



# AI Bridge

Lecture 6

# Classification!

quick  
review  
wine dataset

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol



**White = 0**

**Red = 1**



■ categorical label outputs are named “**classes**”

# Classification!

quick  
review  
wine dataset

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
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- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol

that's a lot  
of features!



Model



**White = 0**

**Red = 1**



■ categorical label outputs are named “**classes**”

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol

■ Linear models might not be the best in some cases

# Decision Trees

# Decision Trees



# Decision Trees



Can I afford it?

# Decision Trees



Can I afford it?

Is it comfortable?

# Decision Trees



Can I afford it?

Is it comfortable?

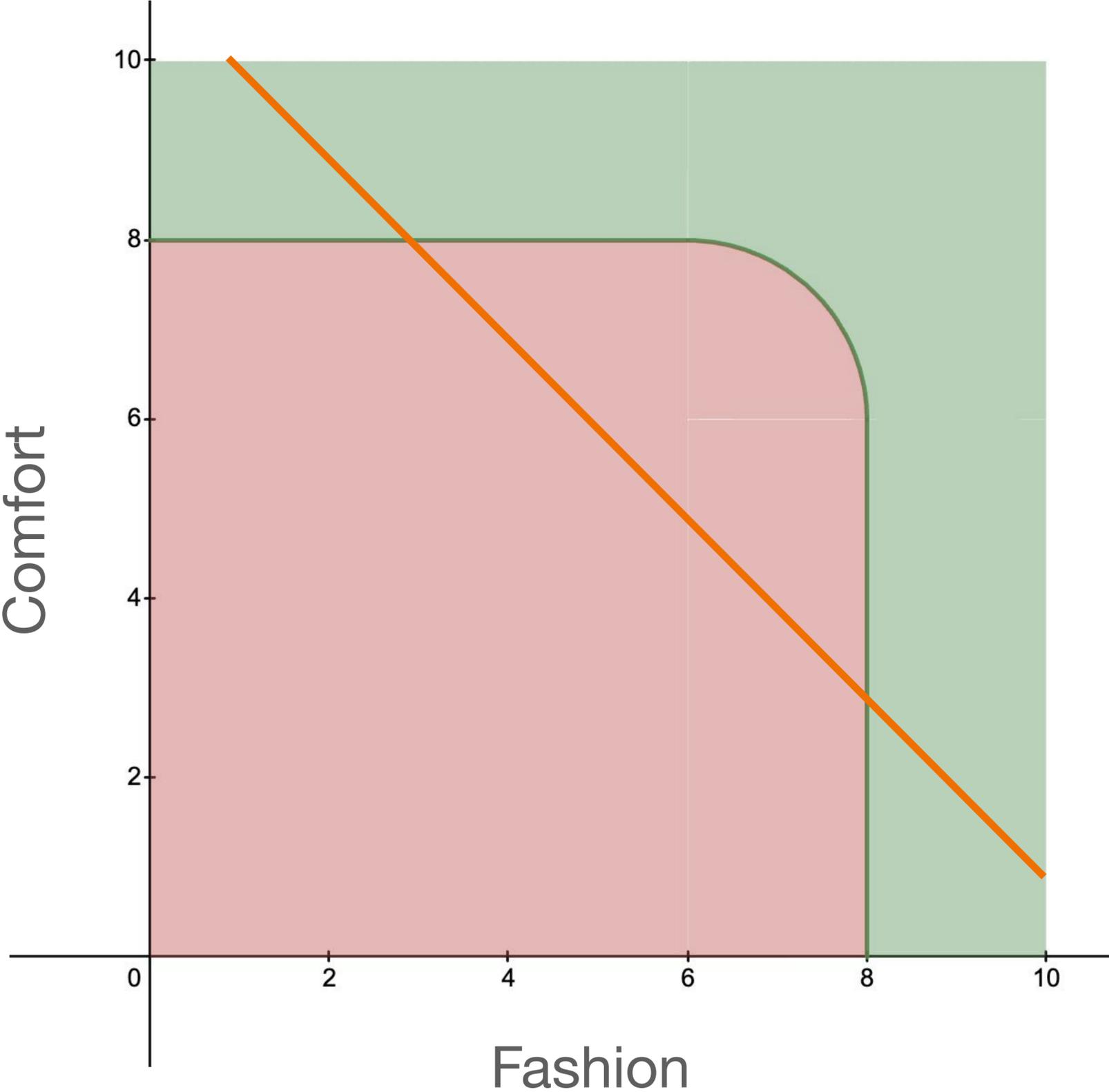
Is it fashionable?

# Decision Trees

Can I afford it?

Is it comfortable?

Is it fashionable?



# Decision Trees



# Decision Trees

that seems awfully hard-coded!

- flowcharts of decisions can create an explainable and repeatable graph of predictions



# Decision Trees

Price	Comfort	Fashion	Purchased?
\$70	4	6	No
\$120	5	8	No
\$20	4	4	No
\$60	1	8	Yes
\$60	6	3	No
\$80	8	8	Yes

# Decision Trees

**Purchased?**

No

No

No

Yes

No

Yes

# Decision Trees

No

No

No

Yes

No

Yes

# Decision Trees

No	Yes
No	No
No	Yes

# Decision Trees



0

0.38

0.44

0.5

- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.

0

0.38

0.44

0.5

- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.
- perfect groups => 0 **Gini Impurity** => 100% predictions

Fraction of that one class in group      Fraction of not that one class in the group

$$G = \sum_{i=1}^C P(i) \cdot (1 - P(i))$$

Add them up for all classes (in one side of the split)

- **Gini impurity** measures the homogeneity in a group

# Decision Trees

**Purchased?**

No

0

No

No

Yes

0.5

No

Yes

---

0.5

# Decision Trees

**Purchased?**

No

No

**0.38**

No

Yes

No

**0.5**

Yes

---

**0.88**

# Decision Trees

we gotta do better than this, right?



Purchased?

No

No 0

No

Yes

No 0.44

Yes

---

0.44

# Decision Trees

**just split  
again!**

**Purchased?**

No

No 0

No

Yes

No 0.44

Yes

---

0.44

# Decision Trees

1. Make splits (using features and thresholds)
2. Calculate Gini impurities
3. Select the split that results in the lowest Gini impurity sum
4. If unhappy, **just split again!**
5. Repeat 1-4 as much as needed



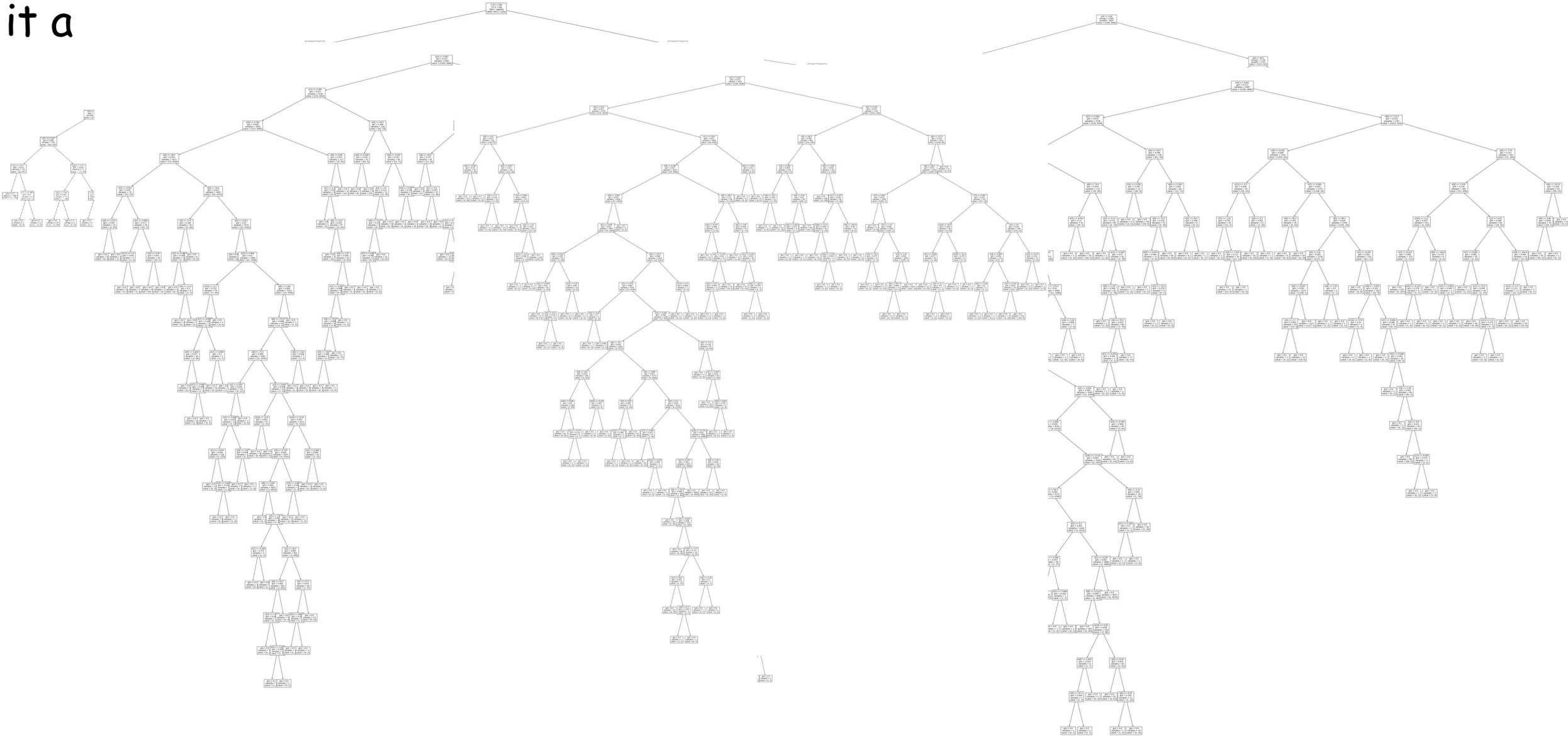
a hyperparameter

# Decision Trees

diverse

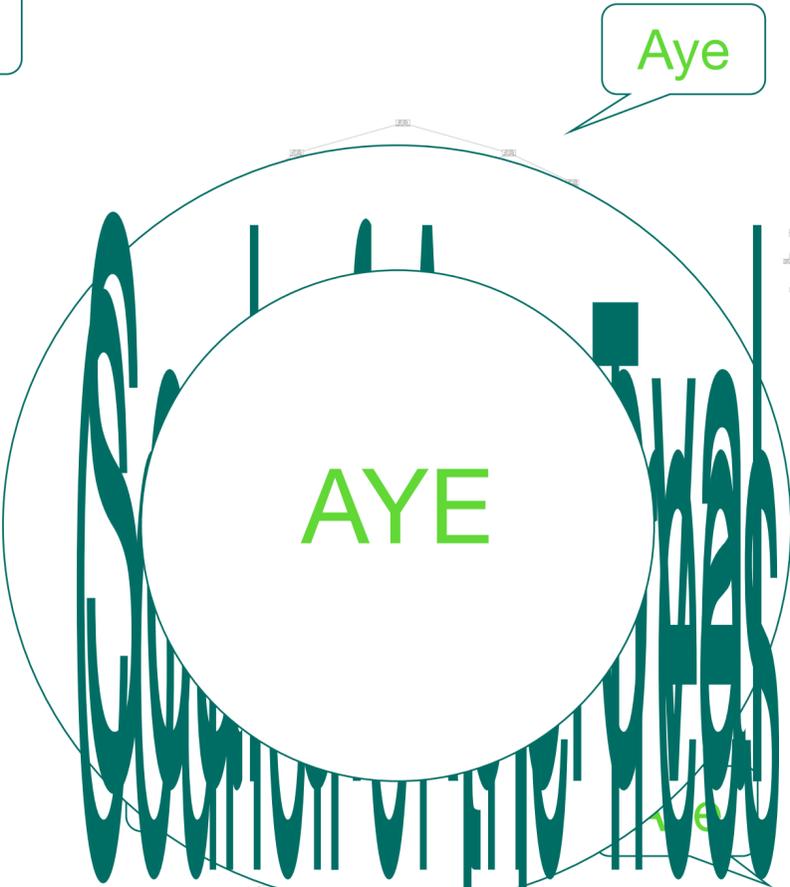
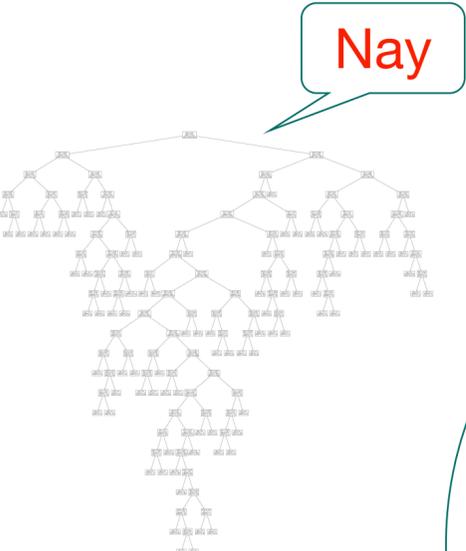
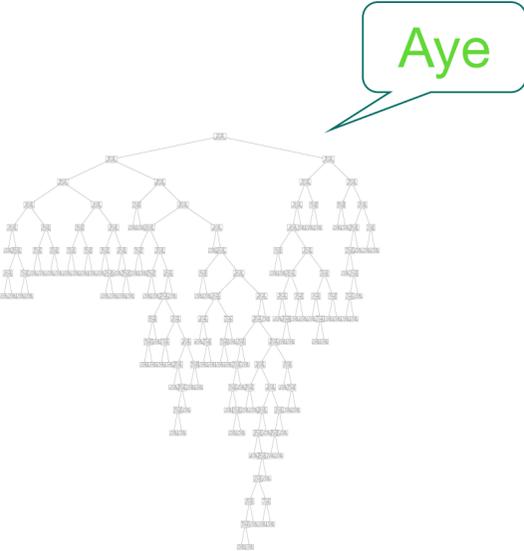


What if we do it a lot?



