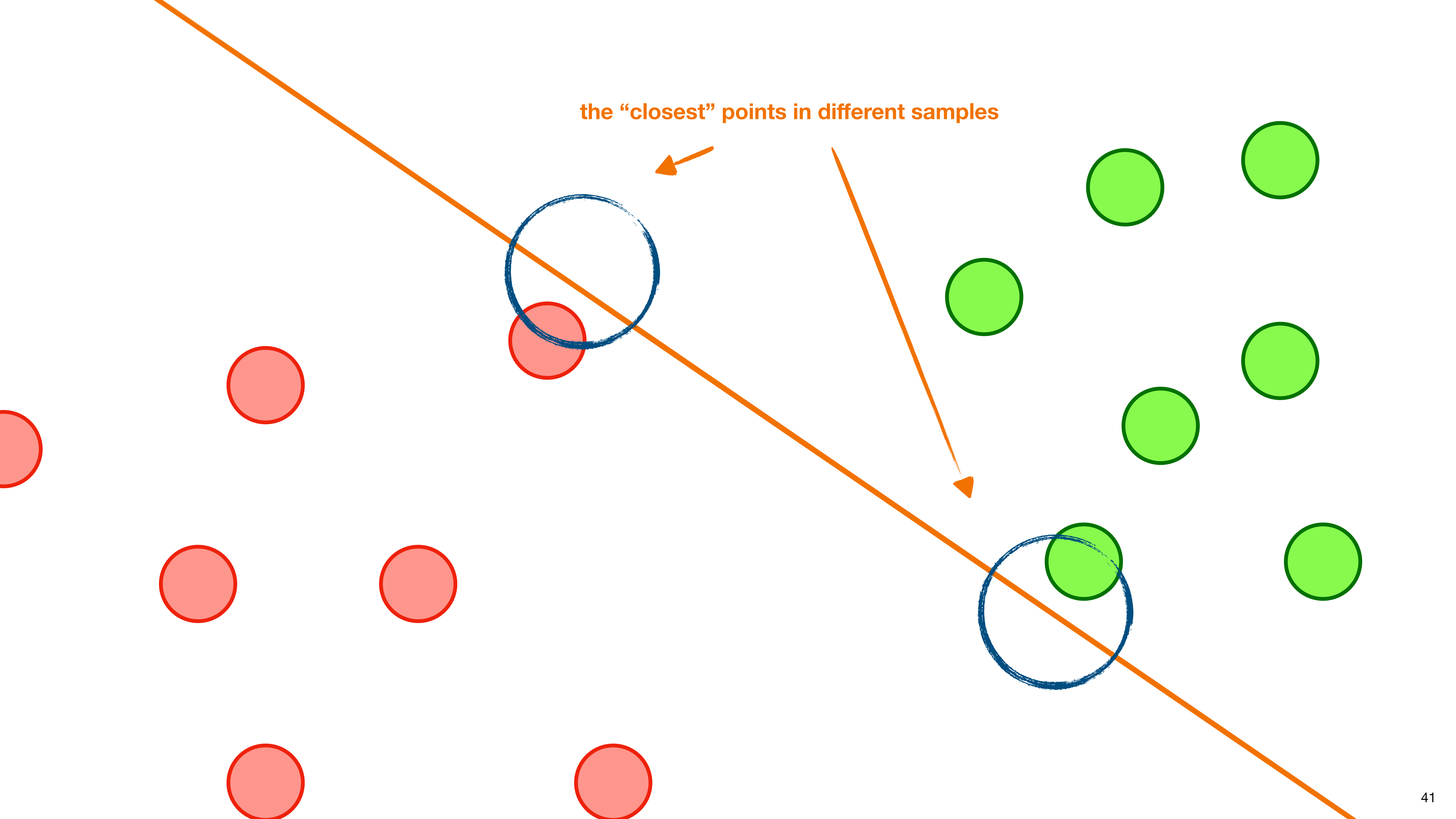


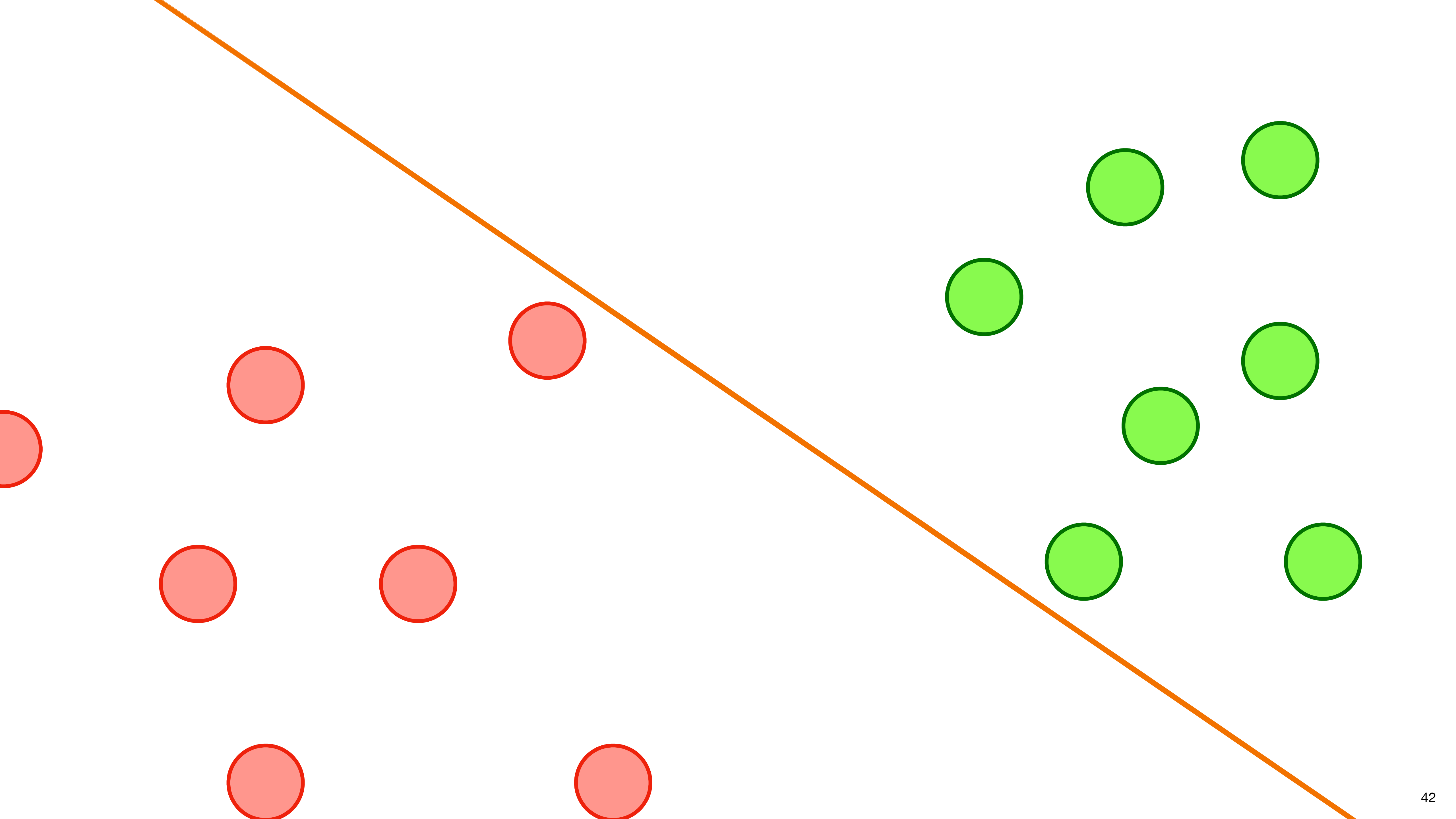