# Decision Trees

## Random Forest



Aye

Aye

Nay

Aye

Aye

Aye

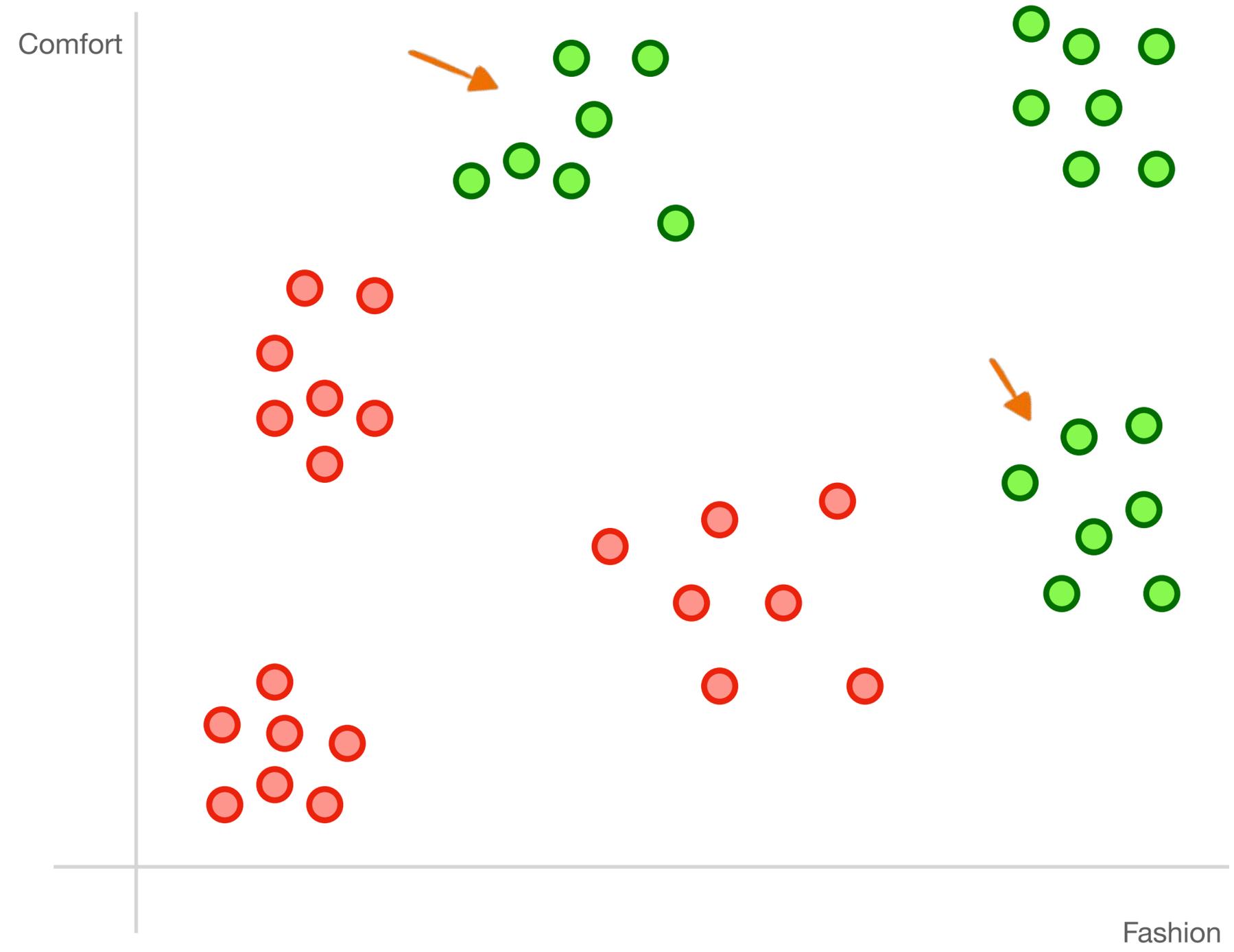
# Decision Trees

## Random Forest

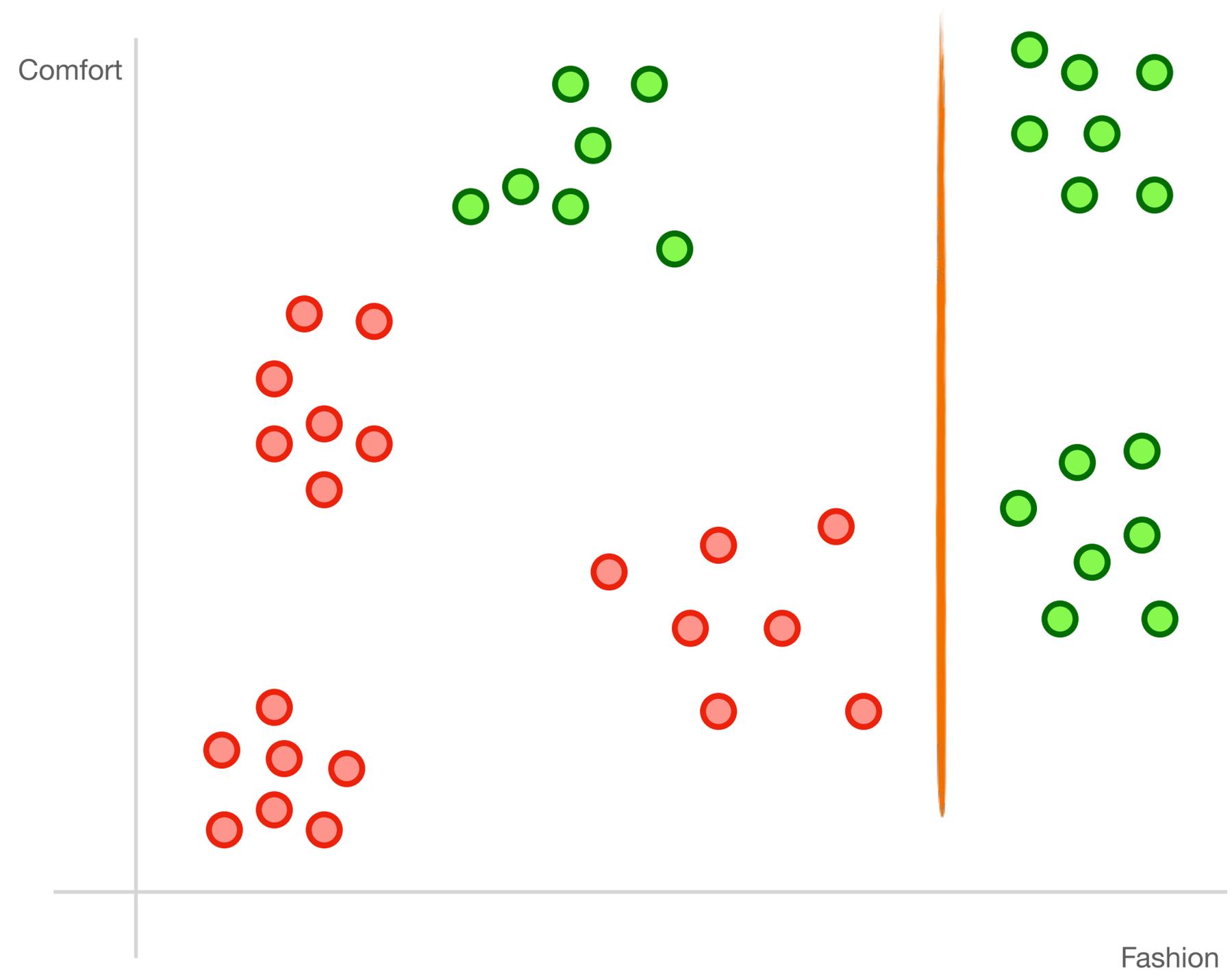
1. Make a lot of decision trees, on different portions of the data
2. For a new sample, run all of them
3. Combine their votes and take the majority

**“split”**

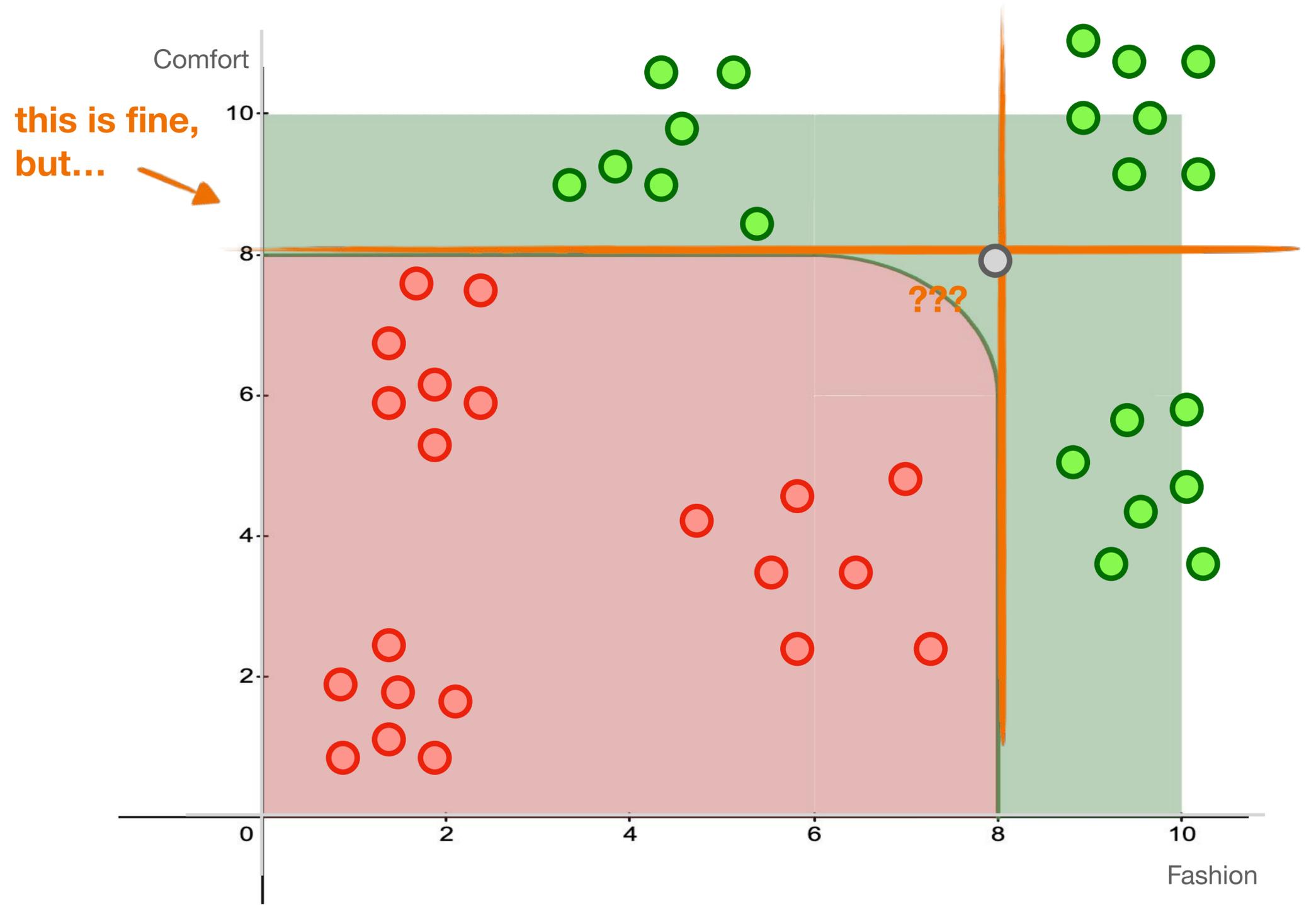
“split”