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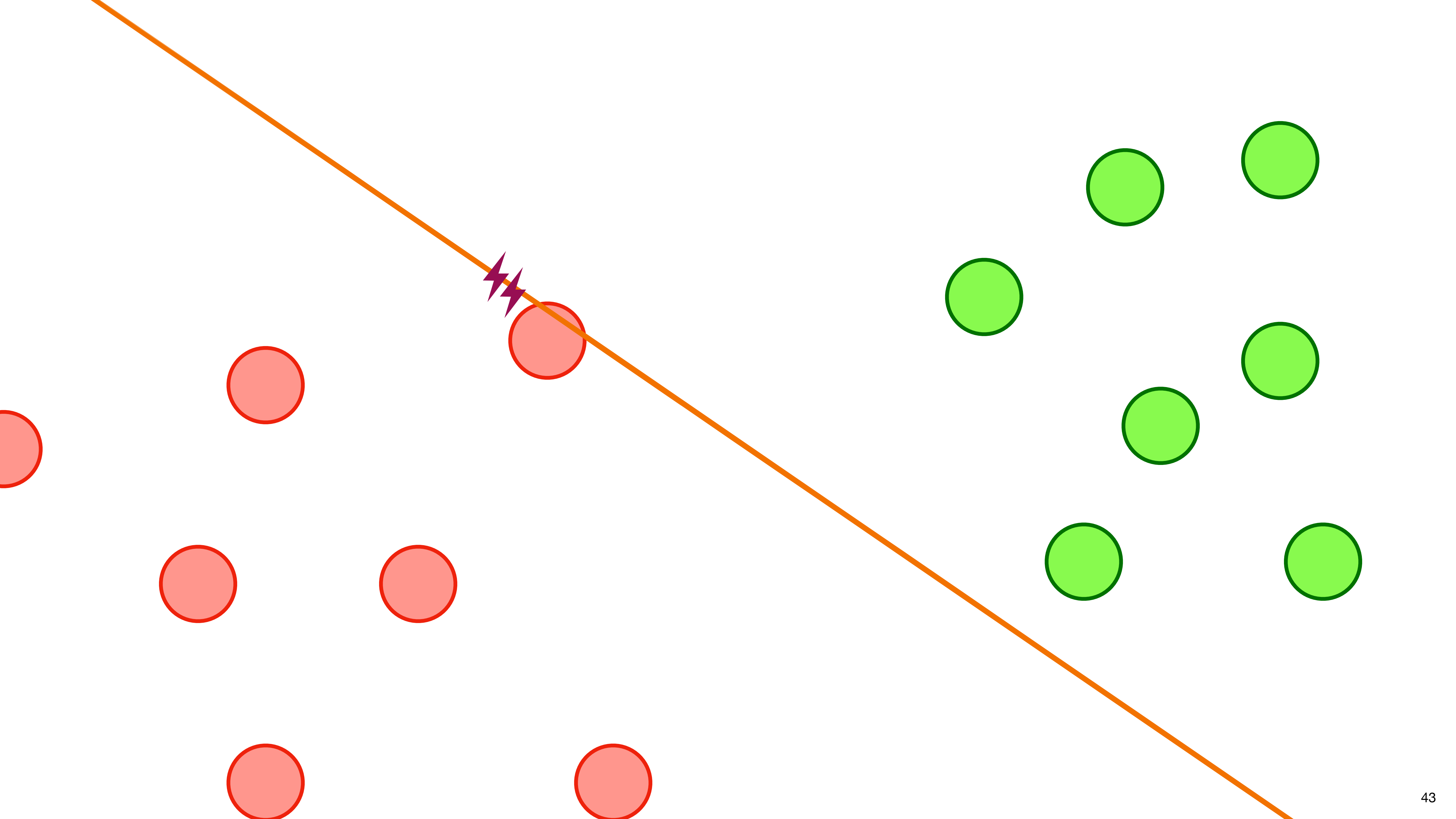


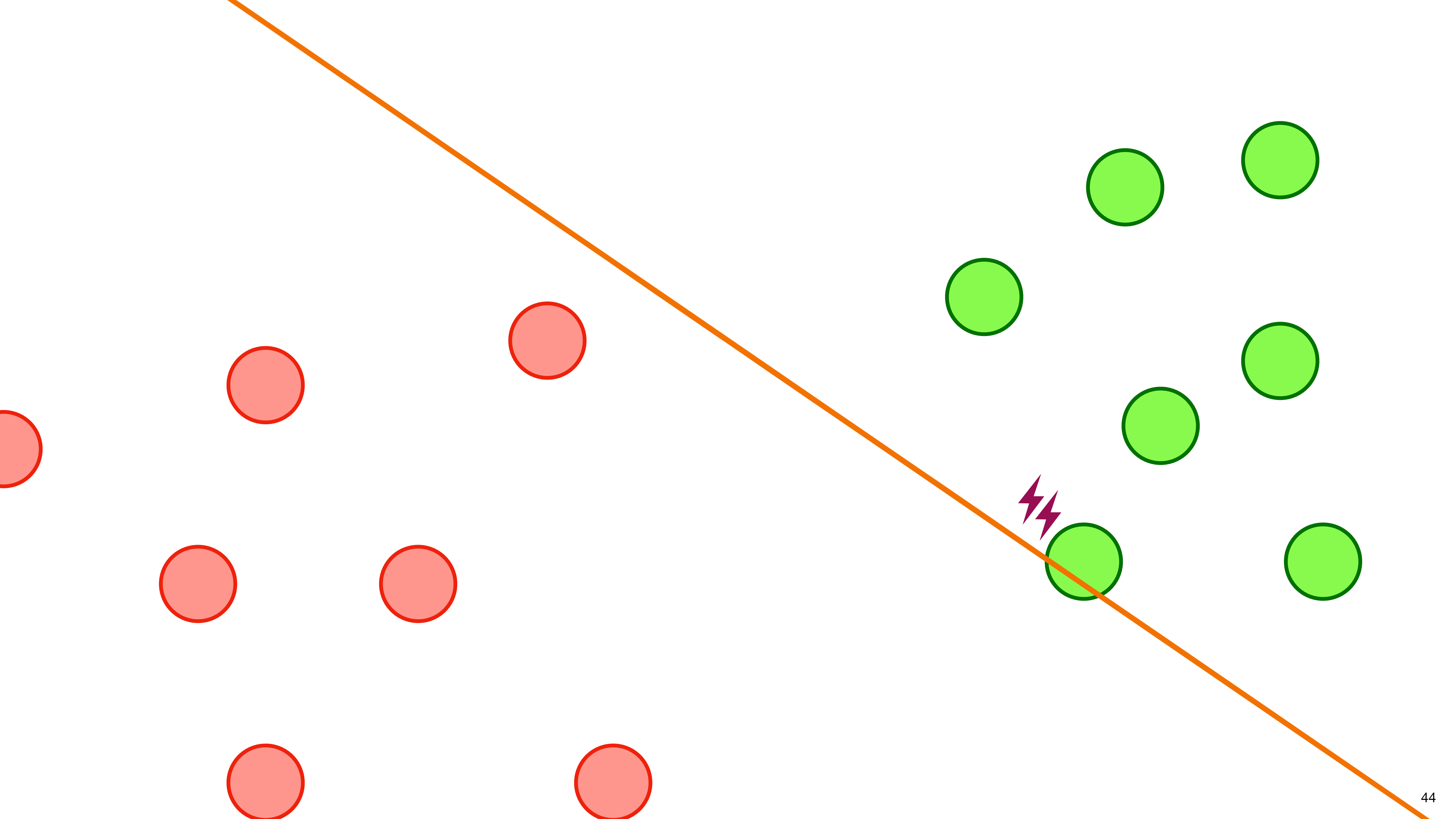


the "closest" points in different samples