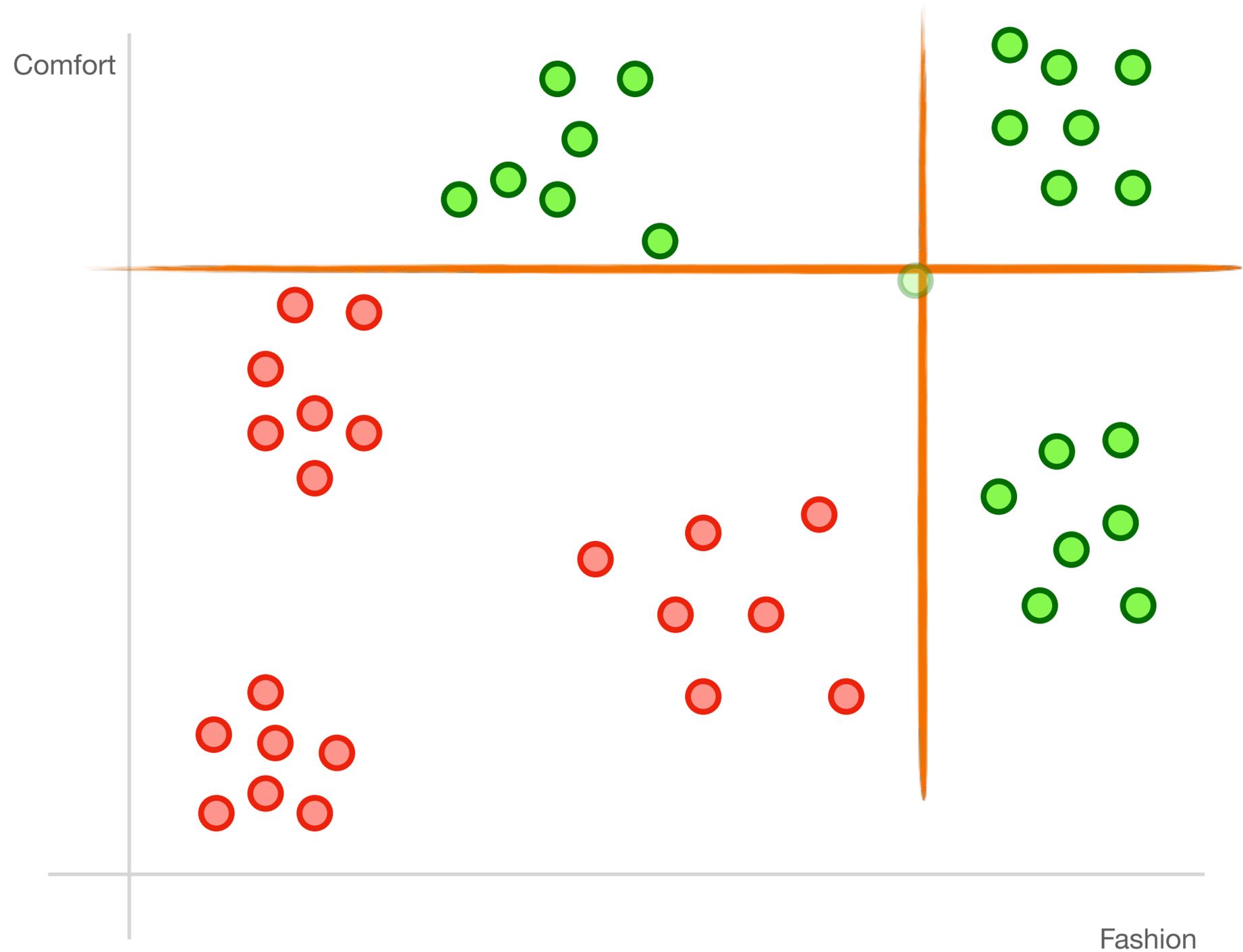
“split”



“split”



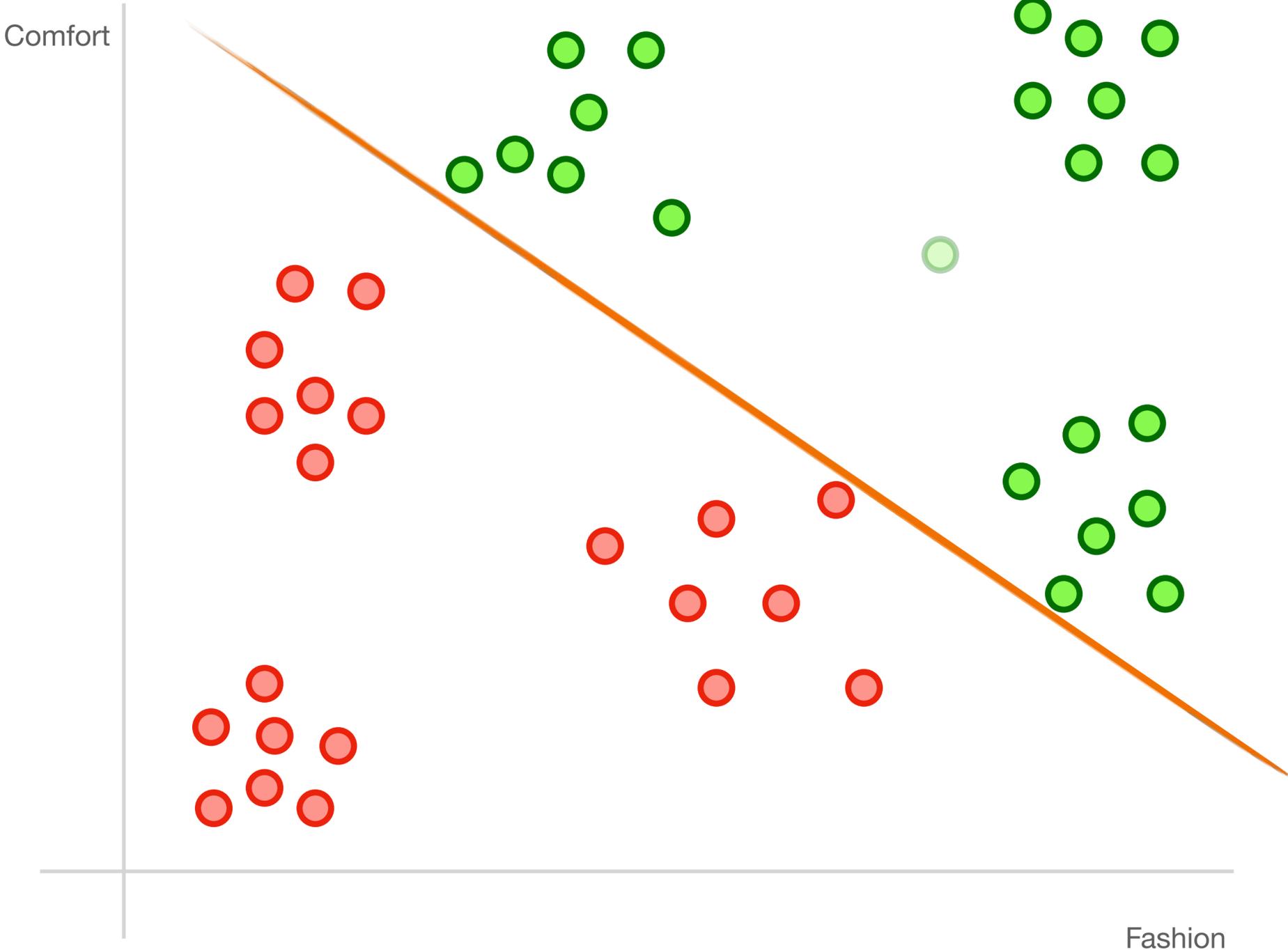
“split”



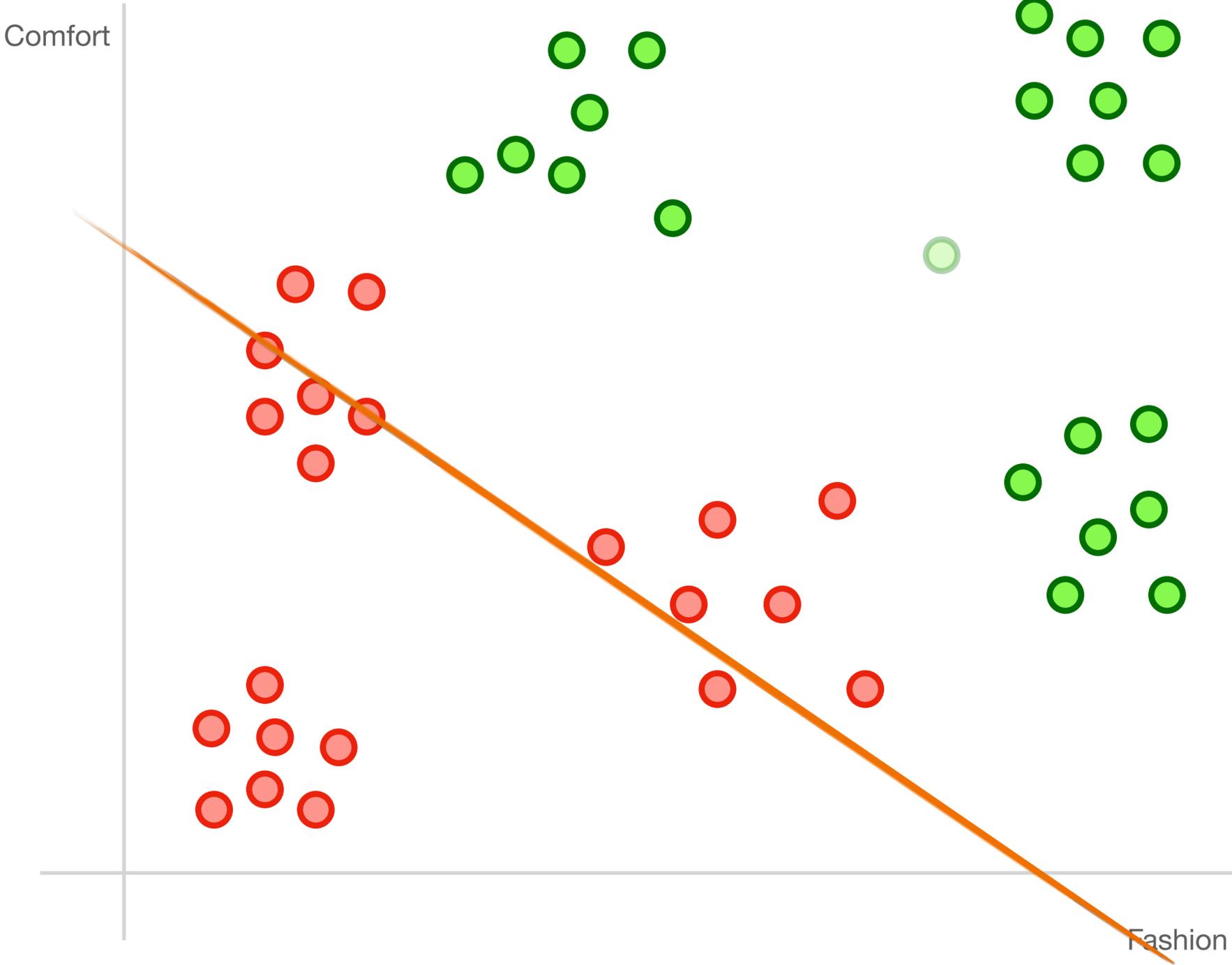
we need a more complex split

**Support vector machines!**

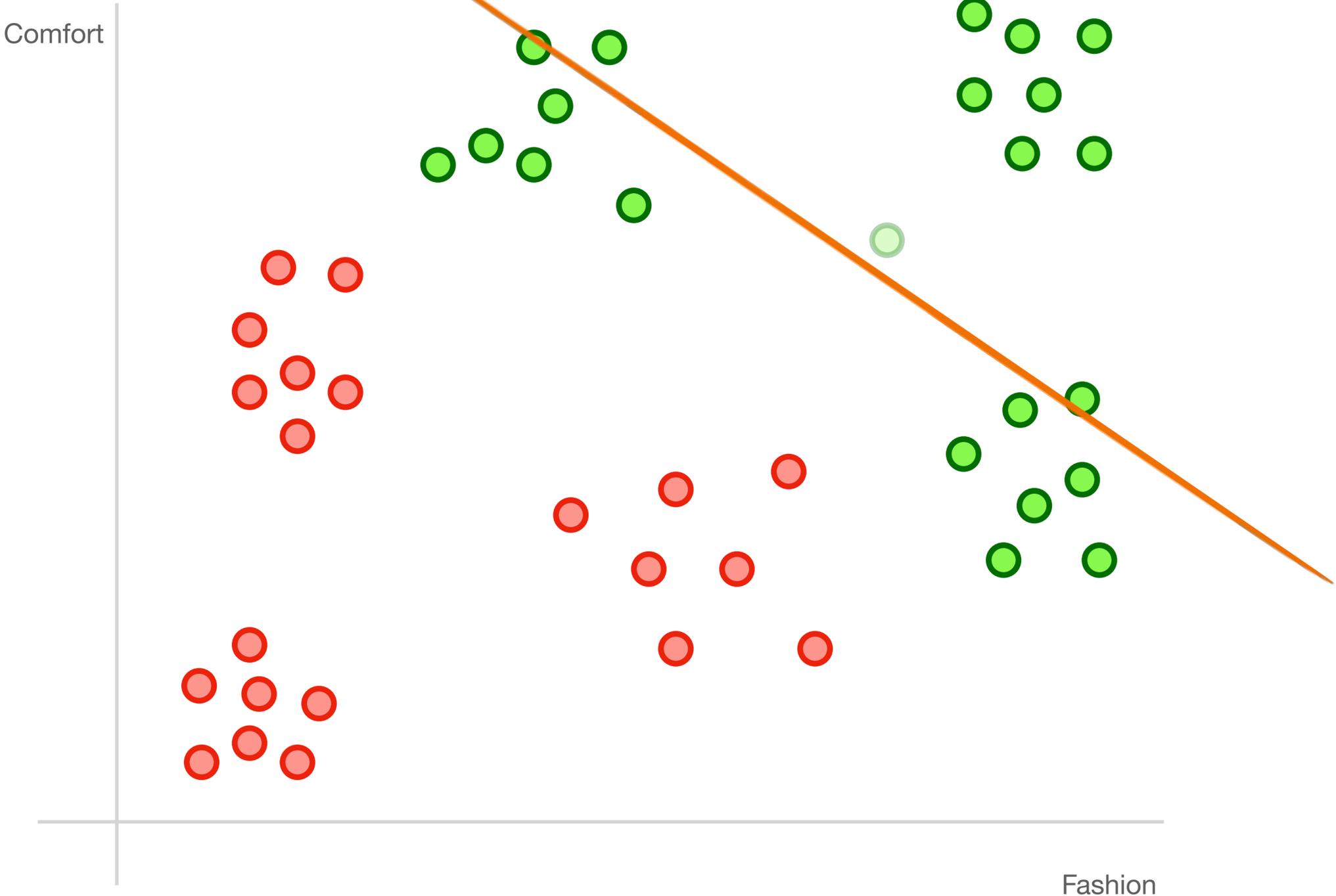
# Support Vector Machines



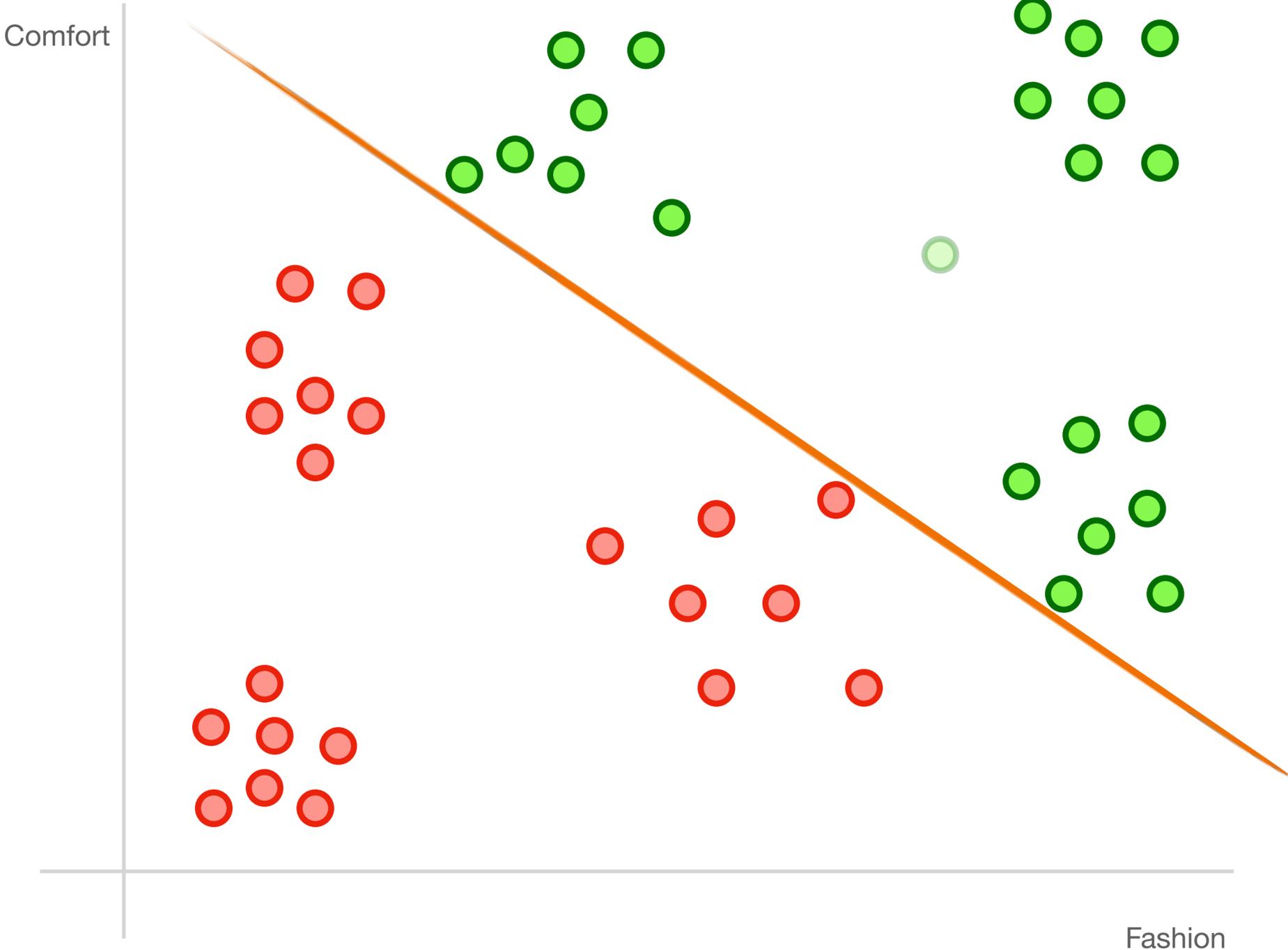
# Support Vector Machines

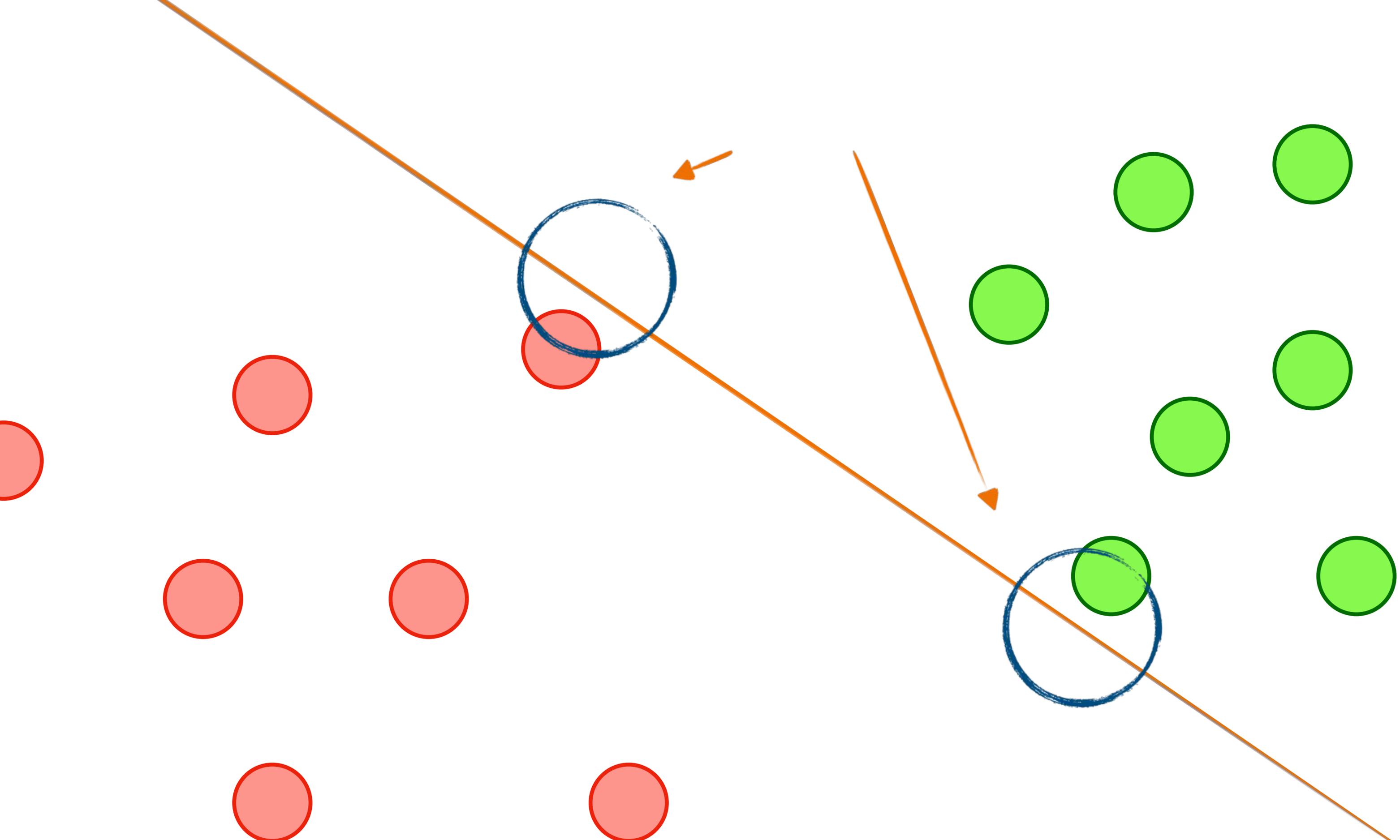


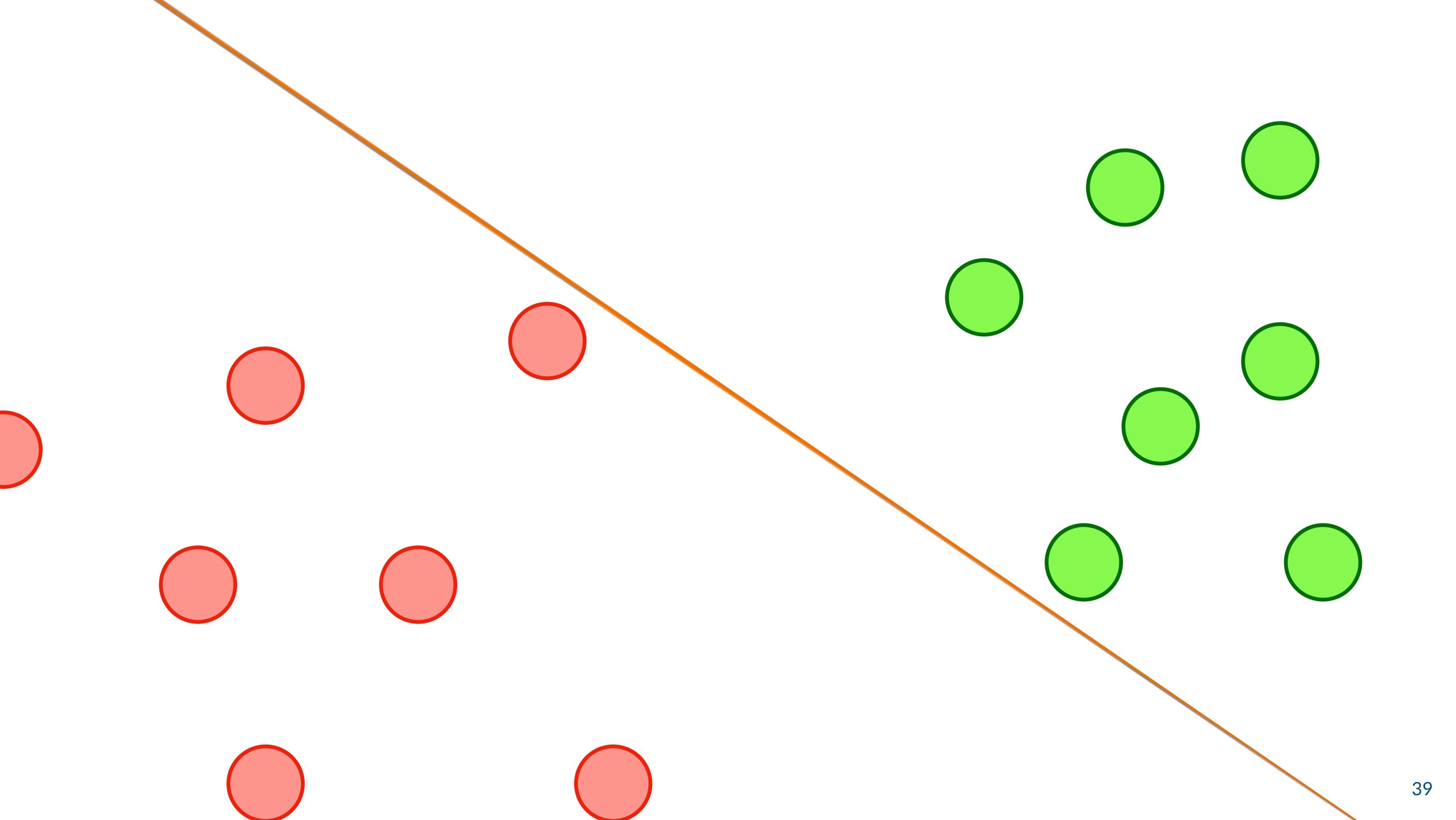