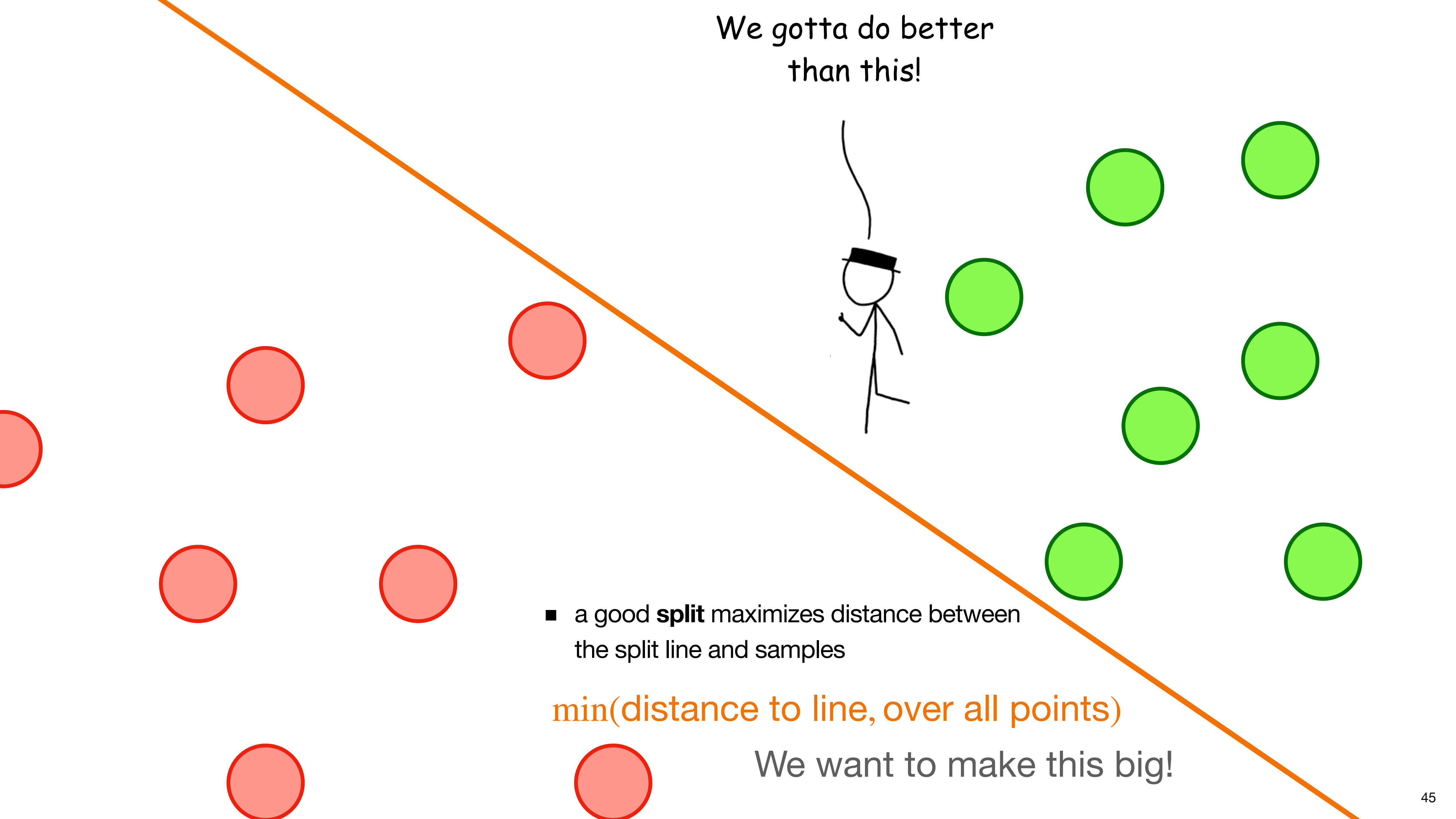








We gotta do better than this!