# Support Vector Machines

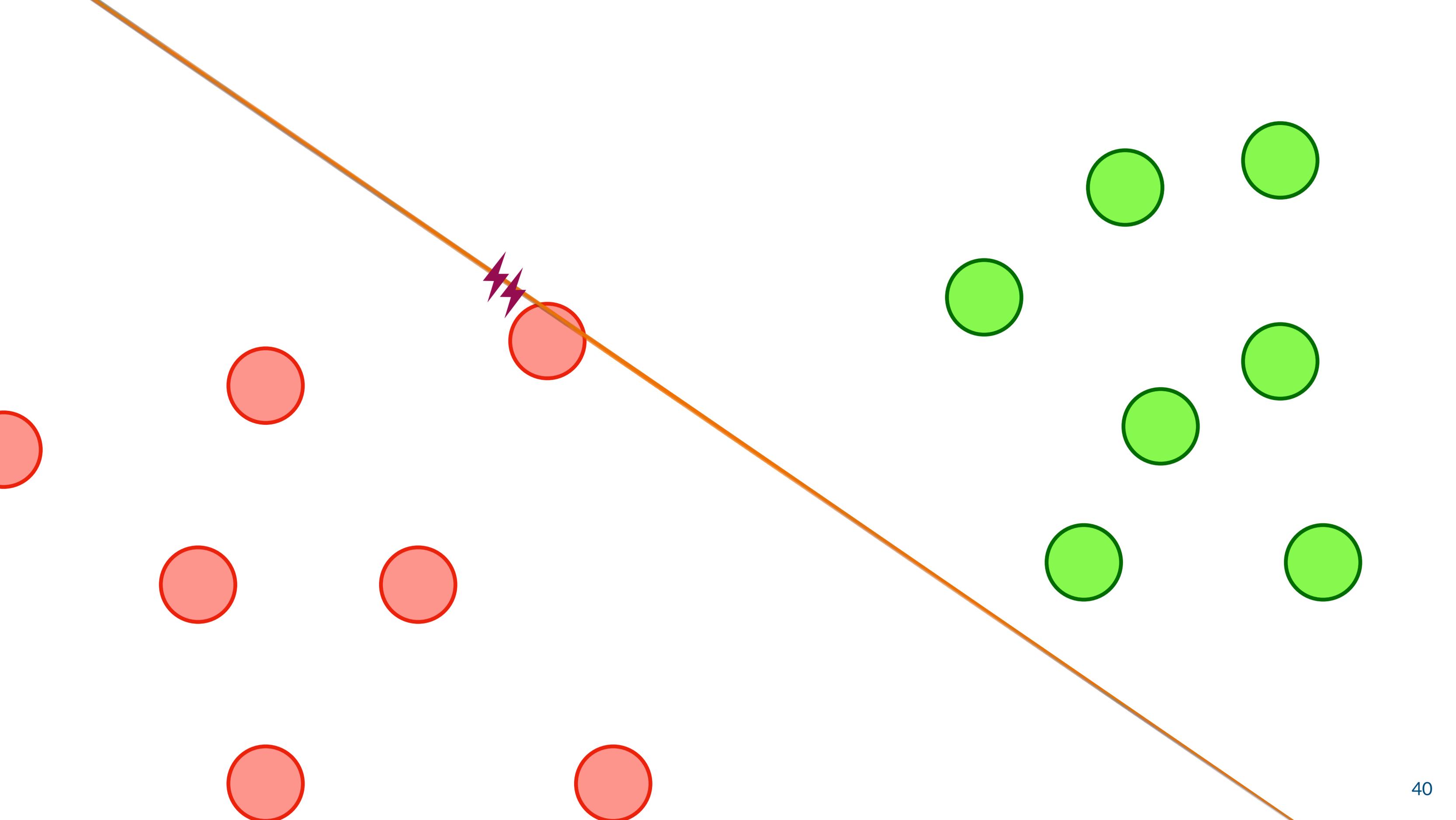


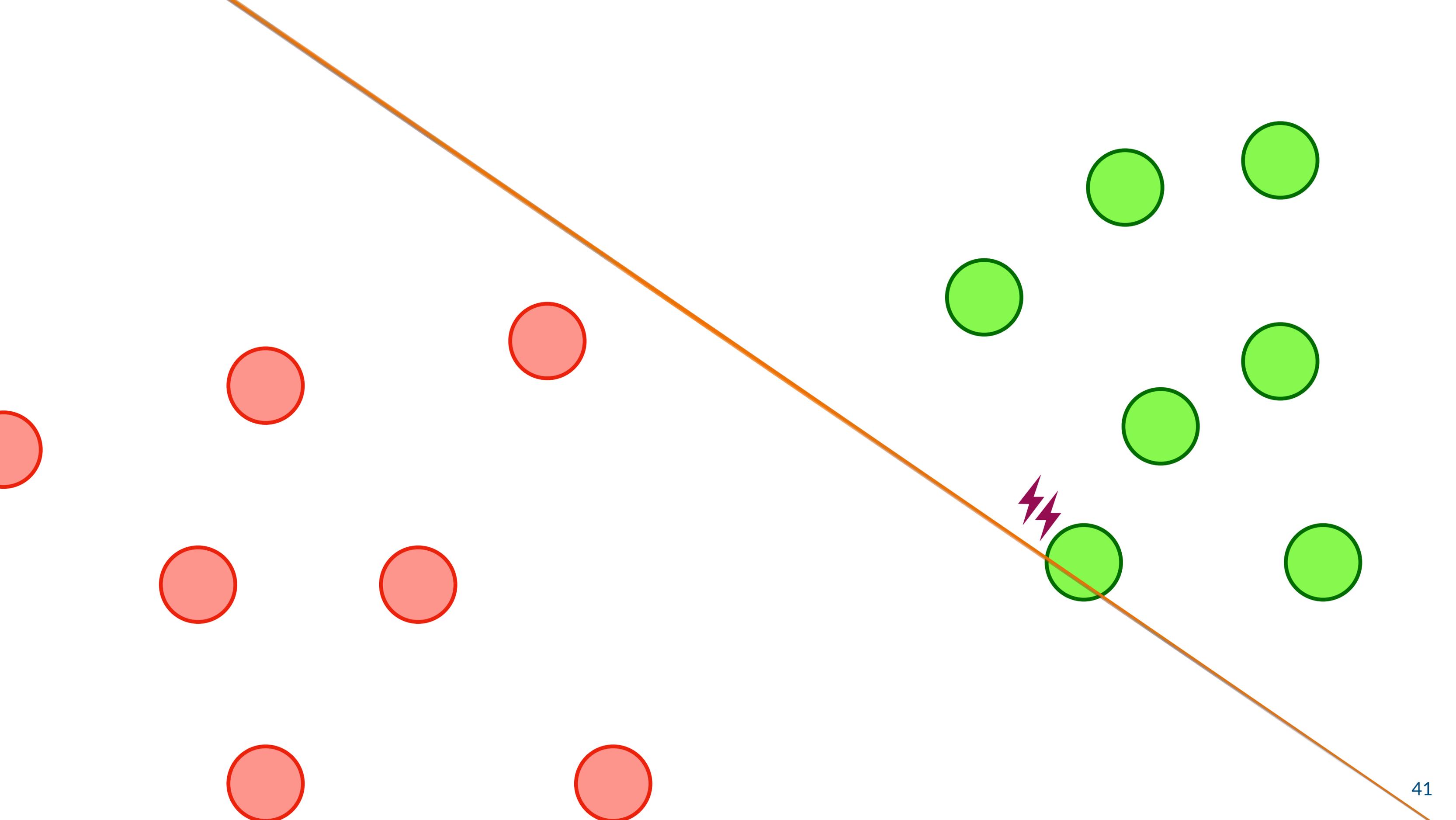
# Support Vector Machines



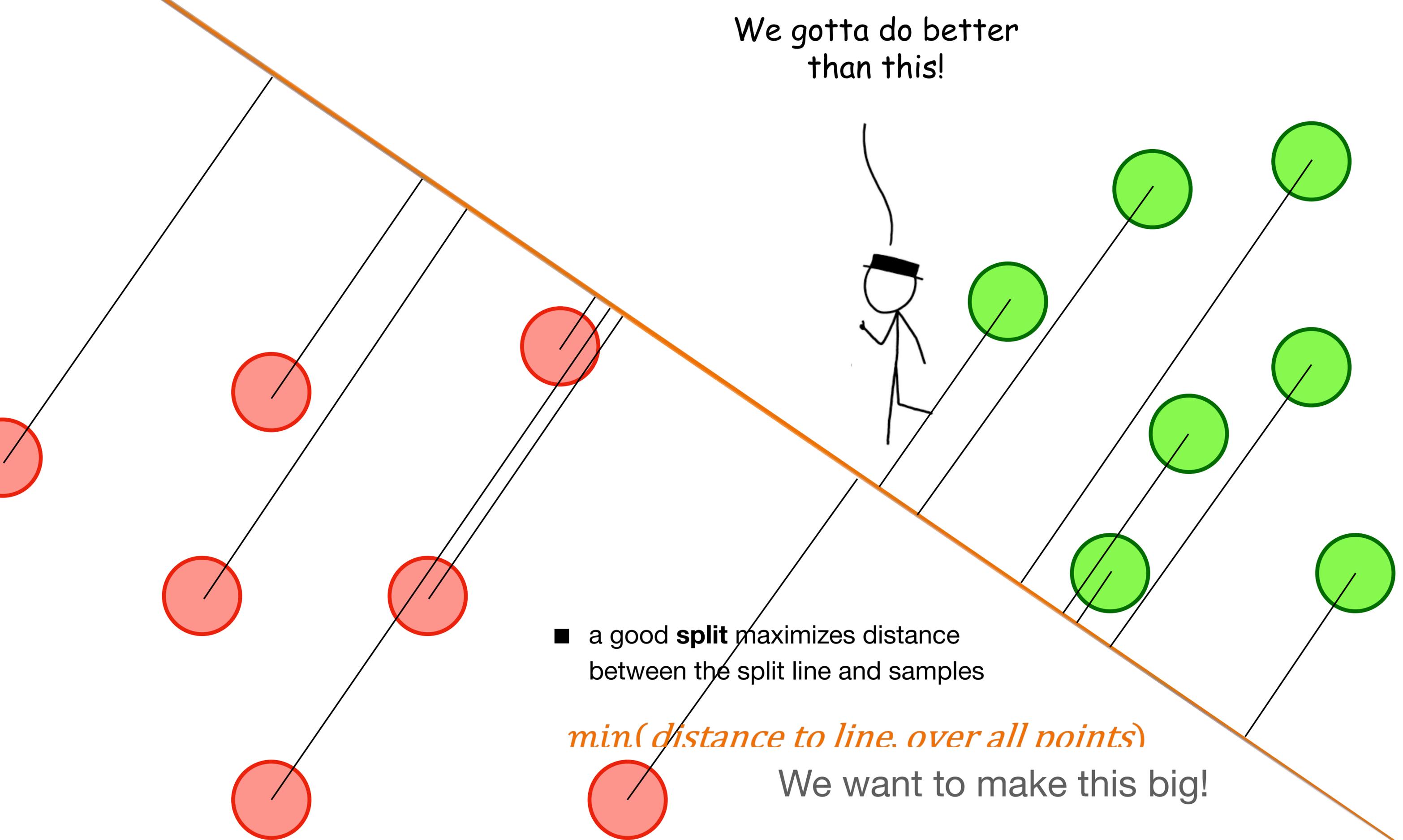








We gotta do better than this!



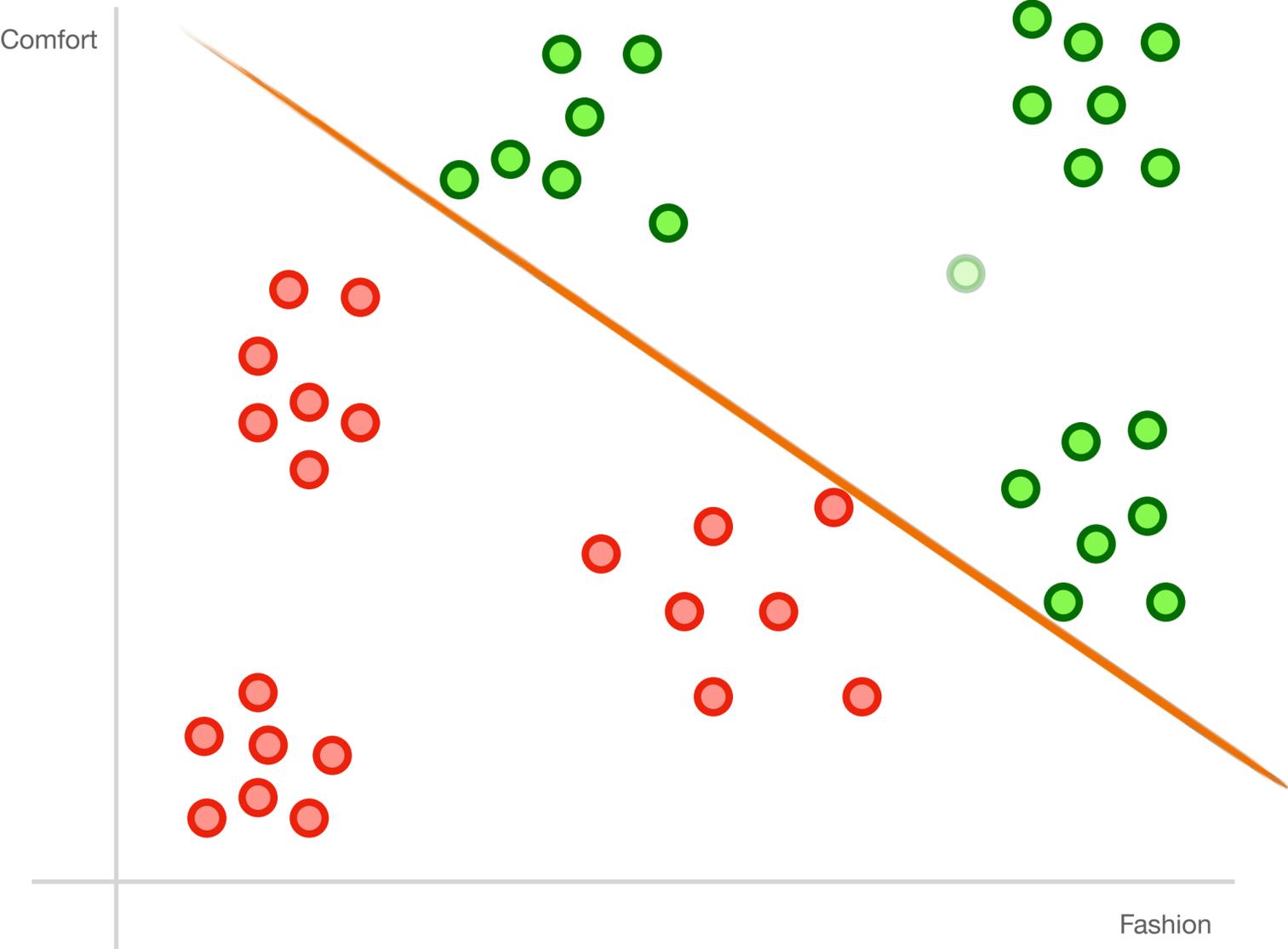
- a good **split** maximizes distance between the split line and samples

*min( distance to line. over all points)*

We want to make this big!

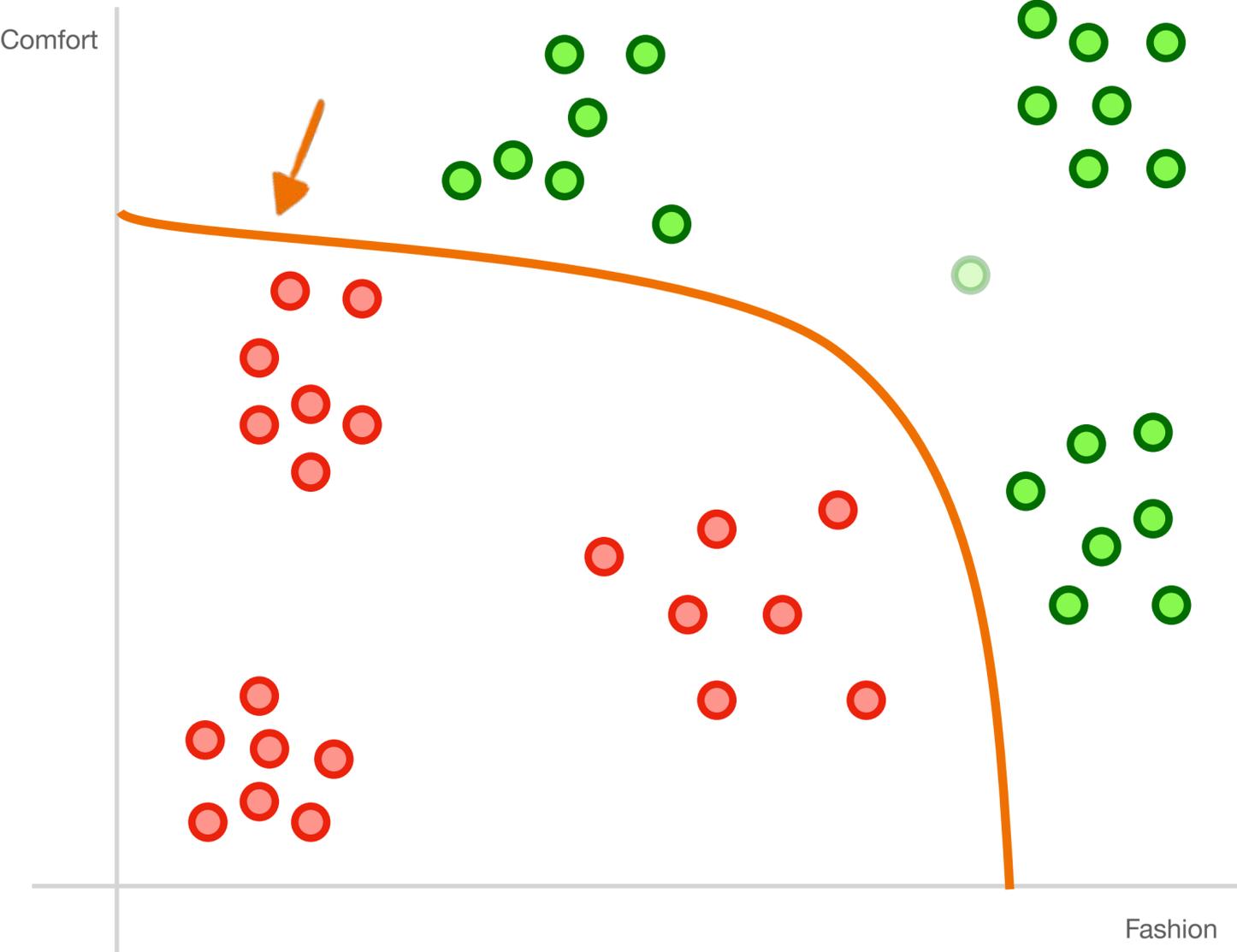
# Support Vector Machines

*min(distance to line, over all points)*  
We want to make this big!



# Support Vector Machines

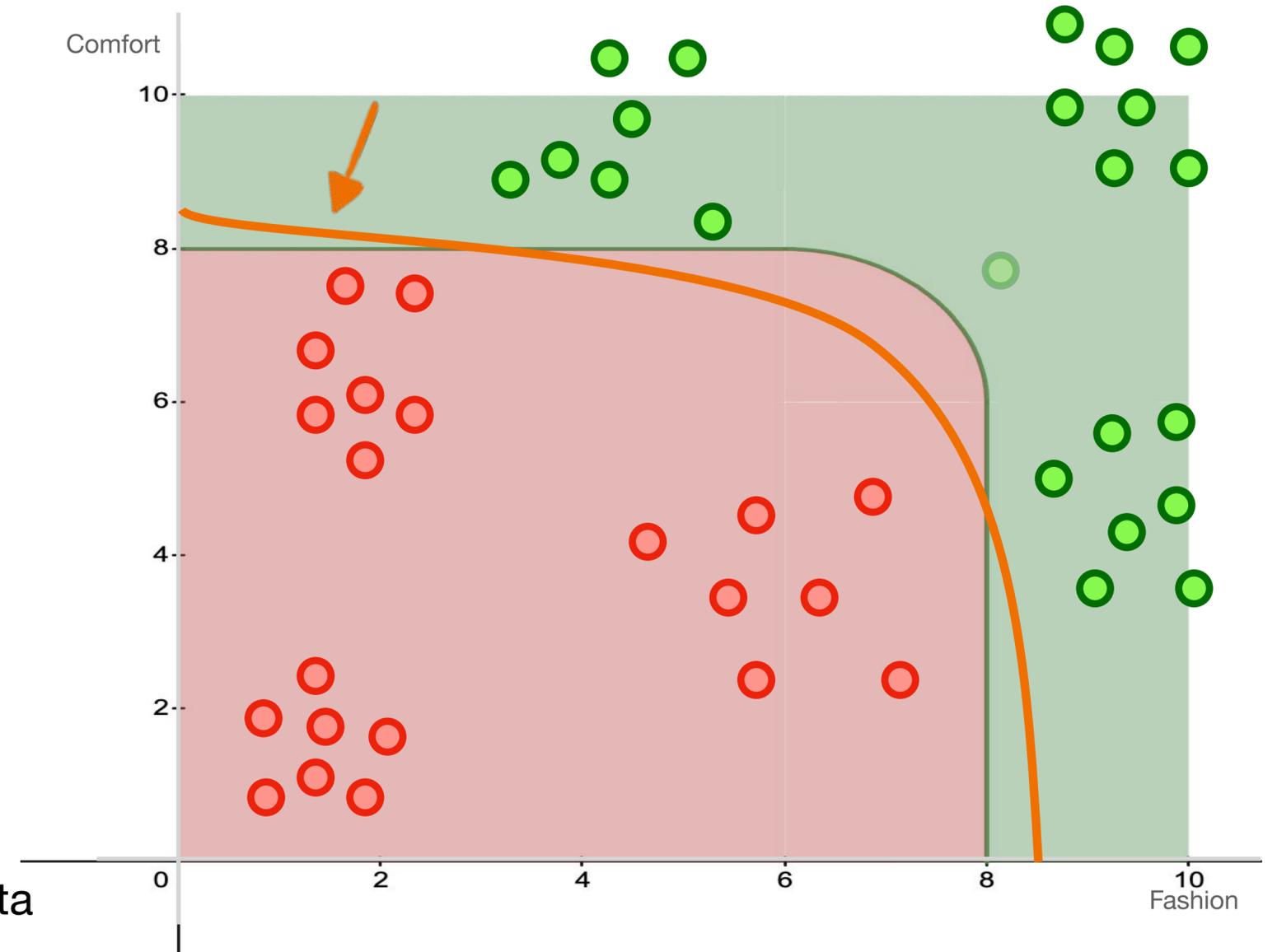
$\min(\text{distance to line, over all points})$   
We want to make this big!