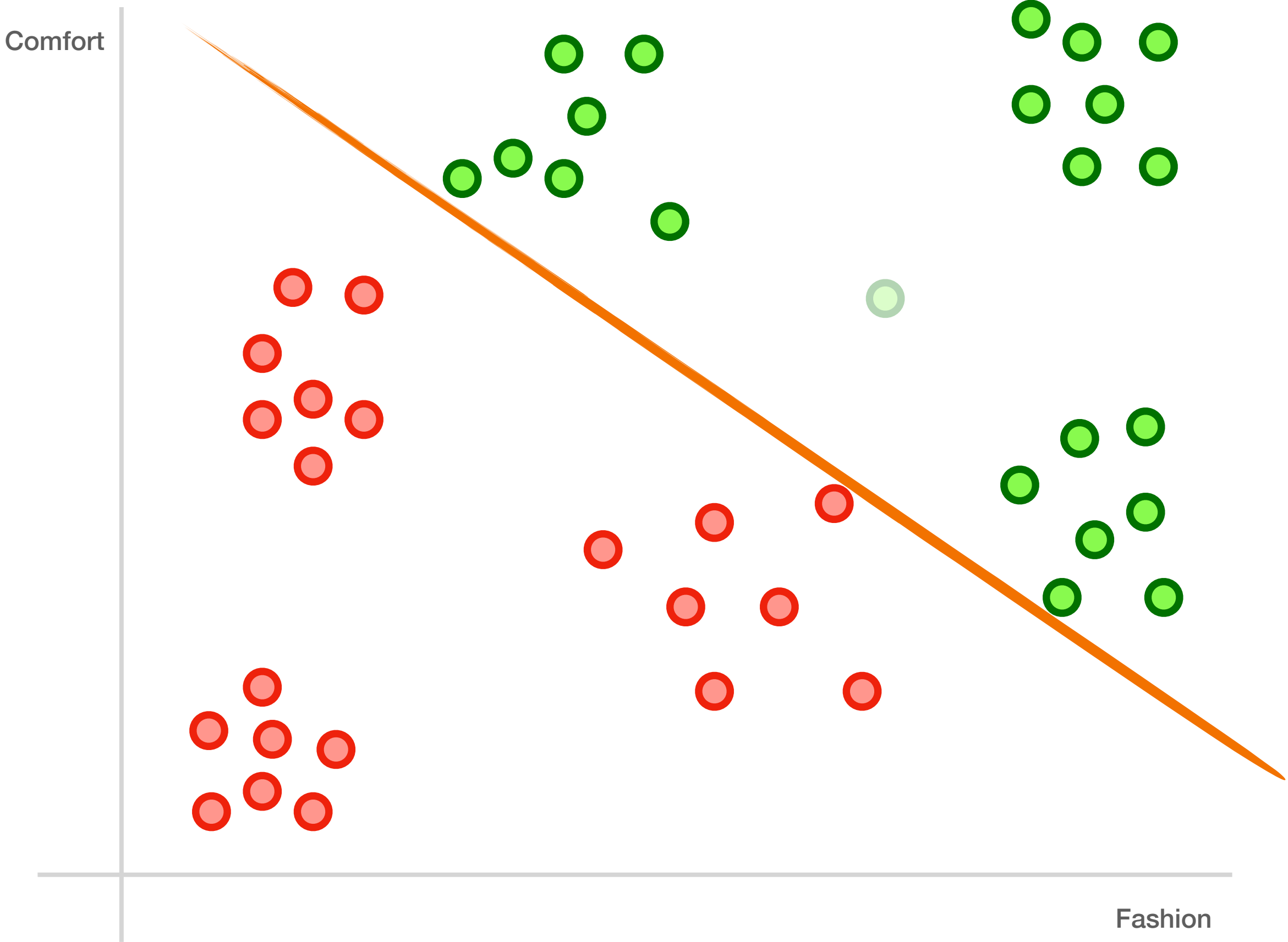
- a good **split** maximizes distance between the split line and samples

min(distance to line, over all points)

We want to make this big!