# Support Vector Machines

*min(distance to line, over all points)*  
We want to make this big!

- **support-vector machines** are classifiers that divide data by class, aiming to create a **margin** that's as wide as possible.
- They can use non-linear functions



**Internal Memo:**

146 Hagley Road, Birmingham  
Birmingham B3 3PJ

From the Desk of  
Mr. Jerry Smith  
Date: 13/01/14

**Attn: Sir/Madam,**

I seize this opportunity to extend my unalloyed compliments of the new season to you and your family hoping that this year will bring more joy, happiness and prosperity into your house hold.

I am certain that by the time you read this letter I might have already gone back to my country **United Kingdom**. I visited South Africa during the New Year period and during my stay, I used the opportunity to send you this letter believing that it will reach you in good state.

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“unalloyed  
compliments”



Spam

“\$100,000  
dollars”



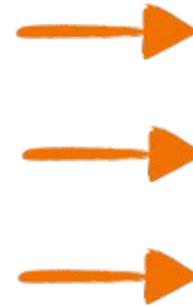
Spam

“relative dying of  
cancer”



Spam

**IF we have this**  
“unalloyed  
complements”  
“\$100,000  
dollars”  
“relative dying of  
cancer”



**we get this**  
Spam  
Spam  
Spam

**we get this IF we have this**

**we get this IF we have this**

***AIR***

**we get this IF we have this**

**A | B**

- **Is Spam**
- **“Nigerian Prince”**

we get this **IF** we have this

*spam* | *niaeriannc*

we get this **IF** we have this

$$P(\textit{spam} | \textit{nigerianprince})$$

high? Nigerian prince  $\longrightarrow$  spam likely

low? Nigerian prince  $\longrightarrow$  not spam

- **conditional probabilities** can be used as a classifier!

# Naïve Bayes

The diagram illustrates the Naïve Bayes formula for calculating the probability of an email being spam given the presence of the words 'nigerianprince'. The formula is:

$$P(\textit{spam}|\textit{nigerianprince}) = \frac{P(\textit{spam})P(\textit{nigerianprince}|\textit{spam})}{P(\textit{nigerianprince})}$$

Annotations with arrows:

- An arrow points from the text "% of spam in dataset" to the term  $P(\textit{spam})$ .
- An arrow points from the text "% of spam in dataset that relates to Nigerian prince" to the term  $P(\textit{nigerianprince}|\textit{spam})$ .
- An arrow points from the text "% of Nigerian prince in dataset" to the term  $P(\textit{nigerianprince})$ .

# Naïve Bayes

## Classifier

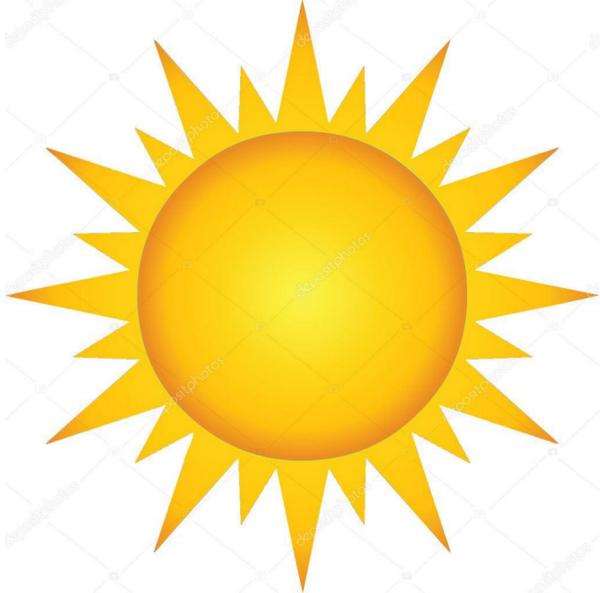
$$P(\textit{spam} | \textit{nigerianprince}, \textit{offer}) = \frac{P(\textit{spam})P(\textit{nigerianprince} | \textit{spam})P(\textit{offer} | \textit{spam})}{P(\textit{nigerianprince})P(\textit{offer})}$$



- **conditional probabilities** can be used as a
- **classifier** made this way, however, is “**naïve**” when extended to multiple features

“naïve”

# Naïve Bayes Independence



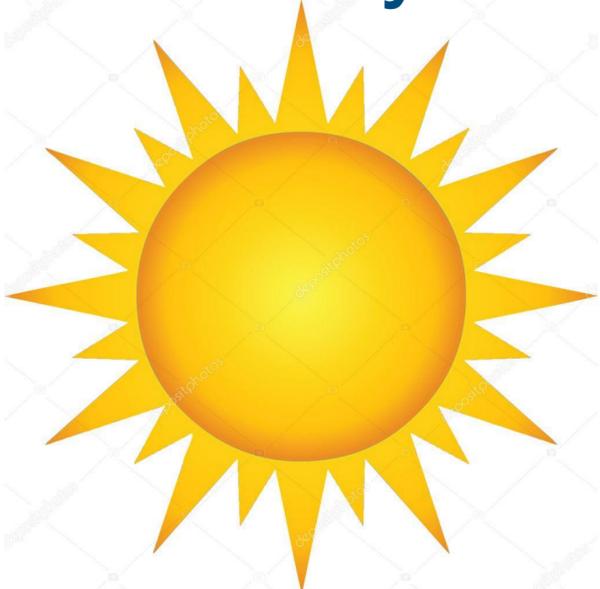
50%



50%

# Naïve Bayes Independence

January 1<sup>st</sup>

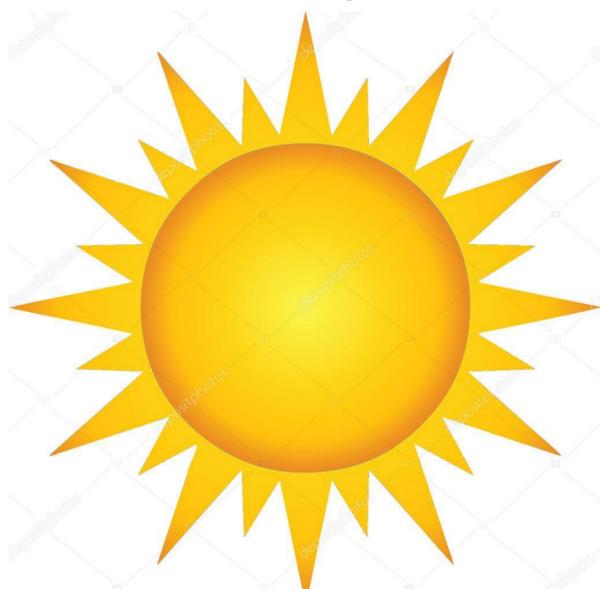


50%



50%

January 2<sup>nd</sup>



50%



50%

# Naïve Bayes Independence

$$P(\text{Rain} \mid \text{January 1}^{\text{st}}) \\ = 50\%$$

$$P(\text{Rain} \mid \text{January 2}^{\text{nd}}) \\ = 50\%$$

# Naïve Bayes Independence

$$P(\text{Rain} \mid \text{January 1}^{\text{st}} \text{ AND } \text{Rain} \mid \text{January 2}^{\text{nd}}) = 45\%$$

**Is NOT**

$$P(\text{Rain} \mid \text{January 1}^{\text{st}}) * P(\text{Rain} \mid \text{January 2}^{\text{nd}}) \\ = 25\%$$

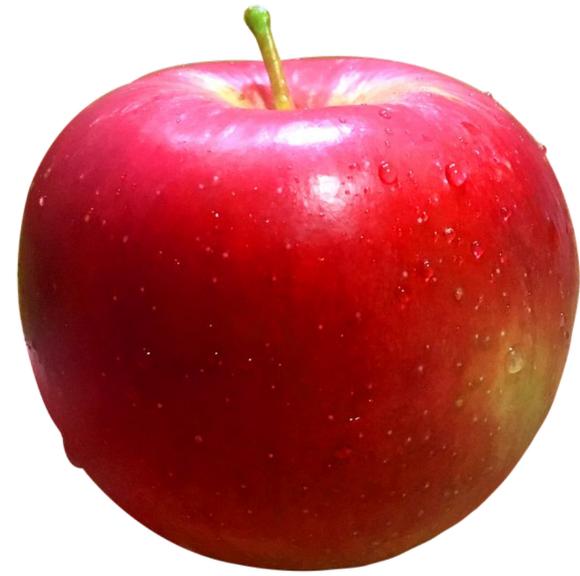
# Naïve Bayes Classifier

$$P(\textit{spam} | \textit{nigerianprince}, \textit{offer}) = \frac{P(\textit{spam})P(\textit{nigerianprince} | \textit{spam})P(\textit{offer} | \textit{spam})}{P(\textit{nigerianprince})P(\textit{offer})}$$



- **conditional probabilities** can be used as a
- **classifier** made this way, however, is “**naïve**” when extended to multiple features

“naïve”



Buy?

Don't buy?