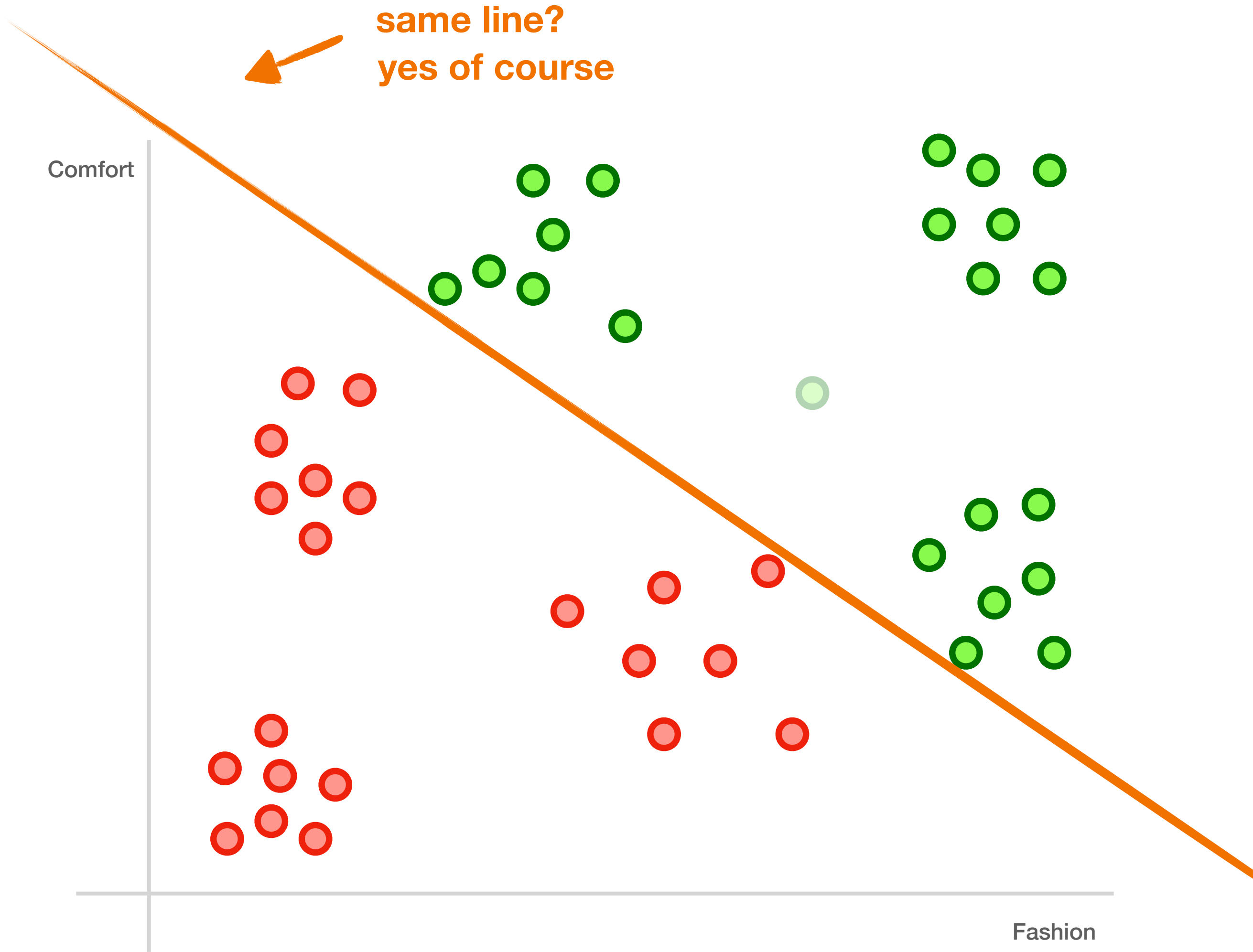
# Support vector machines!

max(distance to line, over all points)



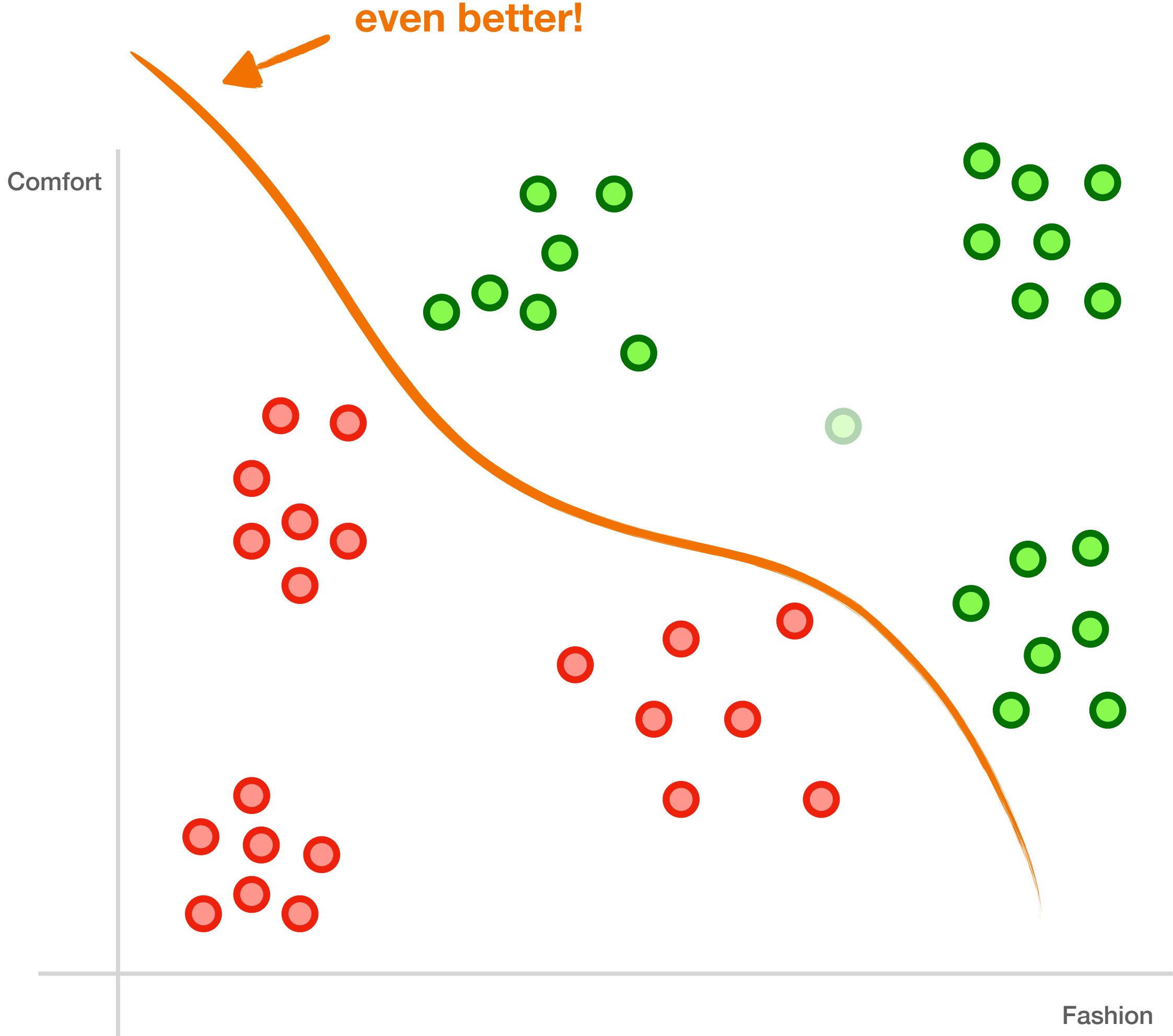
# Support vector machines!

$\max(\text{distance to line, over all points})$



# Support vector machines!

max(distance to line, over all points)