Did Buy



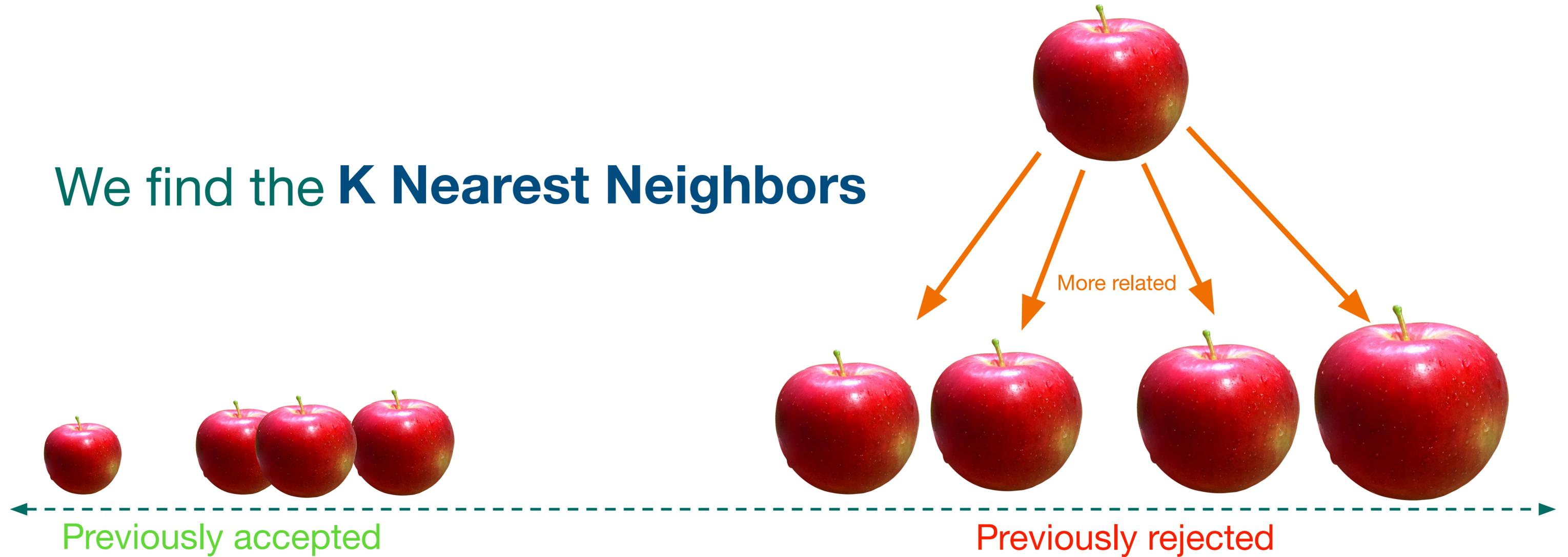
Rejected



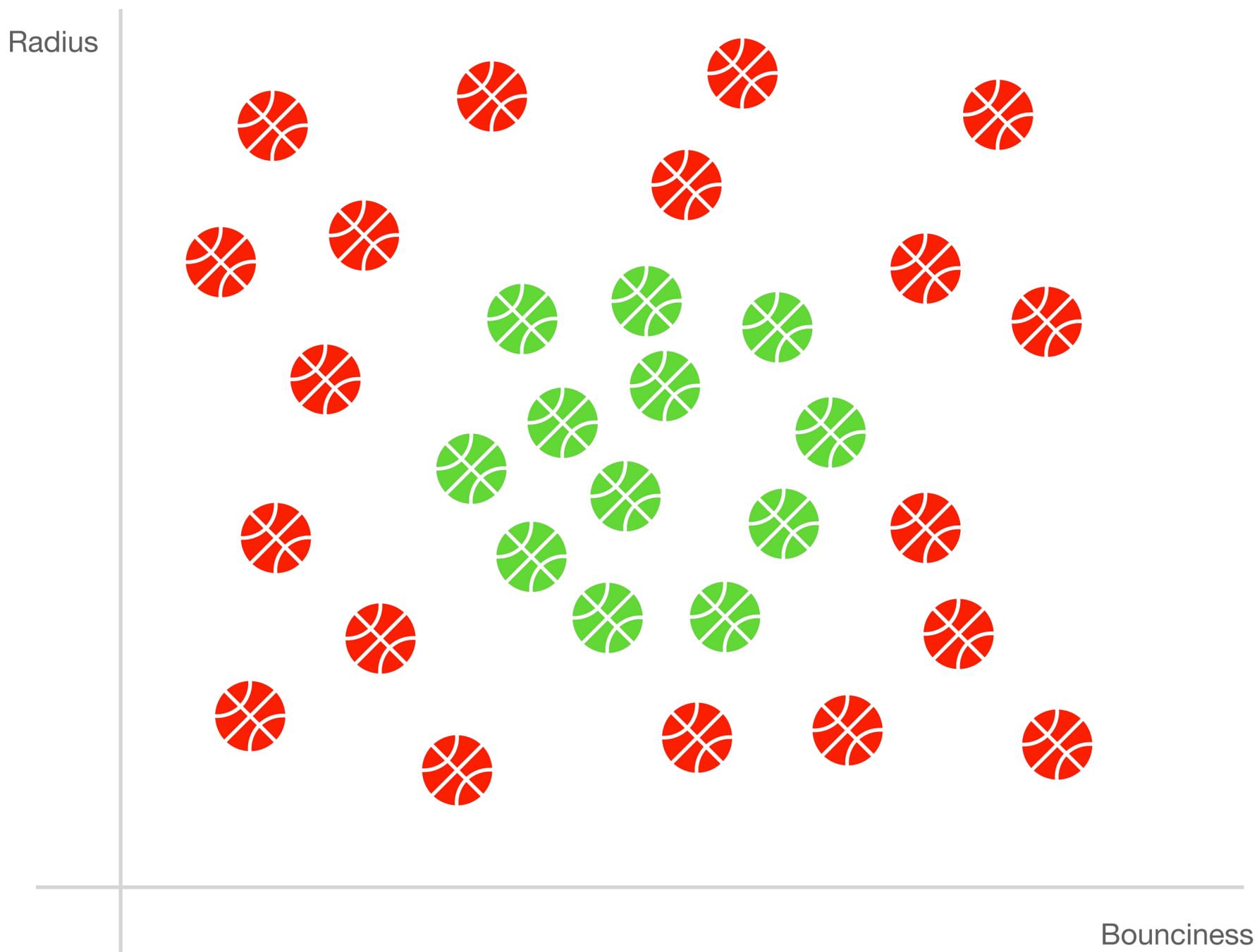
Previously accepted

Previously rejected

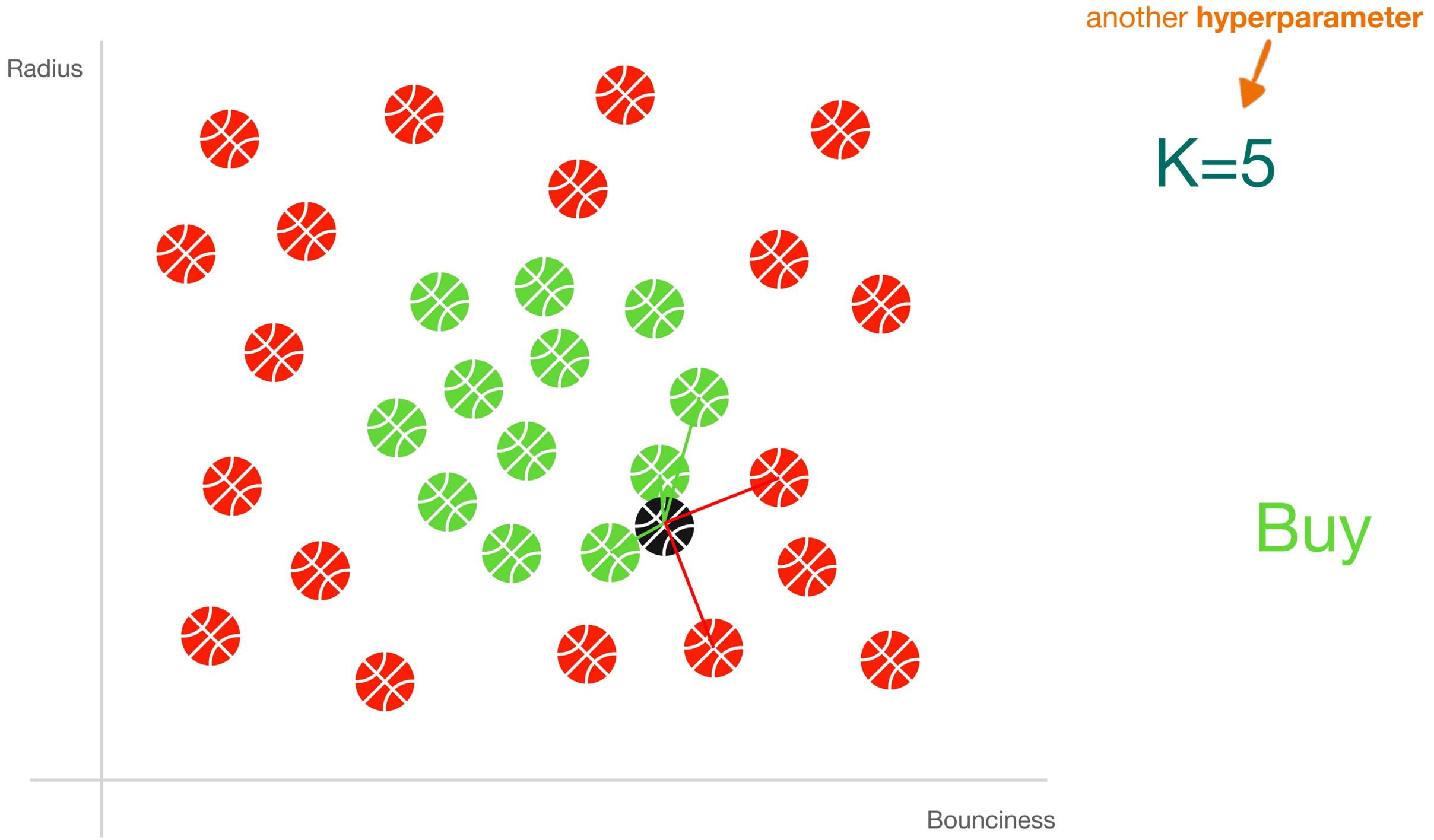
# We find the **K Nearest Neighbors**



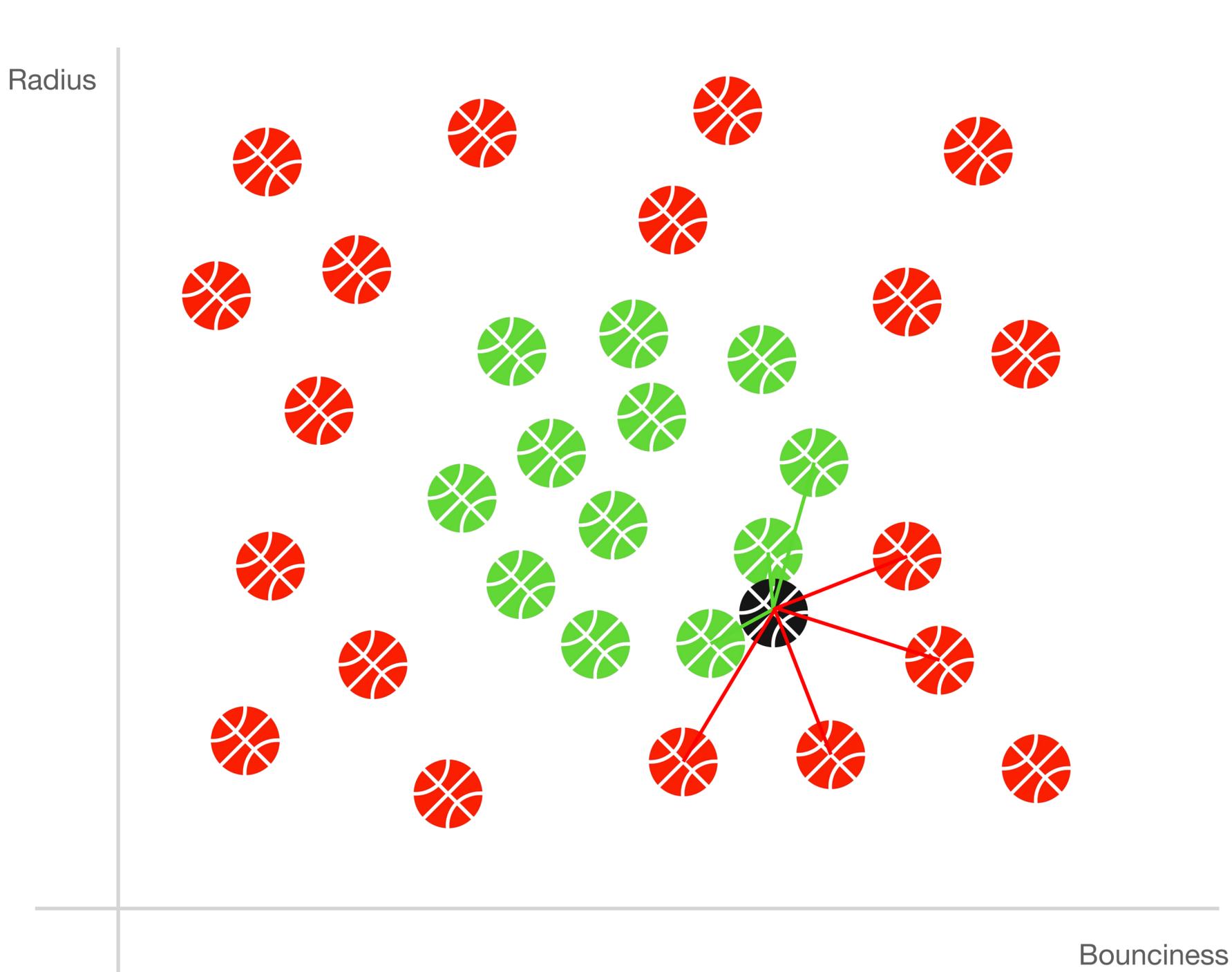
# K Nearest Neighbors



# K Nearest Neighbors



# K Nearest Neighbors



another hyperparameter



$K=7$

Don't Buy

**Five classifiers! That's a lot.**  
**Let's get to the lab!**