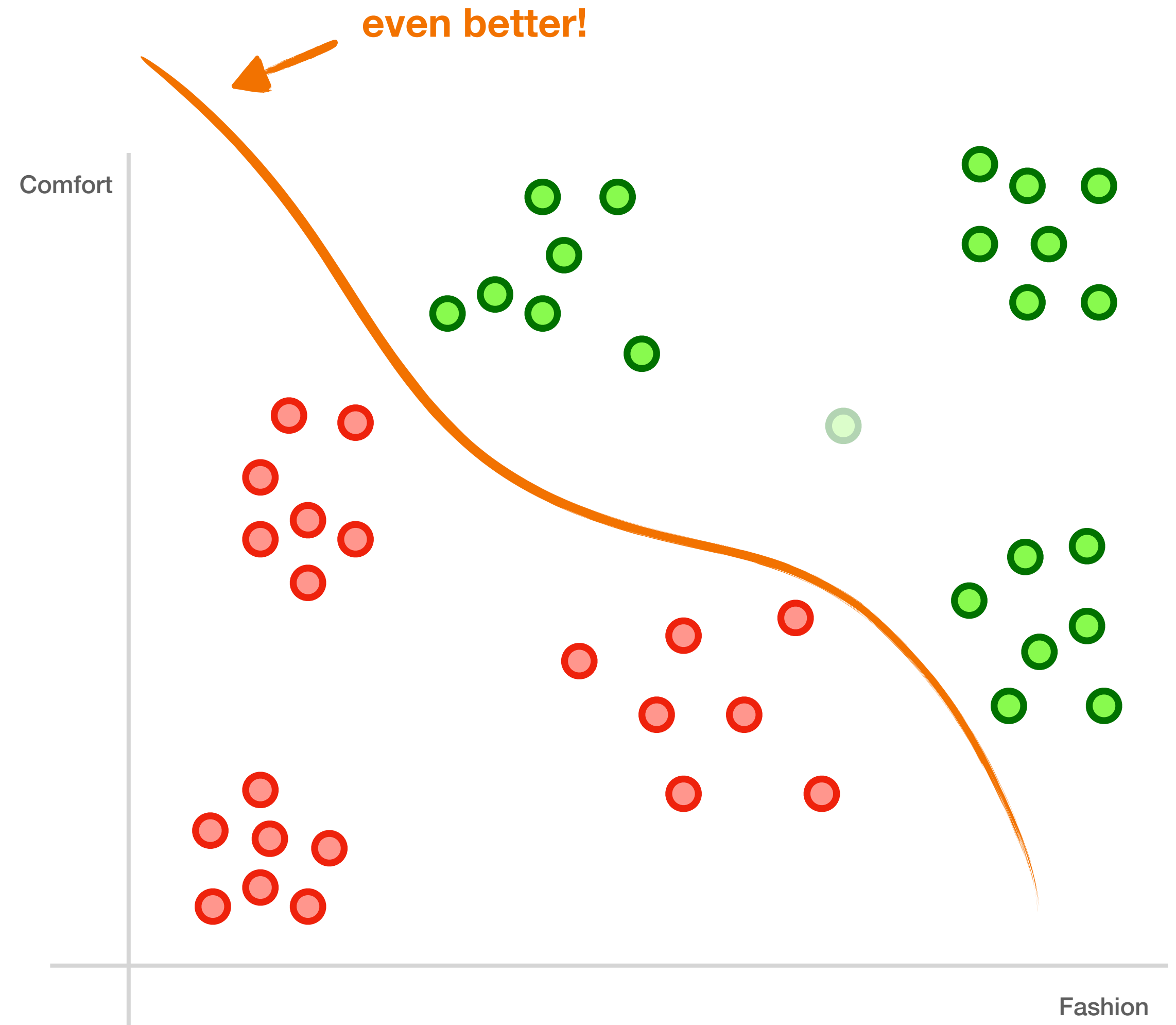




# Support vector machines!

max(distance to line, over all points)

- **support-vector machines** are classifiers that divide data by class, aiming to create a **margin** that's as wide as possible.
- They use non-linear functions



***BACK*** ←  
***TO***  
***THE PROBABILITY***

**Internal Memo:**

146 Hagley Road, Birmingham  
Birmingham B3 3PJ

From the Desk of  
Mr. Jerry Smith  
Date: 13/01/14

**Attn: Sir/Madam,**

I seize this opportunity to extend my unalloyed compliments of the new season to you and your family hoping that this year will bring more joy, happiness and prosperity into your house hold.

I am certain that by the time you read this letter I might have already gone back to my country **United Kingdom**. I visited South Africa during the New Year period and during my stay, I used the opportunity to send you this letter believing that it will reach you in good state.

# PROBABILITY

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“unalloyed complements”



Spam

“\$100,000 dollars”



Spam

“relative dying of cancer”



Spam

# PROBABILITY

IF we have this

“unalloyed complements”



THEN we have this

Spam

“\$100,000 dollars”



Spam

“relative dying of cancer”



Spam

**IF we have this THEN we have this**

**IF we have this THEN we have this**

$$A \mid B$$

**IF** we have this **THEN** we have this

$A \mid B$

- Is Spam
- “Nigerian Prince”



**IF** we have this **THEN** we have this

*spam* | *nigerian prince*

IF we have this **THEN** we have this

$$P(\textit{spam} \mid \textit{nigerian prince})$$

high?	Nigerian prince	→	spam likely
low?	Nigerian prince	→	not spam

- **conditional probabilities** can be used as a classifier!

# PROBABILITY

$$P(\textit{spam} | \textit{nigerian prince}) = \frac{P(\textit{spam})P(\textit{nigerian prince} | \textit{spam})}{P(\textit{nigerian prince})}$$

# PROBABILITY

$$P(\textit{spam} | \textit{nigerian prince}) = \frac{P(\textit{spam})P(\textit{nigerian prince} | \textit{spam})}{P(\textit{nigerian prince})}$$

**% of spam in dataset** →

**% of spam in dataset that relates to Nigerian prince** →

**% of Nigerian prince in dataset** ↗

## Naïve Bayes Classifier

$$P(\textit{spam} \mid \textit{nigerian prince}, \textit{offer}) = \frac{P(\textit{spam})P(\textit{nigerian prince} \mid \textit{spam})}{P(\textit{nigerian prince})} \frac{P(\textit{offer} \mid \textit{spam})}{P(\textit{offer})}$$



- **conditional probabilities** can be used as a classifier!
- a classifier made this way, however, is “**naïve**” when extended to multiple features

**multiplication for AND assumes independence!**  
**“naïve”**

**Three classifiers! That's a lot.**  
**Let's get to the *long lab!***